Proton Shell Evolution below $^{132}$Sn: First Measurement of Low-Lying $\beta$-emitting Isomers in $^{123,125}$Ag


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(Dated: April 26, 2019)

The $\beta$-delayed $\gamma$-ray spectroscopy of neutron-rich $^{123,125}$Ag isotopes is investigated at the Radioactive Isotope Beam Factory of RIKEN and the long-predicted $1/2^-$ $\beta$-emitting isomers in $^{123,125}$Ag are identified for the first time. With the new experimental results, the systematic trend of energy spacing between the lowest $9/2^+$ and $1/2^-$ levels is extended in Ag isotopes up to $N = 78$, providing a clear signal for the reduction of the $Z = 40$ subshell gap in Ag towards $N = 82$. Shellmodel calculations with the state-of-the-art $V_{\text{MU}}$ plus $M3Y$ spin-orbit interaction give a satisfactory description of the low-lying states in $^{123,125}$Ag. The tensor force is found to play a crucial role in the evolution of the size of the $Z = 40$ subshell gap. The observed inversion of the single particle levels around $^{123}$Ag can be well interpreted in terms of the monopole shift of the $\pi 1g_{9/2}$ orbitals mainly caused by the increasing occupation of $\nu 1h_{11/2}$ orbitals.
With nuclear physics studies moving towards radioactive nuclei far from the $\beta$-stability line over the last decades, the well-known magic nucleon numbers (8, 20, 28, 50, 82, and 126) were found to be not necessarily immutable across the nuclear chart [1, 2]. To investigate the underlying mechanism which alters the magic numbers, considerable experimental and theoretical efforts have been made. Nowadays the evolution of shell structure is known to be largely affected by the strong nucleon-nucleon tensor interaction [3–6].

In recent years, many attentions are focused on the detailed location and magnitude of shell and subshell gaps in different mass regions [1, 6–10]. One of the regions of particular interest lies below the doubly magic nucleus $^{132}$Sn. A quenching of the $N = 82$ shell gap was predicted a long time ago [11–13] to take place below $^{132}$Sn. Due to experimental difficulties to produce these extremely neutron-rich nuclides, so far only a few nuclides below $Z = 50$ have been studied around $N = 82$. Recent experimental studies have shown that the $N = 82$ shell closure in $^{132}$Sn, $^{130}$Cd, $^{128}$Pd isotones is still robust [14–18], but a significant reduction of the $N = 82$ gap was suggested to occur between Sn and Zr as a consequence of the absent $Z = 40$ subshell gap [7]. Therefore, when moving away from $Z = 50$, it is very important to further investigate where the predicted quenching of the $N = 82$ shell gap and the $Z = 40$ subshell gap [7, 19] will occur, as well as how the neutron shell gap and proton subshell gap influence each other. In addition, nuclei close to $^{132}$Sn and their structure properties are relevant for the astrophysical rapid neutron-capture process, the $r$-process [20, 21]. A good understanding of the $N = 82$ magic shell and its evolution along the $r$-process path is of crucial importance for the nucleosynthesis calculations in this region [20].

Owing to recent developments in producing intense rare isotope beams worldwide in combination with efficient particle and $\gamma$-ray detection systems, it has become possible to make detailed spectroscopic studies of neutron-rich nuclei below $^{132}$Sn. With the $Z = 47$, the neutron-rich odd- $A$ Ag isotopes are naturally of great interest. Their valence protons are assumed to fill the $\frac{1}{2}^+_{9/2}$ and $\pi 2p_{1/2}$ orbitals, between which the $Z = 40$ subshell gap is formed. Consequently, the energy difference between the lowest-lying $9/2^+$ and $1/2^+$ states in these neutron-rich odd- $A$ Ag isotopes provides direct information on the $Z = 40$ subshell gap.

To illustrate how the $Z = 40$ subshell gap evolves in Ag isotopes, the energy differences between the lowest $9/2^+$ and $1/2^+$ states are summarized for odd- $A$ silver isotopes with $N = 48$ - 78 in Fig. 1. On the neutron-deficient side, the systematic trend of the energy spacing, as well as theoretical calculations [26, 27], suggest a maximum at $N = 50$, manifesting the stability of both $Z = 40$ and $N = 50$ shell gaps in Ag isotopes. With the increase of neutron number, this energy difference drops quickly. At $^{105}$Ag ($N = 58$), the ordering of these two levels swaps and the $1/2^−$ state becomes the lowest state. The energy splittings between the lowest $9/2^+$ and $1/2^+$ states are relatively flat in the neutron mid-shell region till $^{119}$Ag ($N = 72$) where the $1/2^−$ isomeric state was proposed to lie between the $7/2^+$ ground state and the $9/2^+$ excited state at 130 keV [24, 28]. For nuclei beyond $^{119}$Ag, so far only the $9/2^+$ states are assigned in $^{121,123,125}$Ag mainly based on the systematics [29–33], while no experimental information on $1/2^−$ states is available. Therefore, it is very interesting to see how the $1/2^−$ state will evolve with respect to the $9/2^+$ state in the heavier Ag isotopes when approaching $N = 82$: will it remain below the $9/2^+$ state or get even lower, or will the order of the states change?

In this Letter, we report on spectroscopic studies of neutron-rich odd-A Ag isotopes via $\beta$ decay of Pd isotopes. The aim of the present study is to determine the positions of the $2p_{1/2}$ proton-hole states in neutron-rich $^{123,125}$Ag isotopes.

The experiment was performed at the Radioactive Isotope Beam Factory (RIBF) facility [34] at RIKEN in the framework of the EURICA project [35, 36]. A primary beam of 345 MeV/u $^{238}$U$^{86+}$, with an intensity of 7 - 12 pA, impinged into a 3-mm-thick Be target. The ions of interest were separated and identified event by event by the BigRIPS and ZeroDegree spectrometers [37]. A total of about $7.0 \times 10^6$ $^{123}$Pd$^{46+}$ and $2.4 \times 10^6$ $^{125}$Pd$^{46+}$ ions were implanted into an active stopper, named WAS3ABi [35], which consisted of eight compactly stacked double-sided silicon-strip detectors (DSSDs). The WAS3ABi array also served as a detector for the beta particles (electrons). Gamma rays emitted after the $\beta$ decays of the implanted ions were detected with the EURICA spectrometer [36], which con-

\[ E_{1/2} - E_{9/2} \text{[MeV]} \]

FIG. 1. Systematics of experimental energy differences between the lowest-lying $1/2^−$ and $9/2^+$ states in Ag isotopes. Data are taken from Refs. [24, 25] (black filled circles) and present work (red filled circles). The dashed blue arrows are drawn to guide the eye. The range of the shaded region for $^{119}$Ag corresponds to the uncertainties of the experimental data.
sisted of 84 high-purity germanium crystals grouped in 12 clusters.

The ground state of $^{123}$Ag has been assigned as 7/2$^+$ based on the systematics and its decay pattern [30-32]. A low-lying 9/2$^+$ level only 27-keV above the 7/2$^+$ ground state has been reported in $^{125}$Ag [30, 31]. The ground state of $^{125}$Ag was assigned as 9/2$^+$ based on the similar $\gamma$-decay pattern as $^{123}$Ag, and on the systematics [30, 31]. In the previous studies [30, 31], a short-lived (sub-microsecond) 17/2$^-$ isomeric state was observed in both $^{123}$Ag and $^{125}$Ag, and their $\gamma$-decay schemes were established. In the present work, most of the previously reported $\gamma$ transitions following the 17/2$^-$ isomeric decay in $^{123}$Ag and $^{125}$Ag can be clearly seen in the $\beta$-delayed $\gamma$-ray spectra of corresponding Pd isotopes, as shown in Figs. 2(a) and 3(a). Besides, many new $\gamma$ rays are observed.

The partial level schemes of $^{123}$Ag and $^{125}$Ag deduced from the present work, are shown in Fig. 4. It can be seen that these two isotopes have a similar decay pattern. Figs. 2(b) and 3(b) present examples of coincidence spectra in $^{125}$Ag and $^{125}$Ag, respectively. For $^{123}$Ag, the 611.0-keV transition has a clear coincidence with the 1009.2-keV transition, as well as with the 383.1- and 594.0-keV transitions. Meanwhile, the 383.1- and 594.0-keV transitions are found to be in coincidence with each other but not with the 1009.2-keV transition. The coincidence pattern suggests that the 611.0-keV transition feeds a level, which decays via two parallel transition paths. One deexcites via the 1009.2-keV transition and the other decays via a transition sequence of 383.1- and 594.0-keV.

For $^{125}$Ag, the 625.4-keV transition has a clear coincidence with the 1118.5-keV transition, as well as with the 415.1- and 606.3-keV transitions (see Fig. 3(b)). The 415.1- and 606.3-keV transitions are found to be in coincidence with each other but not with the 1118.5-keV transition. Based on the $\gamma-\gamma$ coincidence, intensity balance and systematics of the odd-A Ag isotopes, for $^{125}$Ag, the 415.1-, 606.3-keV transition sequence is suggested to deexcite to the 1/2$^-$ long-predicted isomeric state and the 1118.5-keV transition decay to the 9/2$^+$ ground state. The remarkable similarity of $\gamma-\gamma$ coincidence of $^{123,125}$Ag suggests that for $^{123}$Ag, the 383.1 keV - 594.0 keV transition sequence feeds the 1/2$^-$ isomeric state, and the 1009.2-keV transition decay to the 9/2$^+$ state.

The 1/2$^-$ states in $^{123,125}$Ag are predicted to be $\beta$-decaying isomers. To further explore their decays to Cd isotopes, an asymmetric matrix with $\gamma$ rays from the daughter Ag nuclei on one axis and $\gamma$ rays from the granddaughter Cd nuclei on the other axis, was constructed. To get clean coincident $\gamma$-ray spectra, the time ranges of $\gamma$-rays from mother nuclei decay and daughter nuclei decay are set as twice the half-life for each of the respective nuclei. Figs. 2(c), (d) and Figs. 3(c), (d) exhibit the $\gamma$-ray spectra of the granddaughter nuclei $^{123}$Cd and $^{125}$Cd with gates on the $\gamma$-rays of the daughter nuclei $^{123}$Ag and $^{125}$Ag, respectively. As illustrated in Fig. 2(c),
with gates on the known 713.6-, 629.7- and 685.3-keV γ-transitions which finally feed the 7/2+ ground state of 123Ag, a strong 263.9-keV γ-ray and several relative weak 116.4-, 123.7-, 409.8-, and 591.3-keV γ-rays can be clearly seen. In contrast, with gates on the γ-rays at energies of 325.1-, 383.1- and 594.0-keV which finally feed the 1/2− isomeric state of 123Ag, the 123.7-keV transition becomes the strongest (although the 263.9-keV gamma-ray can also been seen in Fig. 2(d)). Furthermore, the resulting γ-ray spectrum of granddaughter 123Cd with gate on the 1009.2-keV transition in 123Ag shown in the inset of Fig. 2(c) is very similar to Fig. 2(c) rather than Fig. 2(d). Such different populating patterns in granddaughter 123Cd reveal that these two groups of γ-ray transitions (i.e., the 713.6-, 629.7-, 685.3-, 1009.2-keV transitions and 325.1-, 383.1-, 594.0-keV transitions) finally feed the different β-decaying states in 123Ag, which firmly verify the identification of 1/2− isomeric state in 123Ag in the present work. As shown in Figs. 3(c),(d), the different populating patterns can also be seen in 125Cd.

To further probe the nature of the low-lying states in 123Ag and 125Ag, shell-model calculations have been performed using the KSHELL code [38] with the state-of-the-art monopole-based universal interaction $V_{MU}$ plus a spin-orbit force from M3Y($V_{MU}+LS$) [4, 39]. The $V_{MU}$ interaction consists of a Gaussian central force and a tensor force [4], and has successfully been applied to describe the shell structure of exotic nuclei in many regions [5, 40–43]. In the present calculations, the model space consists of four proton orbitals (1f5/2, 2p3/2, 2p1/2, 1g9/2) and five neutron orbitals (1g7/2, 2d5/2, 3s1/2, 1h11/2, 2d3/2) with $^{78}$Ni as an inert core. Since the deeply bound proton orbitals (1f5/2, 2p3/2) and neutron orbitals (1g7/2, 2d5/2) are not expected to play major roles in the low-lying states in Ag isotopes, these orbitals are fully occupied. The calculated levels are plotted in Fig. 4 in comparison with the experimental results. It can be seen that shell-model calculations give an overall satisfactory description of experimental levels in 123,125Ag, particularly for the low-lying levels. The calculations indicate that as approaching $N = 82$, the wave functions from the $\pi 1g9/2$ and $\pi 2p1/2$ orbitals dominate low-lying states of

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**FIG. 4.** Partial level schemes of $^{123}$Ag and $^{125}$Ag constructed in this work in comparison with the shell-model calculations. The experimental information of 17/2− isomeric states in $^{123,125}$Ag, which are not/weakly populated in the present work due to the selection rule, are taken from Ref. [30]. The arrow widths are proportional to their absolute intensities.
Ag isotopes.

With the newly observed 1/2− isomeric states in 123,125Ag, Fig. 1 shows that the 9/2+ and 1/2− levels swap their ordering again around 125Ag. The systematic energy difference indicates an increasing trend beyond 125Ag, which reveals that the Z = 40 subshell gap formed between the π1g9/2 and π2p1/2 orbitals starts to be restored toward N = 82. It is worth emphasizing that although the energy difference between the 9/2+ and 1/2− levels shows a similar trend toward N = 82 as that toward N = 50, the slope at neutron-rich side is obviously much less steep than on the neutron-deficient side close to N = 50. Extrapolating the trend toward N = 82, a considerable diminishment of the Z = 40 subshell gap is expected.

To get more insight into the microscopic origin of shell evolution in this region, the effective single particle energies (ESPEs) are calculated for the proton orbitals in the region of N = 68 - 82 with the V_{MU}+LS interaction and shown in Fig. 5(a). Here, the V_{MU} interaction is decomposed into the two components, i.e. the central and tensor parts, to identify their possible effects on the shell evolution. To show the influence from the neutron ν1h11/2 orbital in the proton-neutron tensor force, the calculated neutron occupation number in the 1h11/2 shell is presented in Fig. 5(b). It can be seen that if only the central + spin-orbit parts are considered, the π2p1/2 orbital lies below the π1g9/2 orbital in the whole region of N = 68 - 82 (see dashed lines in Fig. 5(a)). In contrast, with inclusion of the tensor part (especially the π1g9/2-ν1h11/2 monopole), π1g9/2 orbital is affected much more than the π2p1/2 orbital and the spacing between π1g9/2 and π2p1/2 orbitals is notably reduced (see solid lines in Fig. 5(a)), consequently results in the inversion of these two orbitals at N ∼ 74, which is compatible with the experimental inversion position. In view of this picture, the tensor force manifests its crucial role in the modification of the order of the proton orbitals and the size of the Z = 40 subshell gap in Ag isotopes mainly through the π1g9/2-ν1h11/2 monopole. Vice versa, our calculations indicate that this tensor force will also influence the behavior of the ν1h11/2 orbital, which is important for the N = 82 shell gap.

In conclusion, spectroscopic studies of neutron-rich 123,125Ag have been performed via the β-decays of 123,125Pd at RIKEN and the long-predicted 1/2− isomeric states in 123,125Ag have been successfully identified for the first time. The systematic trend of the energy spacing between the lowest-lying 9/2+ and 1/2− levels in the Ag isotopes provides a clear signal of a reduction of the Z = 40 subshell as approaching N = 82. Shell model calculations with the V_{MU}+LS interaction reproduce well the experimental low-lying states in 123,125Ag. The tensor force is found to play a crucial role in the evolution of the size of the Z = 40 subshell gap.

This work was carried out at the RIBF operated by RIKEN Nishina Center, RIKEN and CNS, University of Tokyo. We thank the staff at RIBF for providing the beams, the EUROBALL Owners Committee for the loan of germanium detectors, the PreSpec Collaboration for the use of the readout electronics. Part of the WAS3ABy was supported by the Rare Isotope Science Project which is funded by MSIP and NRF of Korea. This work was supported by the National Key R&D Program of China (Contract No. 2018YFA0404403), the National Science Foundation of China under Grant No. 11775003, No. 11675003, No. 11775316, No. 11875075, the National Research Foundation of Korea (No. NRF-2016R1A5A1013277 and NRF-2013M7A1A1075764) and the Spanish Ministerio de Economía y Competitividad under contract FPA2017-84756-C4-2-P. This work was partially supported by JSPS KAKENHI (Grants No. 25247045 and 17H06090). Work at ANL is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics, under contract No. DE-AC02-06CH11357.

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