

# Shell structure of $^{43}\text{S}$ and collapse of the $N = 28$ shell closure

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The single-particle structure of the  $N = 27$  isotones provides insights into the shell evolution of neutron-rich nuclei from the doubly-magic  $^{48}\text{Ca}$  toward the drip line.  $^{43}\text{S}$  was studied employing the one-neutron knockout reaction from a radioactive  $^{44}\text{S}$  beam. Using a combination of prompt and delayed  $\gamma$ -ray spectroscopy the level structure of  $^{43}\text{S}$  was clarified. Momentum distributions were analyzed and allowed for spin and parity assignments. The deduced spectroscopic factors show that the  $^{44}\text{S}$  ground-state configuration has a strong intruder component. The results were confronted with shell model calculations using two effective interactions. General agreement was found between the calculations, but strong population of states originating from the removal of neutrons from the  $2p_{3/2}$  orbital in the experiment indicates that the breakdown of the  $N = 28$  magic number is more rapid than the theoretical calculations suggest.

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## I. INTRODUCTION

The emergence of shell closures or their disappearance in exotic nuclei has been one of the main interests of the nuclear structure community since the advent of radioactive beam facilities. Islands of inversion and shape coexistence have been associated with the disappearance of the classical shell closures on the neutron-rich side of the valley of stability [1]. In particular, the  $N = 28$  shell closure, arising in a harmonic oscillator plus spin-orbit mean field, has recently attracted much interest [2]. Below the doubly magic nucleus  $^{48}\text{Ca}$  with 20 protons and 28 neutrons, the  $N = 28$  nuclei show a variety of interesting features. Mass measurements [3], transfer [4], and nucleon knockout reactions [5] support a strong  $N = 28$  shell closure in  $^{46}\text{Ar}$ . Measurements of the reduced transition probability,  $B(E2)$ , find a low degree of collectivity [6, 7], while shell model calculations show enhanced collectivity at the shell closure. This discrepancy is yet to be resolved. In  $^{44}\text{S}$ , the measurement of a large  $B(E2)$  value and its comparison to theoretical calculations suggested a vibrational character of this nucleus [8]. The lowering of the excited  $0_2^+$  state from 3695 keV in  $^{46}\text{Ar}$  [9] to 1365 keV [10] in  $^{44}\text{S}$  indicates the onset of shape coexistence and a rapid weakening of the  $N = 28$  shell closure. The measured  $E0$  strength between the  $^{44}\text{S}$   $0^+$  states was interpreted as arising from the substantial mixing of spherical and prolate configurations [11]. Theoretical calculations of the potential energy surface using the symmetry-conserving configuration mixing method and the Gogny D1S interaction do not show distinct minima characteristic of shape coexistence and rather suggest configuration mixing [12].

Later refinements of the theory and extended calculations find that the ground state of  $^{44}\text{S}$  has a collective wave function which is extended in the  $(\beta, \gamma)$  plane while the excited  $0_2^+$  is prolate, yet  $\gamma$ -soft [13]. Shell model calculations using a newly derived SDPF-MU interaction [14] suggest that the evolution of collectivity along  $N = 28$  is governed by the proton-neutron tensor force [15]. Here, the potential energy surface exhibits a minimum on the prolate side.

The  $^{42}\text{Si}$  nucleus is well deformed, it exhibits a low excitation energy for the first  $2^+$  state [16] and a large  $R_{4/2}$  ratio [17]. Calculations with the SDPF-MU interaction predict the ground state of  $^{42}\text{Si}$  to be strongly oblate deformed [15]. Detailed spectroscopy of  $^{42}\text{Si}$ , however, questioned the  $4^+$  assignment of Ref. [17] and proposed an excited  $0_2^+$  state based on the observed population cross section [18]. Approaching the drip-line [19], the last  $N = 28$  nucleus with excited states known is  $^{40}\text{Mg}$  [20]. The measured two-proton removal cross sections along the  $N = 28$  isotones [17, 21] were interpreted as showing a change of the ground state deformation from prolate in  $^{44}\text{S}$  to oblate for  $^{42}\text{Si}$ , and back to prolate at  $^{40}\text{Mg}$ .

Turning to the even-odd  $N = 27$  nuclei,  $^{43}\text{S}$  has attracted special attention, both from the theoretical and experimental side. In  $^{45}\text{Ar}$  the ground state is  $7/2^-$ , as expected from the normal orbital filling. A low-lying  $J^\pi = 3/2^-$  state with a rather long lifetime [22] is strongly populated in the  $(d, p)$  reaction adding a neutron to  $^{44}\text{Ar}$  [4] and very weakly in the neutron removal reaction [5]. This confirms the vacancy of the  $2p_{3/2}$  orbital in both  $^{44,46}\text{Ar}$  and the existence of a shell closure at  $N = 28$ . In  $^{43}\text{S}$ , an isomeric state with a lifetime of

77 478(48) ns was found at 319 keV [23]. Based on the  
 78 comparison with shell model calculations the isomeric  
 79 state was assigned spin and parity  $7/2^-$  and a level in-  
 80 version compared to  $^{45}\text{Ar}$  was proposed. A measurement  
 81 of the magnetic moment firmly assigned  $J^\pi = 7/2^-$  to  
 82 the isomeric state and, because its lifetime is only com-  
 83 patible with an  $E2$  transition, the ground state was in-  
 84 ferred as  $J^\pi = 3/2^-$  [24]. The spherical nature of the  
 85  $7/2^-$  isomeric state was questioned and the spectroscopic  
 86 quadrupole moment, determined to be  $|Q_s| = 23(3) \text{ efm}^2$ ,  
 87 was significantly larger than the expectation for a single  
 88 hole in the  $1f_{7/2}$  orbital. While the state cannot be con-  
 89 sidered spherical, shell model calculations do not predict  
 90 a band structure built upon the isomeric state [25]. These  
 91 results triggered various theoretical discussions. Anti-  
 92 symmetrized molecular dynamics (AMD) calculations indi-  
 93 cate that the  $7/2^-$  isomer might be triaxial, and that  
 94 bands of prolate, oblate, and triaxial nature coexist at  
 95 low excitation energy [26]. The gap between neutron  
 96 single-particle levels originating from the spherical  $1f_{7/2}$   
 97 and  $2p_{3/2}$  orbitals reduces as a function of the deforma-  
 98 tion parameter  $\beta_2$ ; the two orbitals cross around a pro-  
 99 late deformation with  $\beta_2 \approx 0.2$  and the  $N = 28$  shell  
 100 gap disappears. A state at around 940 keV observed  
 101 in a Coulomb excitation measurement [27] is suggested  
 102 as the  $7/2^-$  member of the prolate  $K^\pi = 1/2^-$  ground  
 103 state band with a negative decoupling parameter. An  
 104 oblate band built on the  $3/2^-$  state is also predicted. A  
 105 shell model study exploiting quadrupole rotational in-  
 106 variants came to similar conclusions [28]. The calcu-  
 107 lations based on the SDPF-U effective interaction [29]  
 108 predict a third, prolate band with a dominant  $2p\text{-}2h$   
 109  $(1f_{7/2})^{-3}(2p_{3/2})^2$  configuration. Calculations using the  
 110 SDPF-MU effective interaction [14] and the variation af-  
 111 ter angular-momentum projection method show that the  
 112 ground state and the isomeric state are dominated by  
 113  $K = 1/2$  and  $7/2$  and the isomeric nature is explained  
 114 by the  $K$  forbiddens of the decay [15]. This interpre-  
 115 tation also explains the occurrence of the long-lived  $0_2^+$   
 116 and  $4_1^+$  states in  $^{44}\text{S}$  [10, 11, 30, 31].

117 Spectroscopic information on states in  $^{43}\text{S}$  beyond the  
 118 ground and isomeric state was obtained from nucleon re-  
 119 moval reactions, however, placement in the level scheme  
 120 proved difficult because of the presence of the isomeric  
 121 state [32]. Most recently, excited state lifetimes in  $^{43}\text{S}$   
 122 were measured. Using the proton knockout reaction from  
 123  $^{44}\text{Cl}$  several states were populated [33]. The level order-  
 124 ing was reversed compared to the earlier study [32]. It  
 125 should be noted that the level scheme and the interpreta-  
 126 tion of Ref. [33] are at variance with the results presented  
 127 here. In the present work, the neutron knockout reaction  
 128 is measured with the additional capability to distinguish  
 129 between decays to the isomer and to the ground state.

130 In the present paper, we report on the measurement of  
 131 the single-particle structure of  $^{43}\text{S}$  using the one-neutron  
 132 knockout reaction from a fast radioactive  $^{44}\text{S}$  beam. The  
 133 combination of prompt and delayed spectroscopy allowed  
 134 for an unambiguous construction of the level scheme

135 and the extraction of spectroscopic factors using reac-  
 136 tion model calculations. The results suggest an intruder-  
 137 dominated configuration in the ground state of  $^{44}\text{S}$ .

## 138 II. EXPERIMENT

139 The experiment was performed at the Coupled Cy-  
 140 clotron Facility of the National Superconducting Cy-  
 141 clotron Laboratory at Michigan State University [34].  
 142 The secondary  $^{44}\text{S}$  beam was produced by projectile frag-  
 143 mentation of a 140 A MeV  $^{48}\text{Ca}$  primary beam on a  
 144  $705 \text{ mg/cm}^2$   $^9\text{Be}$  production target located at the en-  
 145 trance of the A1900 separator [35]. The beam parti-  
 146 cles were identified by their time-of-flight on an event-  
 147 by-event basis. The secondary beam was separated and  
 148 transported to a  $376(4) \text{ mg/cm}^2$   $^9\text{Be}$  secondary target  
 149 located at the pivot point of the S800 spectrograph [36].  
 150 The momentum acceptance of the A1900 separator was  
 151 set to 1%, resulting in a mid-target energy of 93.7 A MeV  
 152 and an average  $^{44}\text{S}$  intensity and purity of about 1900 pps  
 153 and 98(1)%, respectively.

154 The reaction residues were analyzed and identified in  
 155 the S800 spectrograph [36] as shown in Fig. 1. Parti-

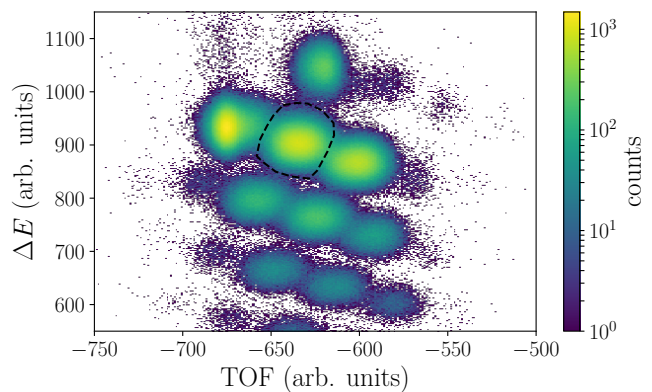


FIG. 1. Particle-identification plot of reaction residues de-  
 tected in the S800 spectrograph. A gate on incoming  $^{44}\text{S}$  ions  
 is applied. The dashed line is the outgoing  $^{43}\text{S}$  gate for the  
 further analysis.

156  
 157 cle identification was achieved by measuring the energy  
 158 loss in an ionization chamber ( $\Delta E$ ) in the focal plane of  
 159 the S800 spectrograph and the time-of-flight (TOF) be-  
 160 tween two plastic scintillators located before the target  
 161 and in the focal plane, respectively. Positions and angles  
 162 of reaction residues at the end of the S800 spectrograph  
 163 were measured by two cathode-readout drift chambers  
 164 (CRDC) and traced back to the secondary target by us-  
 165 ing the ion optics code COSY Infinity [37]. This allowed  
 166 the determination of the non-dispersive position and the  
 167 momentum vector at the secondary target. In order to  
 168 improve the resolution for the momentum transfer, a par-  
 169 allel plate avalanche counter (PPAC) was placed at the  
 170 intermediate image plane upstream of the target. Here,  
 171

172 the dispersive position is correlated with the momentum  
173 of the projectile, and the momentum of the incoming pro-  
174 jectile can thus be obtained. The momentum resolution  
175 for the incoming beam with the PPAC position correc-  
176 tion was deduced as 0.052 GeV/c.

177 The secondary target was surrounded by the  
178 Gamma Ray Energy Tracking In-beam Nuclear Array  
179 (GRETINA) [38, 39]. A GRETINA module consists of  
180 four high-purity germanium crystals, each 36-fold seg-  
181 mented. In the present experiment, four detector mod-  
182 ules were placed at  $58^\circ$  with respect to the beam axis and  
183 four were placed at  $90^\circ$ . The signals were digitized and  
184 an online pulse-shape analysis algorithm allowed for the  
185 determination of  $\gamma$ -ray interaction points with energy and  
186 position information. It was assumed that the hit with  
187 the largest energy deposition was the first interaction,  
188 and its position was used for the Doppler correction. The  
189  $\gamma$ -ray position information was also used in the tracking  
190 analysis, where  $\gamma$ -ray interactions were added together  
191 when the difference between their emission angle with  
192 respect to the target position was less than  $25^\circ$ . This  
193 add-back analysis was adopted for the  $\gamma$ - $\gamma$  coincidence  
194 analysis and for extracting the exclusive parallel momen-  
195 tum distributions. The energy and efficiency calibration  
196 of GRETINA was done with standard radiation sources  
197 and the deviation from literature values were deduced to  
198 be less than 1 keV. The efficiency of the whole array was  
199 measured to be 5.9% at 1 MeV. The  $\gamma$ -ray yields were  
200 determined from a fit of simulated response functions to  
201 the  $\gamma$ -ray energy spectrum. The experimental setup was  
202 implemented in a GEANT4 simulation [40] including the  
203 experimentally determined thresholds and resolutions of  
204 each individual Ge crystal. In the  $\chi^2$  fit, the  $\gamma$ -ray en-  
205 ergies and intensities were individually varied to reproduce  
206 the measured spectrum.

207 Finally, the reaction residues were implanted into a  
208 6.35 mm thick Al plate at the back of the focal plane of  
209 the S800 spectrograph. Delayed  $\gamma$  rays emitted from the  
210 decay of isomeric states were detected in IsoTagger [41]  
211 consisting of 32 CsI(Na) detectors. This allowed con-  
212 struction of the level scheme above the 320 keV isomeric  
213 state in  $^{43}\text{S}$  for the first time and deduction of the pop-  
214 ulation cross sections for all final states. The energy and  
215 efficiency calibration of IsoTagger was performed with a  
216 standard  $^{88}\text{Y}$  source. The efficiency at 898 keV was mea-  
217 sured to be 8.3%.

218 The  $^{44}\text{S}$  nucleus has an isomeric  $0_2^+$  state at 1365 keV  
219 with a 2.619(26)  $\mu\text{s}$  half-life [10, 11]. The beam can thus  
220 reach the secondary target in an excited state. In addi-  
221 tion to the direct  $E0$  transition to the ground state this  
222 isomeric state also decays to the  $2_1^+$  state with a branch-  
223 ing ratio of 16.3(13)% [11]. The  $\gamma$ -ray transition from the  
224  $2_1^+$  state to the ground state could have been observed  
225 in the IsoTagger, however, no transition at this energy  
226 was observed. The isomeric ratio of the  $0_2^+$  state in  $^{44}\text{S}$  is  
227 thus assumed to be negligible for the extraction of cross  
228 sections.

### 229 III. RESULTS

230 Fig. 2 shows the prompt, Doppler-corrected  $\gamma$ -ray en-  
231 ergy spectrum measured with GRETINA gated on the  
232 one-neutron knockout reaction from  $^{44}\text{S}$  to  $^{43}\text{S}$ . Most of

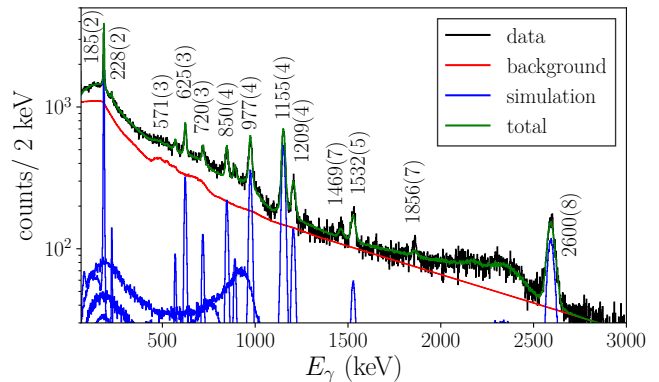


FIG. 2. Prompt, Doppler-corrected  $\gamma$ -ray energy spectrum for the one-neutron knockout reaction from  $^{44}\text{S}$  to  $^{43}\text{S}$ . The peaks are labeled with the transition energy and uncertainty in keV. The background around 500 keV includes transitions from neutron-induced reactions on Ge and Al.

235 the previously observed  $\gamma$  rays [32, 33] were confirmed  
236 and their energies are shown in Fig. 2 together with their  
237 uncertainty. The transition at 571(3) keV is newly ob-  
238 served in this work. For the error estimation of the  $\gamma$ -  
239 ray energy, the uncertainties of the energy calibration  
240 of GRETINA, the velocity of  $^{43}\text{S}$  for the Doppler cor-  
241 rection, and a potential offset of the reaction target loca-  
242 tion along the beam axis were considered. The individual  
243 contributions were, for example for the 2600 keV transi-  
244 tion, less than 0.5, 3, and 6 keV. To deduce the yield  
245 of each prompt  $\gamma$  ray, a  $\chi^2$  fit of the simulated response  
246 functions to the experimental spectrum was performed.  
247 In this fitting procedure, background  $\gamma$  rays of neutron-  
248 induced reactions with the Ge detectors and surrounding  
249 materials were also considered. In the laboratory system  
250 clear peaks around 600 keV are observed. The remaining  
251 continuous background was modeled as the sum of two  
252 exponential functions connected to a linear function in  
253 the lower energy region. The uncertainties for the  $\gamma$ -ray  
254 yields include, besides the statistical uncertainty, consid-  
255 eration of the deviation of the simulated efficiency from  
256 the measured one. This contribution was smaller than  
257 4% over the whole energy range and thus smaller than  
258 the statistical uncertainties. The prompt  $\gamma$ -ray energies  
259 and intensities are compiled in Table I. Fig. 3 shows the  
260 background subtracted  $\gamma$ - $\gamma$  coincidence spectra gated on  
261 the 1155, 625, 850 and 977 keV transitions. The three  
262 transitions at 1155, 625, and 850 keV are emitted in cas-  
263 cade and the 977 and 185 keV transitions are in mutual  
264 coincidence, but not with any of the other transitions.  
265 This is in agreement with the level scheme proposed in  
266 Ref. [33] with a doublet of states at 1155 and 1162 keV.

TABLE I. Observed  $\gamma$  ray energies, efficiency-corrected intensities, and coincidence information for  $^{43}\text{S}$ . The uncertainties of the  $\gamma$  ray energies include all systematic uncertainties while yields include only the statistical errors.

energy (keV)	yield/ion (%)	coincident $\gamma$ rays	level (keV)
185(2)	5.8(3)	977	1162(4)
228(2)	0.44(7)		228(2)
320(2)	49(3)	1532	320
571(3)	0.93(11)		
625(3)	3.6(2)	850, 1155	1780(5)
720(3)	1.8(2)		
850(4)	3.6(2)	625, 1155	2628(6)
977(4)	7.1(4)	185	977(4)
1155(4)	13.2(6)	625, 850	1155(4)
1209(4)	3.6(2)		1209(4)
1469(7)	0.67(13)		2628(6)
1532(5)	2.2(2)	320	1854(4)
1856(7)	0.37(13)		1854(4)
2600(8)	9.7(5)		2600(8)

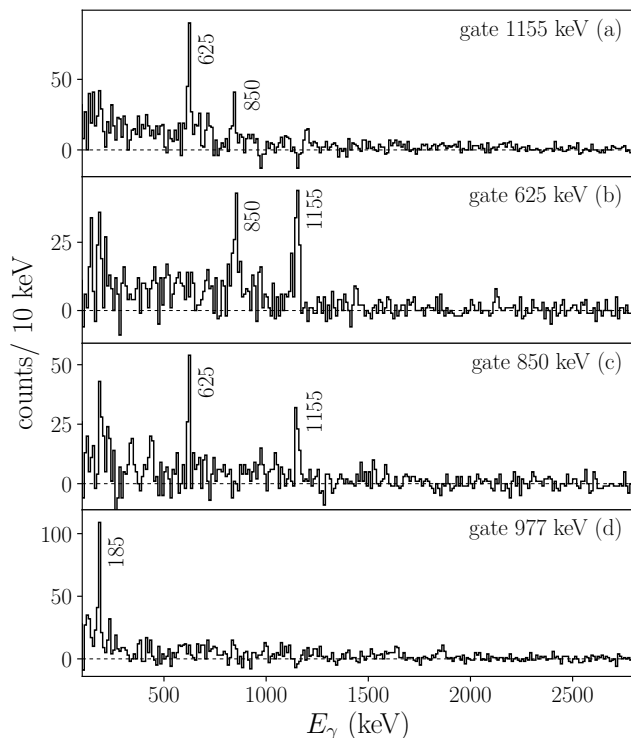


FIG. 3. Background subtracted  $\gamma$ - $\gamma$  coincidence spectra measured in GRETINA. Panels (a), (b), (c), and (d) show the spectra gated on the prompt 1155, 625, 850, and 977 keV transitions.

The high statistics obtained in the present work makes it possible to determine the order of the  $\gamma$ -ray transitions in the cascades by the comparison of the measured  $\gamma$ -ray intensities in Table I. These intensities confirm the order of the 850  $\rightarrow$  625  $\rightarrow$  1155 keV and 185  $\rightarrow$  977 keV cascades. The latter is opposite to the suggestion of Ref. [33] and thus challenges the result of the very similar lifetimes of

the states at 185 and 1162 keV proposed in that work. The present ordering of the cascade is also consistent with earlier measurements of Coulomb excitation [27] assuming that the transition observed around 940 keV corresponds to the 977 peak observed in the present work. In fact, the transition energy is not determined accurately in Ref. [27], and the observed line could be composed of several transitions within the limited energy resolution. The isobar  $^{43}\text{Cl}$  and the isotone  $^{45}\text{Cl}$  have transitions at 943 and 928 keV which could have contaminated the spectrum. A recent Coulomb excitation experiment confirmed the 977 keV state that is directly excited from the ground state [42]. The 850 keV transition is placed on top of the 625 keV one, since the former was not observed in the proton removal reaction [33]. The transition at 1469 keV was placed to feed either the 1155 keV or the 1162 keV state from the 2628 keV state based on the matching energy sum. No coincidences were found for the 1209 and 2600 keV transitions. Based on their intensities, coincidences should have been observed and these transitions are therefore placed as direct ground state decays. The transitions at 228, 571, and 720 keV could not conclusively be placed in the level scheme due to limited statistics. The 228 keV transition is placed as a direct ground state decay from the first excited state at 228 keV, based on the comparison with theoretical calculations (see Section IV).

Fig. 4 shows the  $\gamma$ -ray energy spectrum measured by the IsoTagger in delayed coincidence with identified  $^{43}\text{S}$  reaction residues. The decay of the known 320 keV iso-

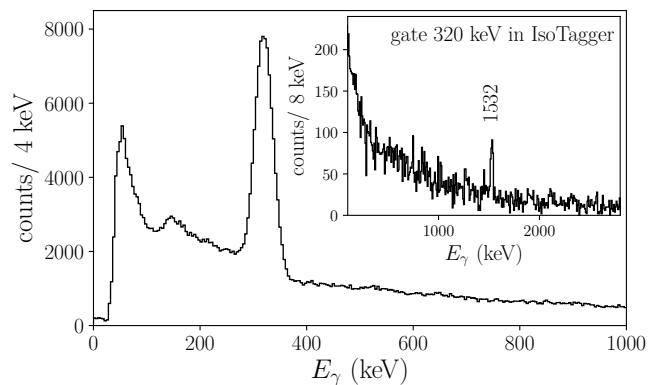


FIG. 4. Gamma-ray energy spectrum measured by IsoTagger. A gate on  $^{43}\text{S}$  has been applied. The isomeric decay of the 320 keV state is observed. The inset shows the prompt, Doppler-corrected  $\gamma$ -ray energy spectrum measured with GRETINA gated on the delayed 320 keV transition.

meric state [23] is observed. The intensity of the 320 keV transition was determined from a  $\chi^2$  fit of a simulated response function [41] to the spectrum in a similar manner as for the prompt spectrum. The background was modeled as the sum of two exponential functions. The implantation position distribution of the  $^{43}\text{S}$  ions was implemented in the simulation as described in Ref. [41].

315 The position on the stopper plate was taken from the experimental  $xy$  distribution measured by the CRDC detectors in the S800 focal plane and extrapolated to the stopper plate. The implantation depth,  $z$  coordinate, was estimated by the ATIMA code [43] using the experimentally measured energy distribution of  $^{43}\text{S}$  ions. In order to extract the yield, the in-flight decay of the isomer between the secondary reaction target and the stopper plate needed to be taken into account. The half-life of the isomeric state has been previously measured ( $T_{1/2} = 478(48)$  ns [23], 415(5) [24], and  $200_{-70}^{+140}$  ns [44]). In the present experiment, the half-life was determined from the decay curve after implantation. The result of  $T_{1/2} = 391(14)$  ns is slightly lower than the most precise value but consistent. Considering the trajectory and the velocity of  $^{43}\text{S}$  behind the secondary target, 79.4(23)% of the isomeric state initially produced at the target reached the stopper. For the uncertainty estimation on the yield, the deviation of the present half-life from the previous measurement of 415(5) ns [24], the velocity distribution of the  $^{43}\text{S}$  reaction products, and the effect of the uncertainty of the simulated implantation depth on the efficiency of IsoTagger (2% at 320 keV) were considered.

338 Fig 4 also shows the prompt  $\gamma$  rays detected in GREYTA in delayed coincidence with the decay of the 320 keV isomer. The 1532 keV transition is clearly in coincidence with the isomeric transition and the energy sum matches the 1856 keV transition. This establishes a new state at 1854(4) keV using the weighted average of the energies. Looking for coincidences with the 1532 keV transition in GREYTA does not reveal another  $\gamma$ -ray transition as a candidate for a transition on top of the isomer.

348 The level scheme of  $^{43}\text{S}$ , determined in the present work, is shown in Fig. 5. The order of the transitions of a  $\gamma$ -ray cascade was determined by comparing the observed yields. The 1469 and the 1856 keV transitions were placed in the level scheme solely based on energy differences. Two states are located close to the neutron separation energy  $S_n = 2629$  keV [45]. The 2600 keV state decays directly to the ground state, while the 2628 keV state decays via a cascade. The fact that the 2600 keV transition was not observed in the fragmentation reaction of  $^{45}\text{Cl}$  [32] nor in the proton knockout reaction [33] from  $^{44}\text{Cl}$  supports the presence of two different states. The very different momentum distributions (see below) for the 2600 and 2628 keV states further confirm the existence of two close-lying states near the neutron separation energy.

365 Using the level scheme presented in Fig. 5 the final-state exclusive cross sections were determined. They are presented in Table II and Fig. 5. The inclusive cross section to bound states in  $^{43}\text{S}$  was determined from the number of particles identified in the S800 spectrograph and amounts to 91(4) mb, slightly larger than but consistent with the previous measurement of the same reaction of 79(7) mb [32]. The uncertainties include, in addition to statistical sources, the selection of the particle identi-

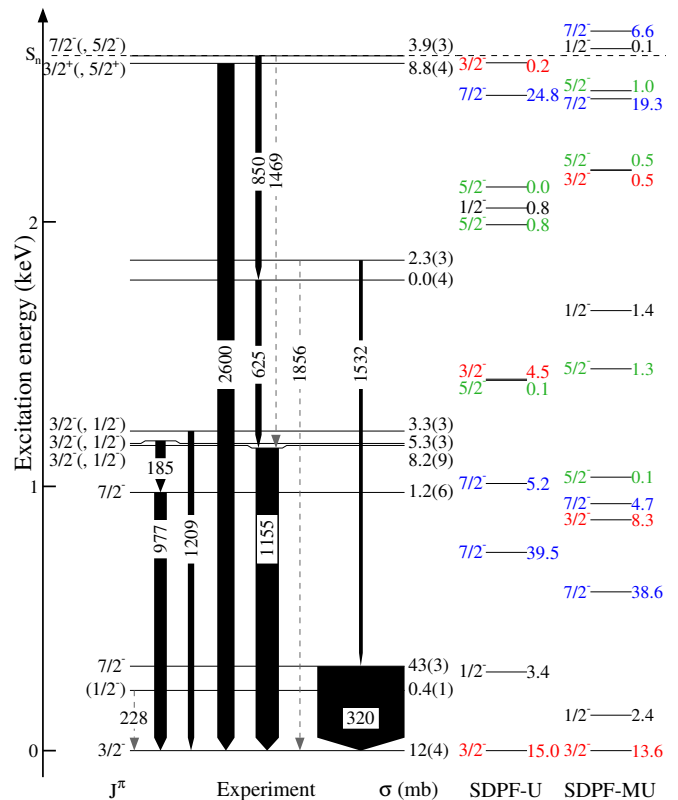


FIG. 5. Level scheme of  $^{43}\text{S}$  determined from the present experimental results and predicted by shell model calculations. The width of the arrows reflects the measured  $\gamma$ -ray yields. Gray, dashed transitions are placed based on the energy differences of established levels, the 228 keV state is placed based on the comparison to the shell model calculations. The levels are labeled with the spin and parity assignments derived from the measured momentum distributions and the partial cross section for each state (in mb). Spins and parities of predicted  $1/2^-$ ,  $3/2^-$ ,  $5/2^-$ , and  $7/2^-$  states are indicated in black, red, green, and blue, respectively. Theoretical cross sections (in mb) include the calculated spectroscopic factors and the reaction model calculations for the single-particle cross sections (see text for details).

375 fication gate, the purity and intensity fluctuation of the incoming  $^{44}\text{S}$  beam, uncertainties related to the transmission of the analysis line of the S800, and the thickness of the secondary target. The one-neutron reaction from  $^{44}\text{S}$  was fully within the acceptance of the S800 spectrograph so that corrections were not necessary.

381 The parallel momentum distributions for several final states populated in  $^{43}\text{S}$  are shown in Fig. 6. In each case gates on the depopulating  $\gamma$ -ray transitions were applied, and feeding from the higher-lying states was subtracted using the level scheme of  $^{43}\text{S}$  and the efficiency of the  $\gamma$ -ray detectors at the respective energies. The data are compared to theoretical calculations of neutron knockout from the  $l = 1, 2,$  and  $3$  single-particle orbits using the eikonal reaction model [46, 47]. In this approach the projectile and target densities, taken from a Skyrme Hartree-

TABLE II. Inclusive and exclusive cross sections to bound final states.  $(nlj)$  refers to the quantum numbers used in the calculation of the single-particle cross section,  $\sigma_{\text{sp}}$ , in the eikonal reaction theory.

$E$ (keV)	$J^\pi$	$\sigma_{\text{exp}}$ (mb)	$(nlj)$	$\sigma_{\text{sp}}$ (mb)	$C^2S_{\text{exp}}$
0	$3/2^-$	12(4)	$2p_{3/2}$	21.7	0.55(17)
228	$(1/2^-)$	0.4(1)	$2p_{1/2}$	20.8	0.019(4)
320	$7/2^-$	43(3)	$1f_{7/2}$	14.3	3.00(21)
977	$7/2^-$	1.2(6)			
1155	$3/2^-_2, (1/2^-)$	8.2(9)	$2p_{3/2}$	18.7	0.44(5)
1162	$3/2^-_3, (1/2^-)$	5.3(3)	$2p_{3/2}$	18.6	0.28(2)
1209	$3/2^-_4, (1/2^-)$	3.3(3)	$2p_{3/2}$	18.5	0.18(1)
1780		0.0(4)			
1854		2.3(3)			
2600	$3/2^+_1, (5/2^+)$	8.8(4)	$1d_{3/2}$	10.7	0.83(4)
2628	$7/2^-_3, (5/2^-)$	3.9(3)	$1f_{7/2}$	12.2	0.32(3)
inclusive		91(4)			

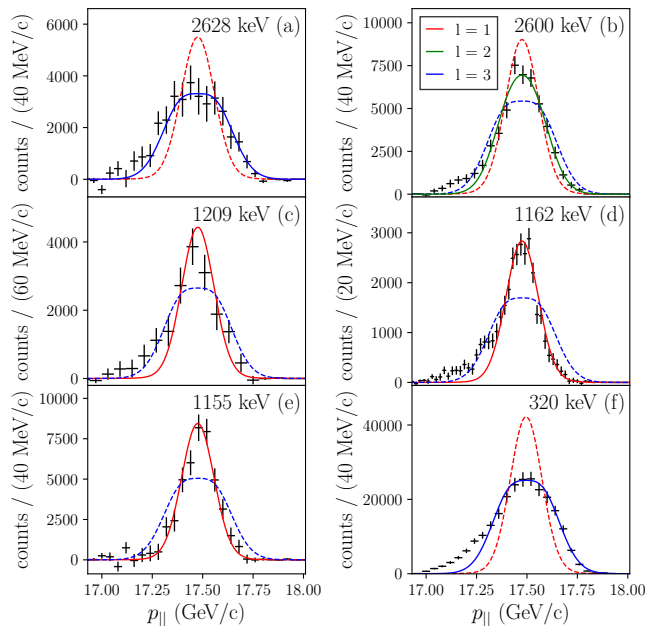


FIG. 6. Parallel momentum distributions of the one-neutron knockout reaction for several states in  $^{43}\text{S}$ . Each panel shows the experimental parallel momentum distribution obtained by gating on  $\gamma$ -ray transitions in black, compared to theoretical eikonal reaction model calculations for removal of a neutron from the  $p$  (red),  $d$  (green), and  $f$  (blue) orbital. Panel (f) is the momentum distribution extracted in coincidence with the isomeric transition measured in IsoTagger and all others are obtained by gating prompt transitions measured in GRETTINA.

Fock calculation for the projectile and assuming a Gaussian distribution for the light target, are used to construct the eikonal  $S$  matrices for the ejectile- and nucleon-target interaction. The radial wave functions of the removed nucleon from each of the active orbitals are calculated in Woods-Saxon potentials with geometries constrained by

the rms radius of the orbital from the Hartree-Fock calculation. The calculated parallel momentum distributions were transformed into the laboratory system and folded with the experimental momentum resolution that was obtained from dedicated calibration runs. The theoretical calculations are normalized to the experimental counts in the 17.3 to 17.8 GeV/c momentum region. This momentum region was selected to eliminate the lower momentum tail region which is not reproduced by the eikonal reaction theory. The states at 1155, 1162, and 1209 keV are well explained by neutron knockout from a  $l = 1$   $p$  orbital, probing the occupation of neutron orbits above the  $N = 28$  shell gap in the ground state of  $^{44}\text{S}$ . On the other hand, the momentum distributions for the state at 2628 keV and the isomeric state at 320 keV are consistent with neutron knockout from the  $l = 3$  orbit. Thus, the spin-parity of the isomeric state of  $^{43}\text{S}$ , already established as  $7/2^-$  [24], is confirmed in the present work. It is interesting to note that the momentum distribution of the state at 2600 keV, shown in Fig. 6 (b), can only be reproduced by assuming removal of a neutron from the  $1d_{3/2}$  orbital with  $l = 2$ . This state is located close to the neutron separation energy [45] and a candidate for a hole state in the  $1d_{3/2}$  orbital below  $N = 20$ . Such a state would not be populated in proton removal reactions in agreement with its non-observation [32, 33]. By subtracting the distributions of all excited states from the inclusive one, the momentum distribution and cross section directly populating the ground state of  $^{43}\text{S}$  via one-neutron knockout reaction was extracted. Due to ambiguities in the level scheme and the unplaced prompt  $\gamma$  rays, the distinction between the neutron knockout from the  $f$  and  $p$  orbits is less clear, but the momentum distribution is well described by knockout from the  $2p_{3/2}$  orbital. In the following discussion, the spin-parity of the ground state of  $^{43}\text{S}$  is assumed to be  $3/2^-$ , which was suggested from the transition rate from the  $7/2^-$  isomeric state to the ground state [24]. The momentum distribution for the 977 and 1856 keV states are asymmetric and very broad, suggesting the population via a non-direct process. This would be expected from a collective rotational band member [27, 42].

Using the eikonal reaction model calculations, the single-particle cross sections  $\sigma_{\text{sp}}$  were calculated (see Table II). These depend on the effective separation energy for the final state and the quantum numbers of the orbital the nucleon was removed from. Using the spin and parity assignments shown in Fig. 5 the spectroscopic factors,  $C^2S_{\text{exp}} = \sigma_{\text{exp}}/\sigma_{\text{sp}}$ , for each state were obtained. They are listed in Table II.

#### IV. DISCUSSION

The experimental level scheme is compared to the results of shell model calculations in Fig. 5. Two effective interactions in the full proton  $sd$  and neutron  $fp$  model space were used to calculate the excitation ener-

TABLE III. Results of the shell model calculations with the SDPF-U [29] and SDPF-MU [14] effective interactions. In addition to the bound states populated in the one-neutron knockout reaction, the members of rotational bands discussed in the text are listed.

SDPF-U				SDPF-MU			
$E$ (keV)	$J^\pi$	$C^2S$	band	$E$ (keV)	$J^\pi$	$C^2S$	band
0	$3/2_1^-$	0.64	(a)	0	$3/2_1^-$	0.58	(a)
298	$1/2_1^-$	0.15	(a)	134	$1/2_1^-$	0.11	(a)
750	$7/2_1^-$	2.66	(b)	601	$7/2_1^-$	2.57	(b)
1010	$7/2_2^-$	0.36	(a)	875	$3/2_2^-$	0.40	(c)
1401	$5/2_1^-$	0.01	(a)	935	$7/2_2^-$	0.32	(a)
1405	$3/2_2^-$	0.23		1035	$5/2_1^-$	0.01	(a)
1990	$5/2_2^-$	0.07	(c)	1444	$5/2_2^-$	0.10	(c)
2053	$1/2_2^-$	0.05		1665	$1/2_2^-$	0.07	
2132	$5/2_3^-$	0.00		2143	$9/2_1^-$		(b)
2366	$9/2_1^-$		(b)	2196	$3/2_3^-$	0.03	
2479	$7/2_3^-$	1.87	(c)	2198	$5/2_3^-$	0.04	
2602	$3/2_3^-$	0.01		2466	$7/2_3^-$	1.46	(c)
3473	$11/2_1^-$		(b)	2496	$5/2_4^-$	0.08	
				2655	$1/2_3^-$	0.01	
				2722	$7/2_4^-$	0.51	
				3651	$11/2_1^-$		(b)

gies, transition probabilities, and spectroscopic factors. Effective charges ( $e_p = 1.35, e_n = 0.35$ ) and  $g$  factors suggested in Ref. [28] have been used. The SDPF-U [29] and SDPF-MU [14] interactions have been previously applied to  $^{43,44}\text{S}$  [14, 15, 25, 28, 33] and predict, at first glance, very similar level schemes shown in Fig. 5. The calculated energies, spectroscopic factors, and band assignments are listed in Table III.

In both cases, three rotational bands are predicted and these are labeled (a), (b), (c) in Table III. For the case of the SDPF-U interaction the band structure in  $^{43,44}\text{S}$  is extensively discussed in Ref. [28]. The collective  $7/2_2^-$  state at 977 keV is a member of the ground state band (a). Based on the comparison with the shell model calculation the 228 keV transition is a candidate for the decay from the  $1/2_1^-$  state. In the shell model calculations, the  $5/2_1^-$  state is predicted to decay to the  $1/2_1^-$  state with a large  $B(E2)$  value, but no such state was observed in the present work. The small cross sections for the  $1/2_1^-$  and  $7/2_2^-$  states suggest that they are not of single-particle character, in agreement with the calculations.

In the present work, we have for the first time identified a state built on top of the isomer. The state at 1854 keV decays to the  $7/2^-$  isomer via the 1532 keV transition (see Fig. 4). The 1856 keV transition has been tentatively assigned to a ground state decay. This would limit the spin and parity values to  $J^\pi = (3/2, 5/2, 7/2)^-$ . The momentum distribution for this state is rather broad, but no conclusion can be drawn. The state could be a candidate for the oblate  $3/2^-$  band head predicted by the AMD calculations whose main decay branch is to the triaxial  $7/2^-$  isomeric states [26]. The shell model calculations do not predict a candidate for a corresponding state, but

rather states with a  $J^\pi = 7/2^-, 9/2^-, 11/2^-$  sequence (band (b)) are predicted, where the  $9/2_1^-$  state is connected by strong  $M1$  ( $0.24 \mu_N$ ) and  $E2$  ( $110 \text{ e}^2\text{fm}^4$  for the SDPF-MU interaction to the  $7/2^-$  isomer. For SDPF-U the values are similar (see [28]). If the 1856 keV transition is placed elsewhere in the level scheme, the 1854 keV state could be a natural candidate for the  $9/2_1^-$  state. A firm spin and parity assignment for the 1854 keV state is required in order to draw further conclusions. Finally, a third band-like structure is built on the  $3/2_2^-$  state at 1155 keV. The  $7/2_3^-$  state at 2628 keV decays to the state at 1780 keV via the 850 keV transition, as well as to the 1155 or 1162 keV state by emission of a 1469 keV  $\gamma$  ray. The 1780 keV state is not populated directly, it decays via the 625 keV transition, a likely spin assignment is thus  $5/2^-$ . The  $3/2^-$  and  $7/2^-$  states can be associated with the shell model states at 1405 (875) and 2479 (2466) or 3093 (2722) keV in the SDPF-U (SDPF-MU) results, based on the comparison of the spectroscopic factors. However, none of the shell model states shows a decay pattern similar to the experimentally observed one. The decay of these is fragmented to several states below with individual  $B(E2)$  values around 1-100  $\text{e}^2\text{fm}^4$ . The  $7/2_3^-$  member of the second prolate band (c) at 2479 keV predicted by the SDPF-U calculations [28], for example, has a strong  $B(E2)$  value for the decay to the  $5/2_2^-$  band head (1990 keV), but the predicted branching ratio is only 15.2 % owing to the higher energy difference for the other possible decays to lower lying states. Furthermore, the SDPF-MU calculations, in contrast with those using SDPF-U, predict a strong transition from the  $5/2_2^-$  state to the  $3/2_2^-$  state suggesting a  $3/2^-$  band head instead, more in line with the results from the AMD calculations [26]. Clearly, more experimental investigation is required to establish the band structure and determine its deformation characteristics.

The neutron knockout cross sections to the bound, shell-model final states in  $^{43}\text{S}$  have been calculated using the theoretical spectroscopic factors  $C^2S$  and the single-particle cross sections  $\sigma_{\text{sp}}$

$$\sigma(J^\pi) = \left( \frac{A}{A-1} \right)^N C^2S(J^\pi) \sigma_{\text{sp}}(nlj, S_n + E(J^\pi)).$$

They are compared to the experimental results in Fig. 5. The inclusive theoretical cross section was calculated by summing the contributions of all states up to the experimental neutron separation energy  $S_n(^{43}\text{S}) = 2629 \text{ keV}$  [45]. The inclusive cross section amounts to 94.3 (91.7) mb for the SDPF-U (SDPF-MU) interactions. Experimentally the cross section populating positive parity states by  $sd$ -shell neutron removal, which are outside of the model space of the calculations, amounts to at least 8.8(4) mb. An estimate for the reduction factor  $R_S$  [47, 48] is thus given by the ratio of the cross section to  $fp$  states to the theoretical value and amounts to 0.87(0.90) for the two effective interactions, in line with the systematics [47, 48].

541 The isomeric  $7/2_1$  state carries the major fraction of  
 542 the single-particle strength, but still significantly less  
 543 than expected from a pure  $\nu(f_{7/2})^{-1}$  configuration. This  
 544 is in agreement with the interpretation of the electric  
 545 quadrupole moment of this state [25], which is signifi-  
 546 cantly larger than expected for a single hole in the  $1f_{7/2}$   
 547 orbital. The shell model calculations predict that a large  
 548 fraction of the  $1f_{7/2}$  strength is located close to the neu-  
 549 tron separation energy. Experimentally, the strength to  
 550 unbound states is inaccessible in the present setup, there-  
 551 fore, part of the  $1f_{7/2}$  strength could be missed in the ex-  
 552 periment. Three states with significant  $l = 1$  strength are  
 553 observed around 1200 keV. This is not reproduced by the  
 554 shell model calculations which predict only one excited  
 555  $3/2^-$  state in this energy region. The 1162 keV state de-  
 556 cays to the 977 keV  $J^\pi = 7/2^-$  state. The lifetime of this  
 557 state, if the present level ordering is adopted, amounts  
 558 to 15(2) ps [33]. Such a state is not found in the shell  
 559 model calculations. The spectroscopic factors for  $1/2^-$   
 560 and  $5/2^-$  states are small as it is expected that the occu-  
 561 pation of the  $2p_{1/2}$  and  $1f_{5/2}$  orbitals in the ground state  
 562 of  $^{44}\text{S}$  is small.

563 The spectroscopic factors can also be compared to  
 564 the  $N = 28$  isotones.  $^{47}\text{Ca}$  has been studied in detail  
 565 by pickup transfer reactions using  $^{48}\text{Ca}$  targets. The  
 566 spectroscopic factor for the ground state amounts to  
 567  $C^2S = 6.22$  [49]. Using the typical reduction  $R \approx 0.7$  of  
 568 the spectroscopic strength when comparing to the shell  
 569 model and assuming this reduction is applicable to each  
 570 transition, this compares well with the expectation of  
 571 the independent particle model of  $C^2S = 8$  for the  $1f_{7/2}$   
 572 orbital. For the  $3/2^-$  state at 2014 keV only a small  
 573 spectroscopic factor of  $C^2S = 0.1$  was found. For the  
 574 radioactive  $^{45}\text{Ar}$  nucleus a measurement of the neutron  
 575 knockout reaction from  $^{46}\text{Ar}$  also found a small spectro-  
 576 scopic factor for the first excited  $3/2_1^-$  state of 0.2(2) [5].  
 577 In the same experiment, the ground state was populated  
 578 with a spectroscopic factor of  $C^2S = 4.9(7)$ . These values  
 579 are in qualitative agreement with the shell model calcula-  
 580 tions which predict spectroscopic factors of 0.59 and 5.34  
 581 for the SDPF-U and 0.79 and 5.00 for the SDPF-MU in-  
 582 teractions. The results indicate that  $N = 28$  is a good  
 583 shell closure in Ca and Ar nuclei.

584 In the present work, the spectroscopic strength for the  
 585 population of the first  $7/2^-$  state amounts to 3.00(21),  
 586 significantly lower than for the heavier isotones. The  
 587 spectroscopic factor for the  $3/2^-$  ground state is 0.55(17).  
 588 However, several other states are populated by the re-  
 589 moval of a neutron from the  $p$  orbitals, as evidenced from  
 590 the momentum distributions shown in Fig. 6. While the  
 591 present experiment cannot distinguish between removal  
 592 of a  $2p_{3/2}$  and a  $2p_{1/2}$  neutron, the latter is unlikely as  
 593 the  $2p_{1/2}$  is expected to lie higher in energy. The shell  
 594 model calculations also do not predict large spectroscopic  
 595 factors for the  $J^\pi = 1/2^-$  states (see Table III). The  
 596 observed fragmentation of the  $2p_{3/2}$  strength is not pre-  
 597 dicted by the shell model calculations. If the experimen-  
 598 tal spectroscopic factors for the  $2p$  states are added, and

599 normalized using the reduction factor [47, 48],  $R_S$ , as  
 600 determined from other nuclei as a function of the sep-  
 601 aration energies, the summed normalized spectroscopic  
 602 strength can be used as an indicator for the occupation  
 603 number. In the present case the sum amounts to 1.8(4)  
 604 where the uncertainty is dominated by a systematic un-  
 605 certainty of  $R_S$  which has been assumed to be 20%. This  
 606 suggests that the ground-state configuration of  $^{44}\text{S}$  is  
 607 composed of up to two neutrons in the  $2p_{3/2}$  orbital.  
 608 The shell model calculation for the summed spectroscopic  
 609 strengths amount to  $\sum C^2S(1f_{7/2}) = 4.89$  (4.35) and  
 610  $\sum C^2S(2p_{3/2}) = 0.89$  (1.01) for the SDPF-U (SDPF-  
 611 MU) interactions. The occupation numbers for the  $2p_{3/2}$   
 612 orbital in the ground state of  $^{44}\text{S}$  are 1.18 and 1.38, re-  
 613 spectively. If the cross-shell  $\pi sd - \nu fp$  tensor compo-  
 614 nent of the SDPF-MU matrix elements is removed, the  
 615 summed spectroscopic strength, up to  $S_n$ , increases to  
 616 5.26 for the  $1f_{7/2}$  orbital. This is in line with the in-  
 617 terpretation that the proton-neutron tensor interaction  
 618 is driving the shell evolution in this exotic region of the  
 619 nuclear chart [14].

620 The location of the  $7/2^-$  and  $3/2^-$  states in  $^{43}\text{S}$  already  
 621 suggested the inversion of the normal  $(1f_{7/2})^{-1}$  and in-  
 622 truder  $(2p_{3/2})$  neutron configurations. The present ex-  
 623 periment proves for the first time an intruder dominance  
 624 of the ground state of  $^{44}\text{S}$ . This is significantly different  
 625 from the less exotic isotones, and the increase in  $2p_{3/2}$   
 626 configurations in the ground state of  $^{44}\text{S}$  compared to  
 627  $^{46}\text{Ar}$  is abrupt. In the even more exotic isotone  $^{41}\text{Si}$  only  
 628 one transition was observed [50], however, many more  
 629 low-lying states are expected based on the shell model  
 630 calculations.  $^{41}\text{Si}$  would be an ideal testing ground for  
 631 the shell model calculations, since there the SDPF-U(-SI)  
 632 and SDPF-MU interactions predict very different spec-  
 633 troscopic factors for the one-neutron removal reaction  
 634 from  $^{42}\text{Si}$ .

635 Finally, in the present experiment the population of a  
 636 positive parity state at 2600 keV was observed. The spec-  
 637 troscopic factor amounts to 0.83(4) assuming removal of  
 638 a neutron from the  $1d_{3/2}$  orbital. This value can be com-  
 639 pared to the isotone  $^{47}\text{Ca}$ , where the  $3/2_1^+$  state is lo-  
 640 cated at 2580 keV and has a deduced spectroscopic factor  
 641 of 1.18 [49], determined from the  $(d, t)$  transfer reaction  
 642 measurement. This state lies outside of the model space  
 643 and is not described with the present shell model calcu-  
 644 lations.

## 645 V. SUMMARY AND OUTLOOK

646 In summary, we have performed spectroscopy of  $^{43}\text{S}$   
 647 using the one-neutron knockout reaction from  $^{44}\text{S}$ . Using  
 648 prompt and delayed  $\gamma$ -ray spectroscopy in coincidence,  
 649 the level scheme of  $^{43}\text{S}$  was constructed. Previously, this  
 650 was beset with ambiguities due to the presence of a long-  
 651 lived isomeric state in  $^{43}\text{S}$ . Final-state exclusive momen-  
 652 tum distributions of the residue allowed for firm spin and  
 653 parity assignments. The level ordering and assignments



of a recent lifetime measurement [33] were revised. A state above the isomer was identified for the first time, but its properties could not be reproduced using shell model calculations. Coulomb excitation measurements using an isomeric  $^{43}\text{S}$  beam could help in resolving this issue. A band-like structure built on a  $3/2^-$  state was observed, but further experimental investigation is required to confirm a band and determine its properties. The cross sections for the population of states originating from the removal of a  $2p_{3/2}$  neutron from the  $^{44}\text{S}$  ground state were found to be large. This is a direct measure of the amount of intruder configuration in the ground state of  $^{44}\text{S}$  and quantifies the  $N = 28$  shell quenching in this exotic nucleus.

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