

# *In vivo* liver tracking with a high volume rate 4D ultrasound scanner and a 2D matrix array probe

Muyinatu A. Lediju Bell<sup>1,2</sup>, Brett C Byram<sup>2</sup>, Emma J Harris<sup>1</sup>, Philip M Evans<sup>1</sup>, Jeffrey C Bamber<sup>1</sup>

<sup>1</sup>Joint Department of Physics, Institute of Cancer Research and Royal Marsden Hospital, Sutton, Surrey SM2 5NG, UK

<sup>2</sup>Department of Biomedical Engineering, Duke University, Durham, NC 27708, USA

E-mail: [muyinatu.lediju@duke.edu](mailto:muyinatu.lediju@duke.edu)

**Abstract.** The effectiveness of Intensity Modulated Radiation Therapy (IMRT) is compromised by involuntary motion (e.g. respiration, cardiac activity). The feasibility of processing ultrasound echo data to automatically estimate 3D liver motion for real-time IMRT guidance was previously demonstrated, but performance was limited by an acquisition speed of 2 volumes per second due to hardware restrictions of a mechanical linear array probe. Utilizing a 2D matrix array probe with parallel receive beamforming offered increased acquisition speeds and an opportunity to investigate the benefits of higher volume rates. *In vivo* livers of three volunteers were scanned with and without respiratory motion at volume rates of 24 and 48 Hz, respectively. Respiration was suspended via voluntary **breath hold**. Correlation-based, phase-sensitive 3D speckle tracking was applied to consecutively-acquired volumes of echo data. Volumes were omitted at fixed intervals and 3D speckle tracking was reapplied to study the effect of lower scan rates. Results revealed periodic motion that corresponded with the heart rate or breathing cycle, in the absence or presence of respiration, respectively. For cardiac-induced motion, volume rates for adequate tracking ranged from 8-12 Hz and was limited by frequency discrepancies between tracking estimates from higher- and lower-frequency scan rates. Thus, the scan rate of volume data acquired without respiration was limited by the need to sample the frequency induced by the beating heart. In respiratory-dominated motion, volume rate limits ranged from 4-12 Hz, interpretable from the root mean squared deviation (RMSD) from tracking estimates at 24 Hz. While higher volume rates yielded RMSD values less than 1 mm in most cases, lower volume rates yielded RMSD values on the order of 2-6 mm.

*Keywords:* ultrasound, 3D speckle tracking, real-time image-guided radiotherapy (IGRT), motion-compensated radiotherapy

## 34 1. Introduction

35 Intensity modulated radiation therapy (IMRT) is a targeted treatment that shapes the  
36 treatment beam profile to deliver greater radiation doses to cancerous tumors and less  
37 to surrounding tissues. Involuntary motion during IMRT (e.g. respiration, cardiac  
38 activity) compromises effectiveness, due to the risk of geometric miss. The current  
39 state of estimating liver motion for radiotherapy treatment planning is to acquire x-  
40 ray computerized tomography (CT) scans of the liver for a predetermined time period,  
41 prior to treatment. The resulting information is used to create a target volume that  
42 administers greater radiation doses to all places where the tumor has moved, an approach  
43 inherently damaging to non-cancerous tissue (Balter et al. 1996). A more detailed  
44 assessment of tumor displacement could lead to reduced planning target volumes (PTVs)  
45 and thereby limit damage to normal healthy tissue.

46 **Liver motion that occurs over the time period of days is referred to as interfraction**  
47 **motion, whereas intrafraction motion occurs during the course of a 30-min. treatment**  
48 **session. The latter type of motion is the focus of this study, where mean peak-to-trough**  
49 **displacements span 5-40 mm in the superior-inferior direction under normal respiratory**  
50 **conditions (Davies et al. 1994, Suramo et al. 1984, Langen & Jones 2001). Intrafraction**  
51 **motion-compensation methods to reduce PTVs range from real-time fluoroscopy or CT**  
52 **tumor tracking to respiratory gating and controlled breathing (Case et al. 2010, Kubo &**  
53 **Hill 1996, Mageras & Yorke 2004, Dawson et al. 2001, Kitamura et al. 2003). Limitations**  
54 **of these techniques include the invasiveness of inserting fluoroscopic markers into the**  
55 **body (Shirato et al. 2000), additional doses to patients due to radiographic imaging**  
56 **(Murphy et al. 2007), irregular liver motion (von Siebenthal et al. 2007), and the**  
57 **exclusion of patients physically unable to withstand respiratory protocols (Mageras &**  
58 **Yorke 2004, Dawson et al. 2001, Eccles et al. 2006). Real-time tumor tracking with**  
59 **ultrasound does not suffer from these limitations.**

60 The feasibility of using ultrasound to track tumors and guide radiation therapy  
61 has previously been studied. Bouchet et al. (2001) have shown that it is possible  
62 to reliably transform ultrasound image coordinates into treatment room coordinates,  
63 eliminating the need for probe orientation to be consistent with standard anatomical  
64 axes. Hsu et al. (2005) demonstrated that positioning a linear array ultrasound probe  
65 to obtain suitable images of treatment regions is possible without significantly affecting  
66 radiation dose distribution. Motion tracking performance with this probe did not suffer  
67 from ultrasound image noise caused by the radiotherapy linear accelerator **and was not**  
68 **compromised by the probe pressure required to achieve reasonable acoustic contact.**  
69 **Multi-beam treatment plans and a mock transducer set-up during treatment planning**  
70 **were the respective solutions to conflicting probe and radiation beam positions and**  
71 **tissue deformations caused by the transducer (Hsu et al. 2005).**

72 A mechanical rocking linear array probe was used to evaluate 3D tracking

73 performance in tissue-mimicking phantoms (Harris et al. 2007, Harris et al. 2010) and  
74 *in vivo* livers (Harris et al. 2010). However, the scanning acquisition rate was limited to 2  
75 volumes per second (2 Hz), due to hardware restrictions of the mechanical probe. These  
76 hardware restrictions limited speckle tracking accuracy and precision to the extent that  
77 adequate performance *in vivo* was obtained only when tracking blood vessel features  
78 (Harris et al. 2010). Further studies on phantoms indicated that poor performance in  
79 tracking fully developed speckle *in vivo* may be due to speckle decorrelation caused by  
80 elevational tissue motion (Harris et al. 2011).

81 The availability of a 2D matrix array probe (Frey & Chiao 2008) connected to  
82 a highly parallel receive-beam count scanner (Ustuner 2008) alleviated many of the  
83 restrictions associated with prior studies. This 4D ultrasound system was previously  
84 operated at 1000 Hz to track 3D displacements in a tissue-mimicking phantom and in *in*  
85 *vivo* cardiac data (Byram et al. 2010). The present study utilizes this system to assess  
86 contributions of high volume rates when tracking liver motion. **Respiration is a primary**  
87 **contributor to intrafraction liver motion in IMRT treatment plans that allow patients to**  
88 **breathe normally. Likewise, liver motion due to cardiac and/or cardiovascular activity**  
89 **is of key importance in radiotherapy strategies that involve active breathing control**  
90 **and respiratory gating (Dawson et al. 2001, Wurm et al. 2006). To provide a complete**  
91 **analysis of appropriate volume sampling rates for ultrasonic guidance of a broad range of**  
92 **radiotherapy procedures, liver displacements during free breathing and voluntary breath**  
93 **hold are evaluated.**

94 Motion tracking of ultrasound data is performed by applying correlation-based  
95 techniques to track an intrinsic property of ultrasound images known as speckle  
96 (Embree 1986). It is hypothesized that volume rates for adequate tracking of 3D  
97 ultrasound sector-scan data should be sufficient to restrict intervolum displacement to  
98 a few millimeters to minimize ultrasonic speckle decorrelation due to angular changes in  
99 tissue orientation (Bamber et al. 1996, Meunier 1998). Adequate volume rates are also  
100 dependent on the frequency of periodic liver motion. This study investigates if greater  
101 rates than those required by sampling theory are necessary to overcome intervolum  
102 speckle decorrelation.

## 103 2. Methods

### 104 2.1. Data Acquisition

105 A Siemens (Siemens Healthcare Sector, Ultrasound Business Unit, Mountain View, CA)  
106 SC2000 ultrasound scanner (Ustuner 2008) and 4Z1c matrix phased array transducer  
107 (Frey & Chiao 2008) were used to acquire 4D raw, baseband-format in-phase and  
108 quadrature (IQ) sampled echo data of *in vivo* livers from three healthy volunteers.  
109 Volunteers were scanned in the supine position on a gurney. The transducer was  
110 positioned subcostally, with its lateral direction aligned approximately with the  
111 transverse plane of the body and angled to obtain suitable views of Couinaud liver

112 segments IV, V, and VIII. It was affixed to the gurney via a flexible arm (Chicago  
 113 Brand, model CB-50220, Fremont, CA) and custom-built probe holder. The flexible  
 114 arm became rigid when locked in position once the desired orientation was achieved.

115 The transmit center frequency was 2.8 MHz. The transmit focus was 8 cm. The  
 116 baseband IQ echo signal was sampled at 2.5 MHz. The combined effect of this level of  
 117 transmit focusing and parallel receive beamforming resulted in pulse-echo lateral and  
 118 elevational resolutions that were approximately 2.5 mm at the 8 cm focal depth. The  
 119 lateral and elevation beam spacings were approximately  $1^\circ$  (i.e. 1 lateral or elevation  
 120 sample is approximately  $1^\circ$ ).

121 To evaluate cardiac-induced displacements, volunteers were asked to inhale and  
 122 hold their breaths during a 3-s acquisition at a volume acquisition rate of 48 Hz. This  
 123 was the maximum amount of data that could be stored on the system buffer for the  
 124 chosen volume configuration of 450 axial samples x 24 lateral samples x 30 elevation  
 125 samples (13.8 cm x 5.8 cm x 7.2 cm sector scan). The volunteers were asked not to move  
 126 but were allowed to breathe normally, while data were transferred for offline analyses  
 127 and the transducer remained locked in position. Subsequently, data was acquired under  
 128 normal respiratory conditions for approximately 6 s at a volume rate of 24 Hz, which  
 129 was the scanner’s buffer limit for the above-stated volume size and volume acquisition  
 130 rate. These data were transferred for offline analyses. Synchronized ECG traces were  
 131 recorded for each acquisition.

## 132 *2.2. Data Analyses*

133 Motion tracking was implemented with a phase-sensitive, normalized cross-correlation  
 134 3D speckle tracking algorithm (Wear 1987, O’Donnell et al. 1994) that was previously  
 135 tested and validated with phantom experiments (Byram et al. 2010). This algorithm  
 136 was applied to the acquired data, before scan conversion. A 3D kernel in one volume is  
 137 specified and the vector describing the location of the best pattern match to that kernel  
 138 in a consecutively-acquired volume is considered the 3D intervolum displacement of  
 139 that kernel. This process was repeated for all possible kernel locations in a volume and  
 140 all volumes in a data set.

141 The kernel size used in this study was 15 axial samples x 4 lateral samples x 4  
 142 elevation samples, **which corresponds to the approximate size of two speckles at the**  
 143 **focus**. Unless otherwise stated, the search region was limited to 67 axial samples x 24  
 144 lateral samples x 26 elevation samples and was centered about the kernel location. **The**  
 145 **size of the search region was determined by the maximum size needed to find at least**  
 146 **twice the maximum intervolum displacement observed in the three dimensions of the**  
 147 **focal region of all data sets**. The grid slopes subsample estimator (Geiman et al. 2000)  
 148 was used to refine displacement estimates in the lateral and elevation dimensions.

149 Displacement maps were generated for axial-lateral, axial-elevation, and lateral-  
 150 elevation scan planes. One pixel in a displacement map represents the displacement  
 151 estimate of one kernel. Maps are available for each of the three components of

152 displacement and for every two sequentially-acquired volumes in a data set (i.e. as  
153 a function of time).

154 Motion was analyzed in a 3D region of interest (ROI) containing several pixels of  
155 displacement data from the different displacement maps. The ROI was centered about  
156 the focal depth of 8 cm and was arbitrarily chosen to measure 20 pixels (axial) x 7  
157 pixels (lateral) x 5 pixels (elevation), which is approximately 6.2 mm x 9.8 mm x 7.0 mm,  
158 respectively. Although lateral and elevational beamwidths increase with depth, the ROI  
159 size was small enough to use the paraxial approximation to assume constant beamwidth  
160 within the ROI. Pixel displacements were converted to units of meters via the use of  
161 a conversion coordinate transformation that was correct for the center of the ROI and  
162 assumed to be apply to all pixels within the ROI. The average and standard deviations  
163 of displacements within the ROI were calculated. Average intervolumne displacements  
164 were cumulatively summed to determine liver motion as a function of time. The method  
165 of tracking between consecutive volumes and cummulatively summing displacements  
166 was previously referred to as “incremental tracking”, while “non-incremental tracking”  
167 was used to denote tracking with a fixed reference frame (Bamber et al. 1996, Harris  
168 et al. 2007, Harris et al. 2010). Non-incremental tracking was explored for this study,  
169 but the resulting standard deviation of displacement estimates within a ROI were  
170 significantly larger (due to larger intervolumne decorrelation than that achieved with  
171 incremental tracking), and thus only the results for incremental tracking are reported.

172 To study the effect of decreased volume rates, relevant volumes in a data set were  
173 omitted at fixed intervals and 3D speckle tracking was re-applied. As volume rates  
174 decrease, errors due to false peaks increase (Byram et al. 2010). This type of error  
175 occurs when secondary peaks in the correlation function are higher than the true peak,  
176 yielding false estimates for a translated kernel location. When such errors occur at  
177 isolated displacement pixel locations, or for small clusters of displacement pixels, they  
178 may be detected and replaced by median filtering (Doyley et al. 2001). A 9x5 (axial  
179 x lateral) median filter was applied to displacement maps in the axial-lateral plane.  
180 Filtered and unfiltered displacement maps were analyzed as described above. All data  
181 processing was implemented with Matlab software (The Mathworks, Inc., Natick, MA).

## 182 3. Results

### 183 3.1. Cardiovascular-induced motion

184 A triplanar view of *in vivo* liver ultrasound data from Volunteer 1 is displayed in Fig. 1  
185 (a). Displacement tracking of sequentially-acquired volumes of breath-hold ultrasound  
186 data resulted in relatively uniform displacement fields in most cases. This uniformity is  
187 demonstrated in Figure 1 (b-d), which shows maps of displacement in the three selected  
188 planes, for each of the three displacement components (axial, lateral, and elevation), at  
189 the same point in time (i.e. at 1.52 s in Fig. 2).

190 Less uniform displacement fields were observed during periods of heightened cardiac

191 activity (i.e. 2.35 s in Fig. 2), as evidenced in Figure 1 (e-g). These displacement  
 192 maps illustrate the more pronounced spatial gradients and tissue transformations within  
 193 liver, due to cardiac activity. For example, the presence of positive, negative, and zero  
 194 displacements in axial displacement maps indicates deformation. Spatial gradients in  
 195 lateral and elevation maps represent shearing and rotation. Similar displacement maps  
 196 were mostly observed during periods of heightened cardiac activity, as dictated by the  
 197 QRS complex of a synchronously-acquired ECG trace. Similar results were achieved in  
 198 all volunteers.

199 Tracked intervolumetric displacements within a 3D ROI at the same location in axial,  
 200 lateral, and elevation displacement maps were averaged and cumulatively summed.  
 201 Average displacement as function of time is illustrated in Figure 2 (a). These  
 202 displacements are attributed to cardiac activity, as data were acquired during breath  
 203 hold. The corresponding ECG trace is shown in Figure 2 (b). Correlation coefficients  
 204 within the ROI were above 0.98 and varied as a function of time, having lower values  
 205 during periods of heightened cardiac activity, as depicted in Figure 2 (c). This trend  
 206 was observed in all volunteers.

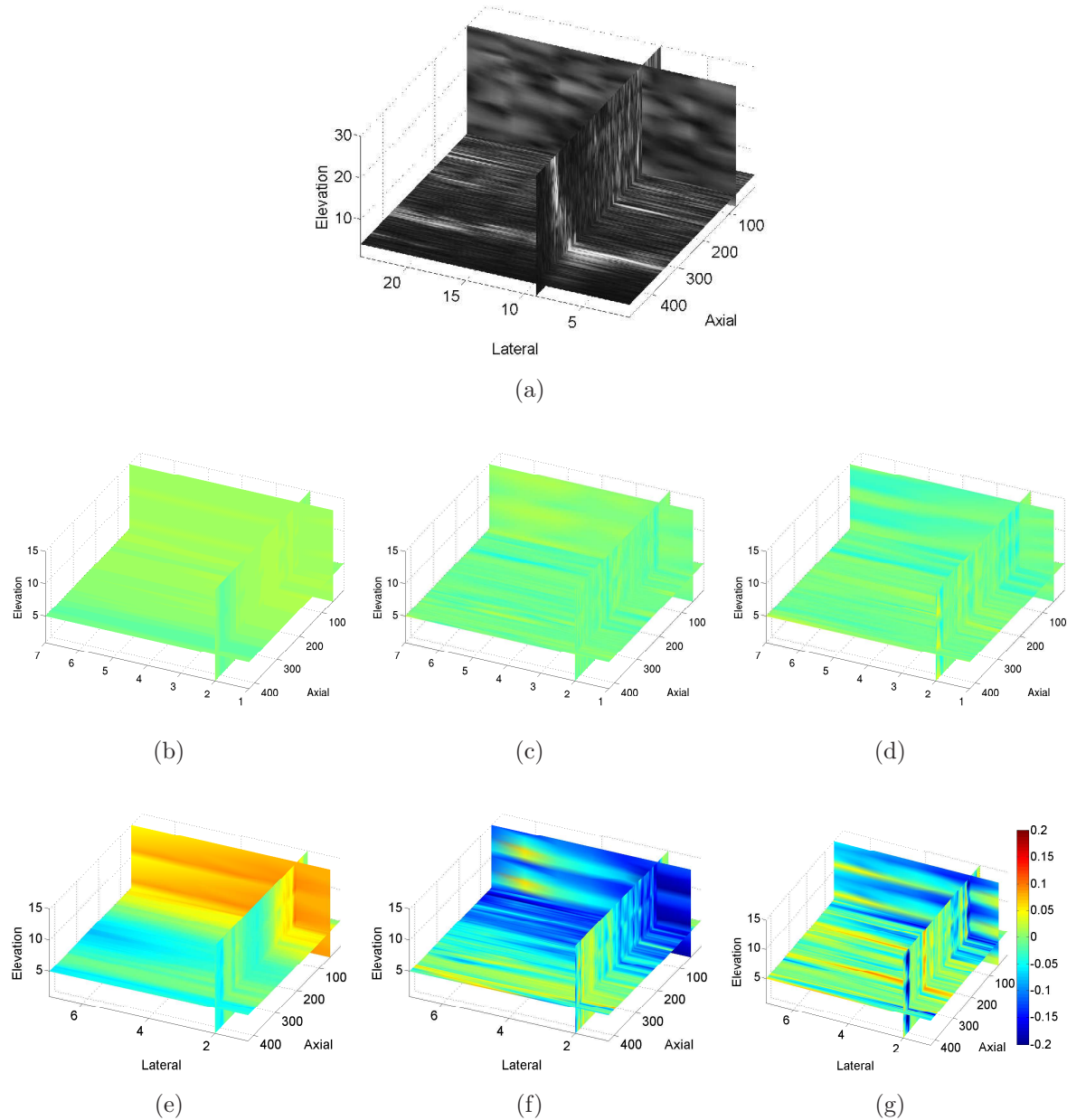
207 Relevant volumes were omitted and tracking was reapplied to study the effect of  
 208 decreased volume rates. Displacement as a function of time for the lower volume rates is  
 209 shown in Figure 3 for Volunteer 1, with the initial 48 Hz volume rate shown as a reference.  
 210 The top and bottom rows of Figure 3 respectively show axial, lateral, and elevation  
 211 displacement estimates before and after the median filtering of displacement maps. **The**  
 212 **mean absolute difference (MAD) between filtered and unfiltered displacement estimates**  
 213 **ranges from 7  $\mu\text{m}$  (at 48 Hz) to 70  $\mu\text{m}$  (at 4 Hz) for Volunteer 1, 9  $\mu\text{m}$  to 20  $\mu\text{m}$  for**  
 214 **Volunteer 2, and 6  $\mu\text{m}$  to 50  $\mu\text{m}$  for Volunteer 3.** In some instances (e.g. compare  
 215 3(a) and 3(d)), median filtering reconciles the displacements of lower volume rates with  
 216 that of higher volume rates and reveals that undersampling of the temporal displacement  
 217 waveform is a primary source of error. Although error bars are not shown, they became  
 218 larger at lower volume rates, indicative of the increased spatial variation observed within  
 219 the ROI. These results demonstrate that tracking is inadequate at volume rates of 2-4  
 220 Hz, where displacement estimates deviate from that of higher volume rates and/or the  
 221 periodic motion of the liver is undersampled.

222 Figure 4 (a) shows a histogram of correlation coefficients within the ROI used to  
 223 average displacements, computed at each volume rate for Volunteer 1. Although there  
 224 is some degree of overlap, the histogram reveals that lower correlation coefficients were  
 225 calculated at the lower volume rates. The histogram also confirms observations that the  
 226 minimum correlation coefficients for each volume rate, which occurred during periods of  
 227 heightened cardiac activity, decreased with decreasing volume rates. Similar histogram  
 228 trends were observed for all volunteers.

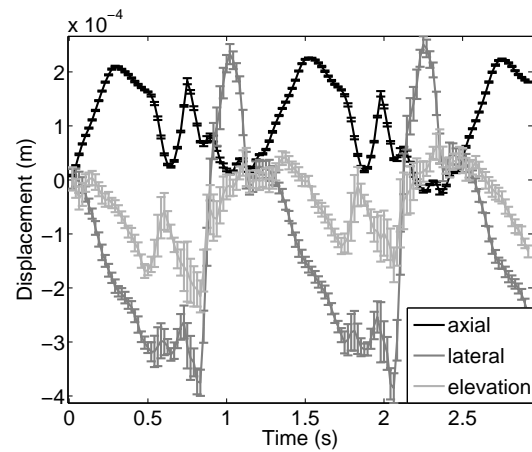
229 Figure 5 shows the mean correlation between tracked volumes of breath hold data  
 230 within the same ROI described above, as a function of volume rate for each volunteer.  
 231 Lower mean correlation coefficients at lower volume rates are observed for all volunteers.

232 To compare expected and measured displacement estimates for the lower

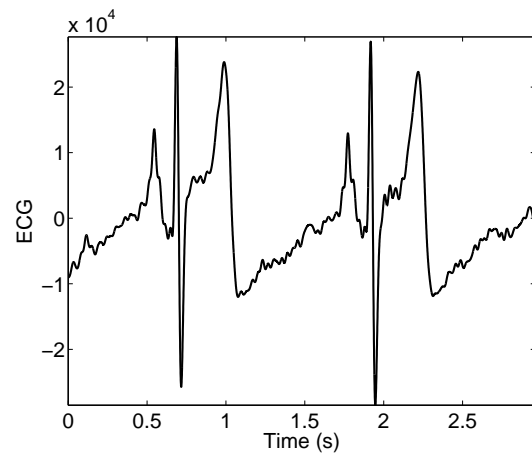




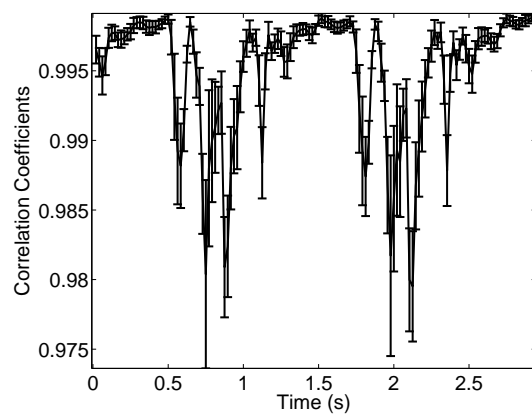
**Figure 1.** Triplanar views of (a) ultrasound data and corresponding (b,e) axial, (c,f) lateral, and (d,g) elevation displacement maps. The three displacement components in each row are displayed for the same point in time. The first row shows displacement fields at the 1.52-s time point in Fig. 2. The second row shows the displacement fields at the 2.35-s time point in Fig. 2. The spatial scale is pixels. The displacement scale is millimeters. **One pixel in the displacement map corresponds to the displacement of one kernel of ultrasound data. The displacement maps have fewer pixels than the ultrasound image because the speckle-tracking algorithm was not applied to kernels near the boundaries of the B-mode image, where the search region extends beyond the image boundary. The search region for these images was reduced to 61 axial samples x 18 lateral samples x 26 elevation samples to show more lateral and elevational extent in the displacement maps. These displacement maps were not median filtered.**



(a)



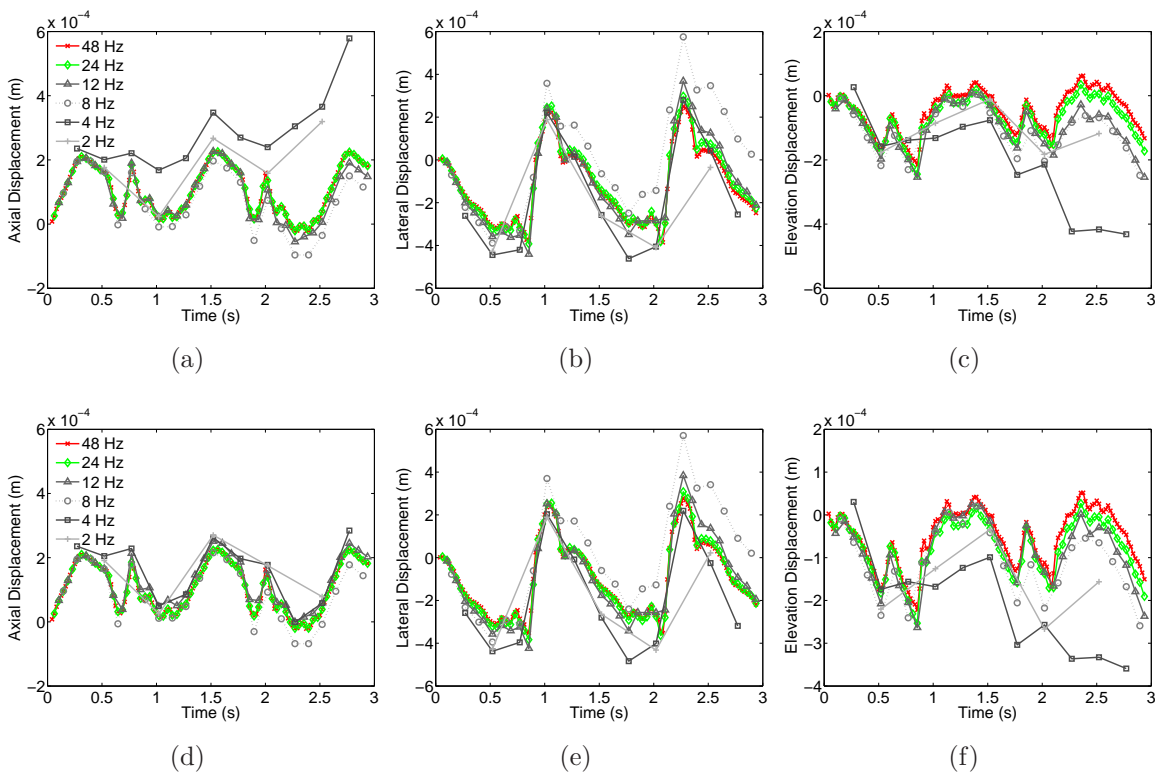
(b)



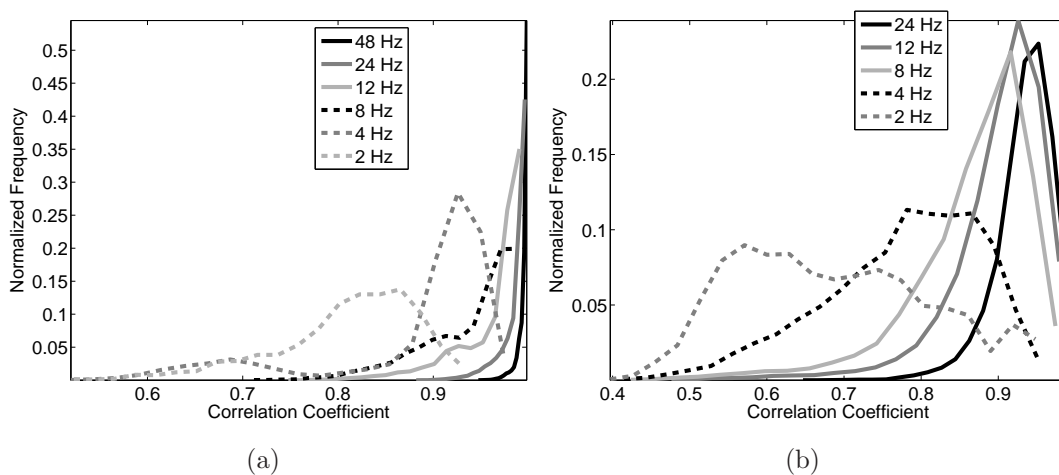
(c)

**Figure 2.** (a) Tracked cardiovascular-induced displacements, (b) matched ECG, and (c) average correlation coefficients. Data points in (a) and (c) indicate the mean within the ROI and error bars indicate plus and minus one standard deviation.



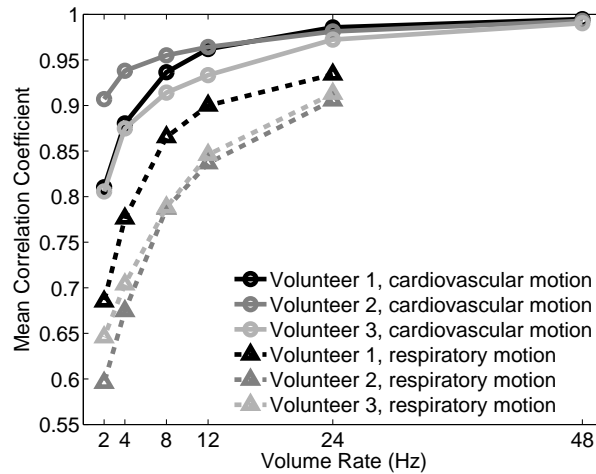


**Figure 3.** Tracked cardiovascular-induced displacements for the volume rates shown in the legend. The top and bottom rows respectively show displacement estimates before and after a median filter was applied to displacement maps. The axial, lateral, and elevation displacement components are shown from left to right respectively.

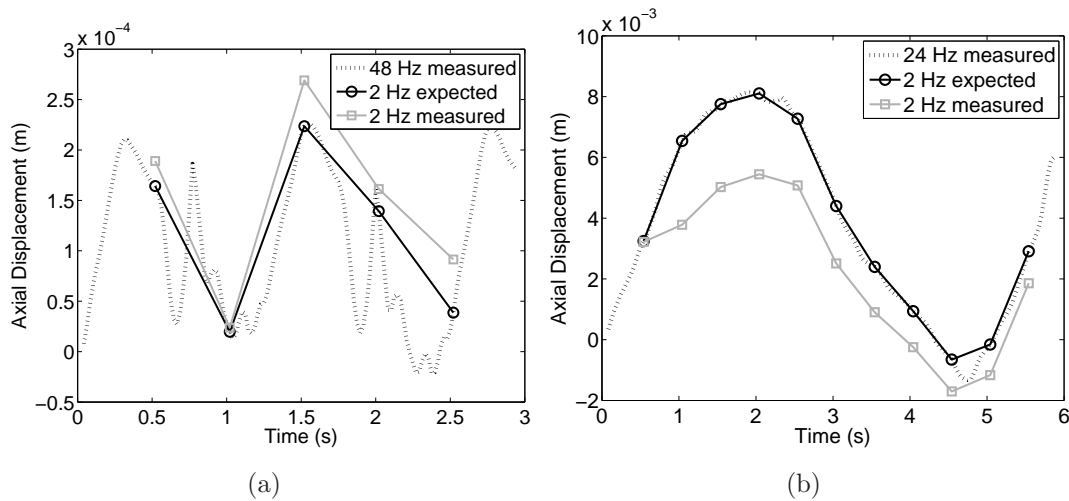


**Figure 4.** Histograms of the correlation coefficient between tracked kernels and their best match in corresponding search regions for the various volume rates of (a) cardiovascular-induced and (b) respiratory-dominated liver motion data for Volunteer 1. Lower correlation coefficients were calculated at the lower volume rates.

234 displacement results obtained at the 48 Hz volume rate. A comparison of expected  
 235 and tracked results at 2 Hz is shown in Fig. 6 (a). In this example, expected and



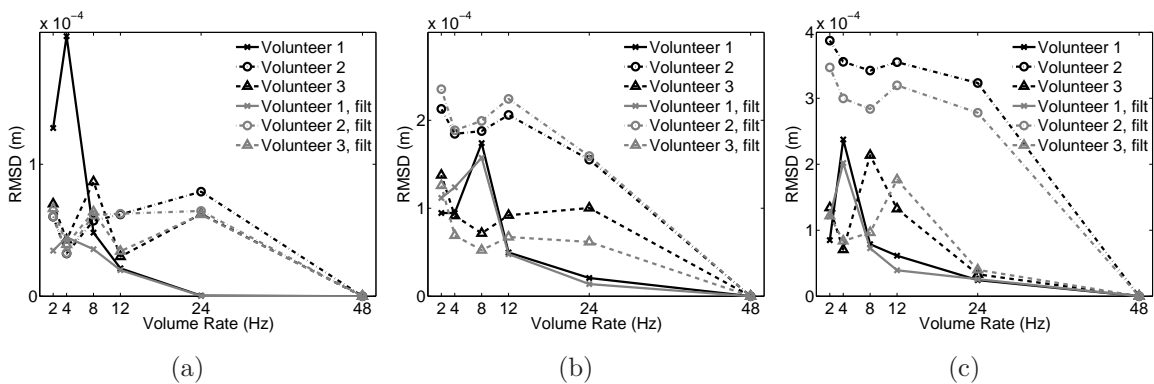
**Figure 5.** Mean correlation coefficients within the same 3D ROIs used to estimate displacements for all available time points, as a function of volume rate in cardiovascular-induced and respiratory-dominated liver motion data. The mean correlation coefficient decreases as the volume rate decreases.



**Figure 6.** Comparison of measured and expected values at 2 Hz for (a) cardiovascular-induced motion and (b) respiratory-dominated motion. These results were measured using median-filtered axial displacement data from Volunteer 1.

236 tracked results are within 0.05 mm agreement. It is also clear from this example that 2  
 237 Hz is inadequate to sample frequencies of cardiac-induced liver motion.

238 The deviation of tracked displacements at lower volume rates from tracked  
 239 displacements at the initial 48 Hz volume rate was measured via the root mean squared  
 240 deviation (RMSD). Figure 7 shows this result for the three volunteers, in each of the  
 241 three dimensions, calculated with data from pre- and post-median filtered displacement  
 242 maps. Unfiltered 48 Hz estimates serve as the reference for unfiltered results while  
 243 median-filtered 48 Hz estimates serve as the reference for filtered results. The RMSD  
 244 generally increases as volume rate is decreased. Median filtering lowers the RMSD in



**Figure 7.** Root mean squared deviation (RMSD) from tracked estimates at 48 Hz in (a) axial, (b) lateral, and (c) elevation dimensions of cardiac-induced liver motion. Median filtering (denoted as filt) lowers the RMSD in most cases.

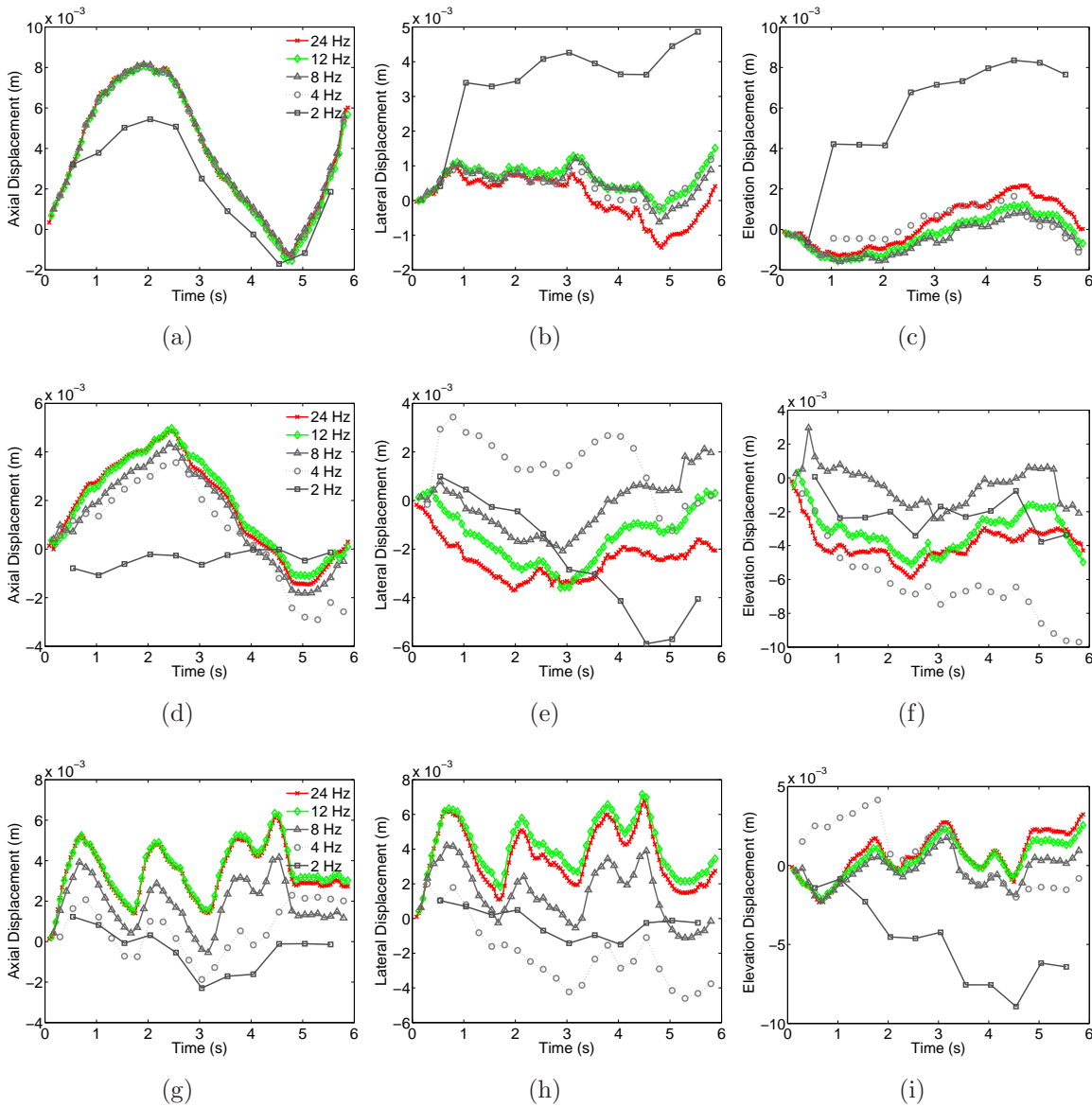
245 most cases.

### 246 3.2. Respiratory-dominated motion

247 **Median-filtered** displacement estimates during free breathing are shown in Figure 8 for  
 248 **the three volunteers, as a function of time. The MAD between median-filtered and**  
 249 **unfiltered displacements ranged from 0.06-0.9 mm.** Results are displayed for tracked  
 250 estimates at the initial 24 Hz volume rate and for tracked estimates after the omission  
 251 of relevant volumes to achieve lower volume rates. The axial, lateral, and elevation  
 252 displacement components are shown in the columns, from left to right respectively.  
 253 Displacement estimates at the initial 24 Hz volume rate are in good agreement with  
 254 lower volume rates, and tracking appears adequate at volume rates of 4-8 Hz and above  
 255 **for Volunteer 1 (top row) and 12-24 Hz for Volunteers 2 and 3 (middle and bottom**  
 256 **rows, respectively).** At 24 Hz, average correlation coefficients within the ROI were  
 257 greater than 0.85 **for all volunteers** (see Figure 5) with insignificant temporal variation.

258 Similar to results obtained without respiratory motion, as the volume rate was  
 259 decreased, intervolum displacements were greater, as expected. Although not shown,  
 260 the spatial variation within displacement maps also increased with decreased volume  
 261 rates. Figure 4 (b) shows the histograms of correlation coefficients within the same  
 262 ROI used to average intervolum displacements in respiratory-dominated motion data  
 263 from Volunteer 1. Figure 5 shows the mean correlation between tracked volumes within  
 264 the same ROI, as a function of volume rate for each volunteer. Both figures indicate  
 265 a decrease in correlation with decreasing volume rates. Furthermore, the correlation  
 266 coefficients observed for respiratory-dominated liver motion were lower than those for  
 267 cardiovascular-induced liver motion

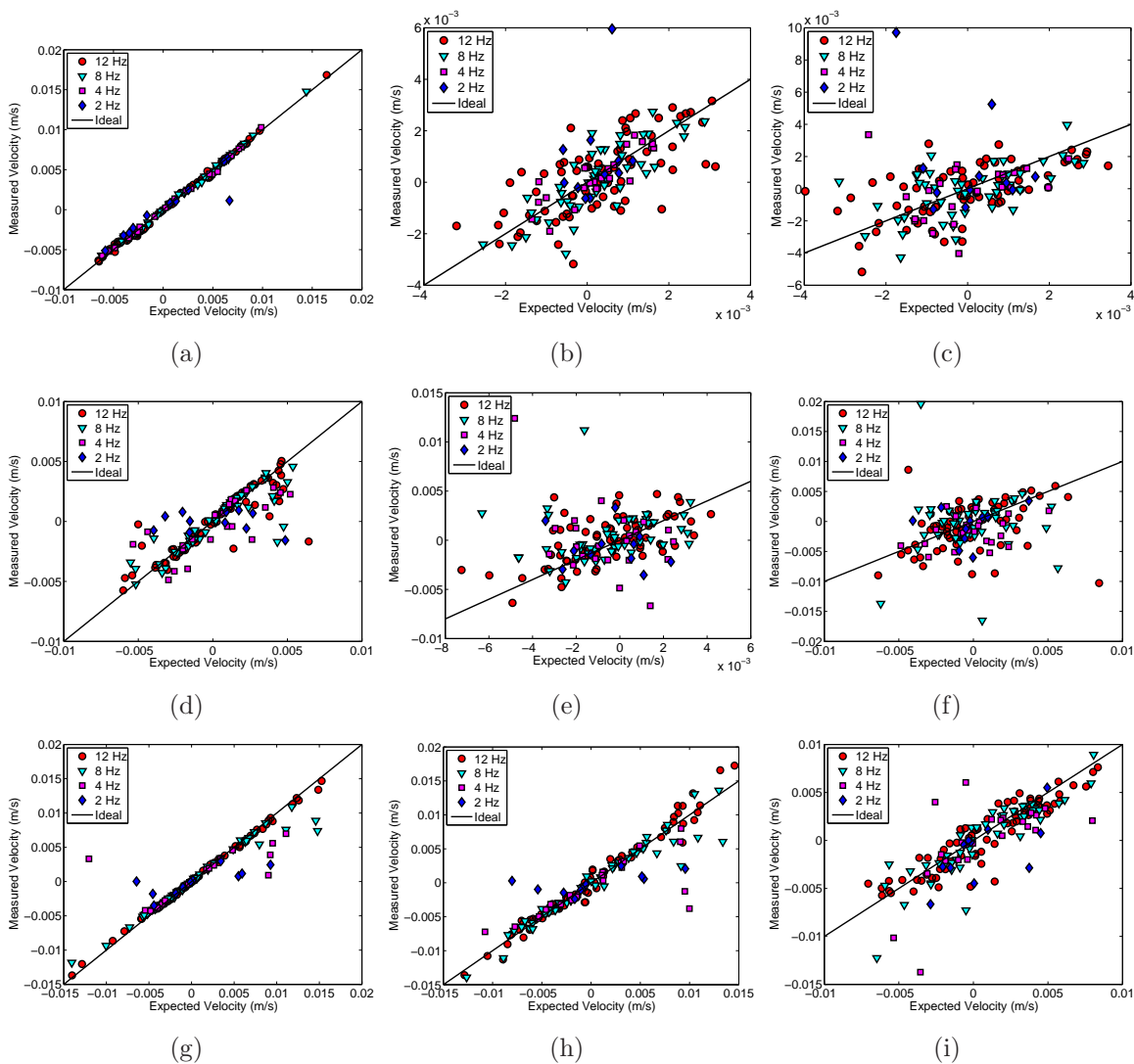
268 A comparison of expected and measured displacements at the 2 Hz volume rate is  
 269 shown in Figure 6 (b). Expected values were calculated by decimating cumulatively-  
 270 summed displacement results obtained at the 24 Hz volume rate. The measured  
 271 values are lower than expected, particularly around the peak. These lower values are



**Figure 8.** Respiratory-dominated tracked displacements with decreased volume rates. The three rows show median-filtered displacement estimates for Volunteers 1, 2, and 3, from top to bottom, respectively. The axial, lateral, and elevation displacement components are shown in the columns, from left to right respectively.

272 predominantly due to one bad estimate within the high-velocity region.

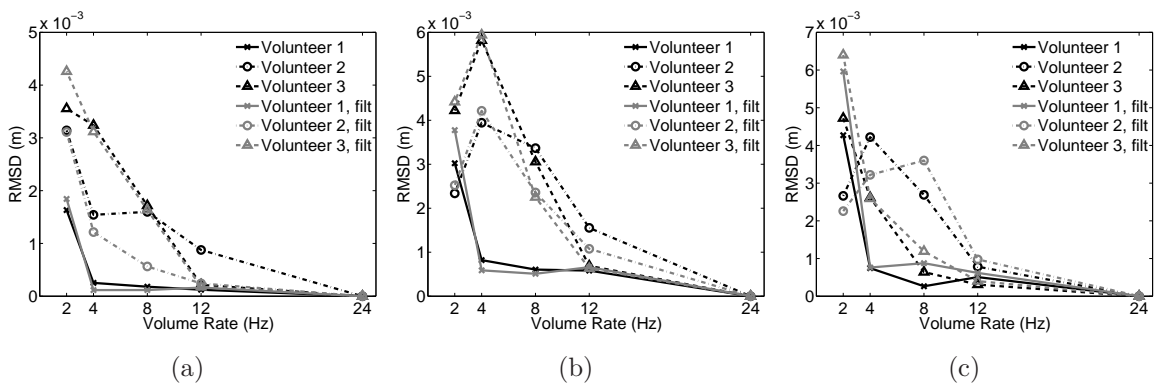
273 Figure 9 shows scatter plots of expected and measured velocities for all volume rates,  
 274 calculated with median-filtered data. The three rows, from top to bottom, correspond  
 275 to results from Volunteers 1, 2, and 3, respectively. The three columns, from left to  
 276 right, correspond to results in the axial, lateral, and elevation dimensions, respectively.  
 277 These results reveal that displacement estimates are generally in good agreement with  
 278 the exception of a few bad estimates (i.e. estimates that largely deviate from the ideal  
 279 1:1 relationship between expected and measured values). If these bad estimates could be  
 280 removed or corrected, tracking with lower volume rates would be improved. Otherwise,



**Figure 9.** Scatter plots of expected and measured velocities during free breathing, for the volume rates indicated in the legend. The three rows, from top to bottom, correspond to results from Volunteers 1, 2, and 3, respectively. The three columns, from left to right, correspond to results in the axial, lateral, and elevation dimensions, respectively.

281 these bad estimates are expected to raise RMSD measurements.

282 The RMSD between tracked displacements at 24 Hz and tracked displacements at  
 283 lower volume rates are displayed in Figure 10 for each volunteer. Results before and after  
 284 application of a 2D median filter are shown. Filtered and unfiltered 24 Hz estimates  
 285 were the reference for filtered and unfiltered results, respectively. The median filter  
 286 lowers RMSD values by at most 1.7 mm. In some cases, the median filter raises RMSD  
 287 estimates. Otherwise, filtered and unfiltered results are fairly similar. The RMSD  
 288 generally increases with decreasing volume rates and values less than or close to 1mm  
 289 are achieved at volume rates of 8-12 Hz in the three volunteers. Volunteer 1 performs  
 290 the best, showing RMSD values well below 1 mm for volume rates of 4 Hz and above.



**Figure 10.** Root mean squared deviation from tracked estimates at 24 Hz in (a) axial, (b) lateral, and (c) elevation dimensions of respiratory-dominated liver motion. Median filtering (denoted as filt) lowers the RMSD in some cases.

291 These RMSD values are notably larger than those obtained for cardiovascular-induced  
 292 motion.

#### 293 4. Discussion

294 While IMRT is primarily administered during free breathing, tracking liver motion  
 295 during breathhold has greatest implications for motion-compensated strategies such  
 296 as such as active breathing control and gated therapy. This type of tracking also  
 297 lends insight into the nature of cardiovascular-induced displacements and elucidates  
 298 the relationship between spatial variation and correlation coefficients. For example, in  
 299 Figure 1 (e-f), the spatial variations observed during periods of increased cardiac activity  
 300 illustrate rotation, translation, and deformation of liver tissue. These three types of  
 301 tissue transformations are common sources of decorrelation in ultrasonic speckle tracking  
 302 (Bamber et al. 1996, Meunier 1998, Trahey et al. 1986). As noted, the transformations  
 303 and associated spatial variations were more prevalent during periods of heightened  
 304 cardiac activity.

305 During these periods, lower correlation coefficients were also observed, as  
 306 demonstrated in Figure 2, and they can be explained by the greater tissue  
 307 transformations that occur in the liver when cardiac activity is at its peak. Similarly,  
 308 the decreased correlation at lower volume rates, shown in Figures 4 and 5, may be  
 309 attributed to increased intervolumetric tissue transformations. Decreased correlation can  
 310 result in poorer tracking performance, confirming the hypothesis that intervolumetric tissue  
 311 transformations must be kept at a minimum by using high-enough volume rates.

312 Figure 3 demonstrates that volume rates greater than 8-12 Hz are needed to reliably  
 313 use ultrasound data obtained with the configuration described in Section 2 to track  
 314 liver motion due to cardiovascular activity. Note that the lower volume rates show poor  
 315 agreement with expected values before the median filter was applied, indicating that  
 316 lower volume rates produce erroneous results that have the potential to be corrected



317 via filtering methods. Despite filtering attempts, tracked displacements at 2 and 4 Hz  
318 show inadequate sampling of the temporal displacement waveform, as demonstrated in  
319 Figure 6 (a).

320 The volume rate limit for tracking cardiac-induced displacements is highly  
321 influenced by the frequency components of liver motion due to cardiac activity. Shirato  
322 et al. (2004) measured liver motion frequencies of  $0.9 \pm 0.2$  Hz due to the beating heart  
323 in nine volunteers (not including the smaller-amplitude, higher-frequency components  
324 localized near the QRS complex which are of lesser importance for motion-compensated  
325 therapy due to their relatively small displacement scale). Practical applications of the  
326 Nyquist Theorem suggest a minimum volume acquisition speed of approximately 9 Hz  
327 to realistically sample periodicity for motion-compensated therapy, which agrees with  
328 results displayed in Figure 3 as well as with comparable results for all volunteers. In  
329 addition to inadequately-sampled cardiovascular-induced motion, lower volume rates  
330 have larger RMSD values (Figure 7), indicating increased tracking error at the lower  
331 volume rates. **With regard to radiation therapies that rely on cardiac-induced motion  
332 tracking, the volumetric scan rate should at least be fast enough to sample the  
333 frequencies of cardiac motion in the area of interest. The resulting information could  
334 be used in lieu of fluoroscopy tracking measurements to eliminate the surgical costs  
335 associated with fluoroscopic markers and the associated radiation doses to patients.**

336 In respiratory-dominated motion, cumulatively-summed displacements estimated  
337 with lower volume rates usually show smaller peak or trough amplitudes when  
338 compared to measurements at higher volume rates and corresponding expected values,  
339 as demonstrated in Figure 6 (b). The lower estimates are considered inaccurate by  
340 comparison and are primarily due to isolated tracking estimates that substantially  
341 deviate from expected values and influence all subsequent tracked displacements. A  
342 comparison of Figure 8 with Figure 9 demonstrates how a few bad estimates can cause  
343 large departures in the cumulatively-summed data (e.g. compare Figure 9 (a) with  
344 Figure 8 (a)). **Another example of this is observed by comparing the 12 Hz and 8 Hz  
345 results of Figures 8 (g) and 9 (g)), where the few bad estimates in the high-velocity  
346 region of the 8Hz data accumulate to give a displacement estimate at 5.5s that differs  
347 by 2mm.** This behavior of the incremental tracking method has been noted in previous  
348 work (Bamber et al. 1996, Harris et al. 2010, Harris et al. 2011).

349 Displacement profiles that agree with estimates achieved at high volume rates  
350 are used to identify suitable volume rate limits for tracking respiratory-dominated  
351 liver motion. Displacement estimates obtained with low volume rates are corrupted  
352 by speckle decorrelation, even if temporal resolution is good enough to resolve the  
353 frequencies of motion. Results from three volunteers indicate that a minimal volume  
354 rate of 8-12 Hz is needed to achieve RMSD values less than or close to 1 mm, as shown in  
355 Figure 10. The exact volume rate limit varies with each volunteer and with acceptable  
356 RMSD threshold values, which should be based on knowledge of tracking limitations  
357 (discussed below).

358 **There are several sources of error with this tracking method. First, incremental 3D**

359 tracking suffers from an accumulation of tracking error, as noted previously. Secondly,  
360 false peaks and jitter are common sources of error in speckle tracking (Ramamurthy  
361 & Trahey 1991, Walker & Trahey 1995, Akiyama et al. 1988, Meunier 1998, Trahey  
362 et al. 1986). Jitter occurs when the peak of a correlation function is shifted due to  
363 electronic noise, decorrelation, and other factors, placing an uncorrectable lower bound  
364 on tracking accuracy. Byram et al. (2010) have demonstrated with tissue-mimicking  
365 phantom studies that the error of our 3D tracking algorithm is within expected jitter  
366 magnitudes, ranging from 0.1 to 1 mm in lateral and elevational dimensions and  
367 significantly less than 0.1 mm in the axial dimension. These expected jitter magnitudes  
368 dictate the minimum accuracy of the scatter plots in Figure 9. However errors of 0.1-  
369 1.0 mm are well within the range acceptable for radiotherapy treatment set-up and are  
370 comparable to fluoroscopy tracking errors (Shirato et al. 2000). Note that correlation  
371 coefficients are lower and RMSD values are greater for the respiratory-dominated 4-8  
372 Hz volume rates of Volunteers 2 and 3 (compared to those of Volunteer 1). This is  
373 likely due to the larger displacements and velocities in the respiratory-dominated liver  
374 motion for these volunteers, particularly in the lateral and elevation dimensions where  
375 jitter in tracking estimates is greatest. The accumulation of error further increases the  
376 RMSD values for these volunteers. A third source of error is the spatial averaging of  
377 displacements within an ROI, which could introduce errors due to spatial variation,  
378 particularly at lower volume rates where increased intervolumetric tissue transformations  
379 are expected. However, 3D spatial averaging has the advantage of reducing noise  
380 artifacts in tracking estimates. These sources of tracking error should be considered  
381 when selecting appropriate RMSD thresholds and designing PTV margins for each  
382 patient.

383 Isolated tracking errors were mitigated by applying a 2D median filter to  
384 displacement maps. In most cases, the median filter reduced deviations between higher  
385 and lower volume rates, while maintaining comparable unfiltered values at the higher  
386 volume rates, as demonstrated in Figure 3. As a result of the median filter, lower RMSD  
387 values were achieved in most cases.

388 The scatter plots in Figure 9 indicate that a more robust error detection, correction,  
389 and/or rejection scheme has the potential to further improve tracking estimates. Such  
390 improvements are especially necessary when scanning time is increased, given the  
391 previously-discussed accumulation of tracking error. Improvements are possible by  
392 considering the motion of adjacent pixels in the three spatial dimensions (i.e. axial,  
393 lateral, and elevation) and in the temporal dimension, and coupling that information  
394 with knowledge of the spatiotemporal continuity of liver tissue. The 2D median filter  
395 employs this concept. A more refined approach is expected to improve tracking results,  
396 yet the study of such methods is beyond the scope of this paper.

397 The availability of 4D ultrasound scanners with matrix array transducers and  
398 parallel receive beamforming offers increased opportunity to track tissue at higher  
399 volume rates than previously possible. This is the first study to use such a system  
400 to track 4D liver displacements at volume rates as high as 48 Hz. Although analyses

401 were performed off-line, real-time speckle tracking has been implemented in a variety of  
402 commercial 2D and 3D ultrasound systems for the purposes of elastography (Treece  
403 et al. 2008, Lindop et al. 2008) and should therefore be feasible in the context of  
404 radiotherapy guidance. Buffer size does not pose a limitation to clinically-relevant  
405 tracking time durations if data is not stored on the scanner’s hardware.

406 The presented approach of tracking average displacements within a ROI could be  
407 useful for guiding IMRT if the ROI is placed within a treatment PTV to monitor when  
408 cumulatively-summed liver displacements in any dimension exceeds a certain percentage  
409 of the PTV in that dimension. Ideally, the ROI and the focal depth would be in the  
410 same region since there are advantages (e.g. better resolution and signal-to-noise ratios,  
411 less jitter) to tracking near the focus (Nightingale et al. 2002).

## 412 5. Conclusion

413 This study utilized a 4D ultrasound system and 2D matrix array to demonstrate that  
414 volume rates as high as 8-12 Hz are needed to estimate cardiovascular-induced and  
415 respiratory-dominated liver motion with 3D ultrasound speckle tracking. Displacement  
416 estimates obtained with lower volume rates were shown to be corrupted by the  
417 undersampling of cardiovascular-induced motion and speckle decorrelation. Volume  
418 acquisition rates within this range should be employed for effective ultrasound-guided  
419 motion compensation during IMRT with this type of imaging system. The absolute  
420 limit may vary with each patient.

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