The VLT-FLAMES Tarantula Survey

XXXI. Radial velocities and multiplicity constraints of red supergiant stars in 30 Doradus

L. R. Patrick\textsuperscript{1,2}, D. J. Lennon\textsuperscript{3,1}, N. Britavskiy\textsuperscript{1,2}, C. J. Evans\textsuperscript{4}, H. Sana\textsuperscript{5}, W. D. Taylor\textsuperscript{4}, A. Herrero\textsuperscript{1,2}, L. A. Almeida\textsuperscript{6}, J. S. Clark\textsuperscript{7}, M. Gieles\textsuperscript{8,9,10}, N. Langer\textsuperscript{11}, F. R. N. Schneider\textsuperscript{12}, and J. Th. van Loon\textsuperscript{13}

\textsuperscript{1} Instituto de Astrofísica de Canarias, 38205 La Laguna, Tenerife, Spain
e-mail: lpatrick@iac.es
\textsuperscript{2} Universidad de La Laguna, Dpto. Astrofísica, 38206 La Laguna, Tenerife, Spain
\textsuperscript{3} Department of Computer Science and Mathematics, European Space Astronomy Centre (ESAC), Camino Bajo del Castillo s/n, Urbanizacion Villafranca del Castillo, Villanueva de la Cañada 28 692, Madrid, Spain
\textsuperscript{4} UK Astronomy Technology Centre, Royal Observatory Edinburgh, Blackford Hill, Edinburgh EH9 3HJ, UK
\textsuperscript{5} Institute of Astrophysics, KU Leuven, Celestijnenlaan 200D, 3001 Leuven, Belgium
\textsuperscript{6} Departamento de Física Teórica e Experimental, Universidade Federal do Rio Grande do Norte, CP 1641 Natal, RN, Brazil
\textsuperscript{7} School of Physical Sciences, The Open University, Walton Hall, Milton Keynes MK7 6AA, UK
\textsuperscript{8} Institute of Astrophysics, KU Leuven, Celestijnenlaan 200D, 3001 Leuven, Belgium
\textsuperscript{9} Departamento de Física Teórica e Experimental, Universidade Federal do Rio Grande do Norte, CP 1641 Natal, RN, Brazil
\textsuperscript{10} ICREA, Pg. Lluís Companys 23, 08010 Barcelona, Spain
\textsuperscript{11} Argelander-Institut für Astronomie, Universität Bonn, Auf dem Hügel 71, 53121 Bonn, Germany
\textsuperscript{12} Department of Physics, University of Oxford, Keble Road, Oxford OX13RH, UK
\textsuperscript{13} Lennard-Jones Laboratories, Keele University, Staffordshire ST5 5BG, UK

Received 20 December 2018 / Accepted 1 March 2019

ABSTRACT

\textbf{Aims.} The incidence of multiplicity in cool, luminous massive stars is relatively unknown compared to their hotter counterparts. In this work we present radial velocity (RV) measurements and investigate the multiplicity properties of red supergiants (RSGs) in the 30 Doradus region of the Large Magellanic Cloud using multi-epoch visible spectroscopy from the VLT-FLAMES Tarantula Survey.

\textbf{Methods.} Exploiting the high density of absorption features in visible spectra of cool stars, we used a novel slicing technique to estimate RVs of 17 candidate RSGs in 30 Doradus from cross-correlation of the observations with model spectra.

\textbf{Results.} We provide absolute RV measurements (precise to better than \( \pm 1 \text{ km s}^{-1} \)) for our sample and estimate line-of-sight velocities for the Hodge 301 and SL 639 clusters, which agree well with those of hot stars in the same clusters. By combining results for the RSGs with those for nearby B-type stars, we estimate systemic velocities and line-of-sight velocity dispersions for the two clusters, obtaining estimates for their dynamical masses of \( \log(M_{\text{dyn}}/M_\odot) = 3.8 \pm 0.3 \) for Hodge 301, and an upper limit of \( \log(M_{\text{dyn}}/M_\odot) < 3.1 \pm 0.8 \) for SL 639, assuming virial equilibrium. Analysis of the multi-epoch data reveals one RV variable, potential binary candidate (VFTS 744), which is likely a semi-regular variable asymptotic giant branch star. Calculations of semi-amplitude velocities for a range of RSGs in model binary systems and literature examples of binary RSGs were used to guide our RV variability criteria. We estimate an upper limit on the observed binary fraction for our sample of 0.3; for this sample we are sensitive to maximum periods for individual objects in the range 1–10 000 days and mass ratios above 0.3 depending on the data quality. From simulations of RV measurements from binary systems given the current data, we conclude that systems within the parameter range \( q > 0.3 \), \( \log P[\text{days}] < 3.5 \) would be detected by our variability criteria at the 90\% confidence level. The intrinsic binary fraction, accounting for observational biases, is estimated using simulations of binary systems with an empirically defined distribution of parameters in which orbital periods are uniformly distributed in the 3.3 < \( \log P[\text{days}] < 4.3 \) range. A range of intrinsic binary fractions are considered; a binary fraction of 0.3 is found to best reproduce the observed data.

\textbf{Conclusions.} We demonstrate that RSGs are effective extragalactic kinematic tracers by estimating the kinematic properties, including the dynamical masses of two LMC young massive clusters. In the context of binary evolution models, we conclude that the large majority of our sample consists of effectively single stars that are either currently single or in long-period systems. Further observations at greater spectral resolution or over a longer baseline, or both, are required to search for such systems.

\textbf{Key words.} binaries: spectroscopic – stars: late-type – Magellanic Clouds – galaxies: star clusters: individual: Hodge 301 – galaxies: star clusters: individual: SL 639

* Full Table A.1 is only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/624/A129

** Based on observations collected at the European Organisation for Astronomical Research in the Southern Hemisphere under ESO programme 182.D-0222.
1. Introduction

A clear picture has emerged that most massive stars reside in multiple systems (Zinnecker & Yorke 2007; Mason et al. 2009; Sana & Evans 2011; Chini et al. 2012; Sana et al. 2014), and ~70% are expected to interact with a companion during their lifetimes (e.g. Sana et al. 2012, 2013, 2014; Duchêne & Kraus 2013; Kobulnicky et al. 2014; Dunstall et al. 2015; Moe & Di Stefano 2017). The ramifications of this are now being explored in detailed simulations of binary populations to understand the impact on, for example massive-star evolution (Eldridge et al. 2008, 2013; de Mink et al. 2013; De Marco & Izzard 2017) and the timescales of core-collapse supernovae (Podsiadlowski et al. 1992; Yoon et al. 2010; Zapartas et al. 2017).

In this context, the cool part of massive-star evolution has received relatively little attention. To some extent the assumption has been that as a massive star cools (extending its radius significantly) any close binary systems simply interacts or merges, or both, such that the star may not even make it all the way across the Hertzsprung–Russell (H–R) diagram, i.e. only currently single (or effectively single) stars evolve to sufficiently large radii so as to become red supergiants (RSGs). Indeed, the large radial extent of RSG atmospheres limits the potential companions in a binary system compared to hotter stars. The most reliable observational estimates of RSG radii are of order 650–1500Session, 2017; Arroyo-Torres et al. 2013, 2015), which immediately rule out short-period systems of the type found in hot stars (e.g. Sana et al. 2012, 2013; Almeida et al. 2017; Lohr et al. 2018). Nonetheless, placing firm constraints on multiplicity in the RSG phase is important, both in terms of understanding the pathways for binary and single stellar evolution as the progenitors of type II supernovae and is particularly relevant for stripped-envelope supernovae of types IIn and Ibn (e.g. Smartt 2009; Eldridge et al. 2013; Götberg et al. 2018).

In contrast to efforts for OB-type stars, multi-epoch studies of the radial velocities (RVs) of RSGs have been somewhat limited to date (e.g. Spencer Jones 1928; Sanford 1933; Smith et al. 1989) and the campaign by Josellin & Plez (2007) provides a useful reference sample. These authors used high-resolution (R ~ 40 000) spectroscopy of 13 Galactic RSGs to estimate precise RVs (to better than 0.1 km s−1) over a 15 month period. These authors estimated “atmospheric” RVs for each target at each epoch, finding two groups: the first with low-level variations (δRV < 5 km s−1) and the second with variations of up to ~10 km s−1 over the full baseline of their observations (see their Fig. 3). In their characterisation of the velocities in different atmospheric layers of their targets, they attributed the variable velocity fields as probably originating from atmospheric convective cells, which is supported by theoretical studies that predict RV variations on similar scales (Schwarzchild 1975; Freytag et al. 2002; Sutshow 2010).

Examples of known RSGs in binary systems can also help guide expectations. VV Cep-type binaries are eclipsing binary systems that have generally been identified by peculiar, variable spectra arising from a companion (typically a B-type star) shining through the atmosphere of the RSG. Some ζ Aur-type binaries contain K-type supergiants with B-type secondaries and are by definition eclipsing systems (Levesque 2017). Typical semi-amplitude velocities within these systems are in the range from 20 km s−1 to 30 km s−1 (e.g. Wright 1977; Eaton & Shaw 2007).

Motivated to obtain better empirical constraints on multiplicity in the cool part of the H–R diagram, we have turned to the cool stars observed as part of the VLT–FLAMES Tarantula Survey (VFTS; Evans et al. 2011, hereafter Paper I). The VFTS obtained multi-epoch optical spectroscopy of ~1000 stars in the 30 Doradus region of the Large Magellanic Cloud (LMC). Although primarily focussed on the OB-type population in this region, the unbiased target selection led to the inclusion of 91 later-type objects (Table 3 in Paper I).

The VFTS observations have been used to estimate the binary fraction of O- and B-type stars (Sana et al. 2013; Dunstall et al. 2015, respectively). In this work we present a similar RV analysis (albeit using very different methods and sample sizes) of the K- and M-type stars observed in the VFTS to investigate their multiplicity. A parallel study (Britavskiy et al. 2019, hereafter B19) presents stellar parameters for the same sample and investigates their evolutionary status.

This paper is organised as follows. In Sect. 2 we describe the observations and target selection for the study. Section 3 presents the RV estimates and a comparison of our results to literature measurements. In Sect. 4 we estimate the kinematic properties and dynamical masses of the two lower mass clusters in the 30 Dor region and highlight the effectiveness of RSGs as kinematic tracers. Section 5 presents a first look at a biniarity analysis of our sample using multi-epoch data, in which we determine an upper limit to the observed binary fraction and the intrinsic binary fraction of our sample using simulations. Conclusions are presented in Sect. 6.

2. Observations

The data were obtained with the VLT–FLAMES spectrograph (Pasquini et al. 2002) as part of the Tarantula Survey. Nine multi-object fibre configurations (Fields A to I) were used to assemble the VFTS sample, and the wavelength coverage and resolving power for the three FLAMES–Giraffe settings are given in Table 1.

The observing strategy involved two back-to-back exposures executed at the telescope in the service queue. To ensure sufficient signal-to-noise (S/N) for quantitative spectral analysis, three observations were obtained with the LR02 and LR03 settings and two with the HR15N setting. Three additional observations were obtained with the LR02 setting to look for RV variations; the last (sixth) epoch is obtained two observing seasons later to give a ~1 yr baseline to improve the detection of long-period systems. There were no strong time constraints on the execution of the first three LR02, nor the LR03/HR15N.

Table 1. Wavelength coverage, resolving power (R), and number of slices used in the RV analysis for the three observed FLAMES–Giraffe settings.

<table>
<thead>
<tr>
<th>Setting</th>
<th>Range (Å)</th>
<th>R (λ/Δλ)</th>
<th>No. slices</th>
</tr>
</thead>
<tbody>
<tr>
<td>LR02</td>
<td>3960–4564</td>
<td>7000</td>
<td>16</td>
</tr>
<tr>
<td>LR03</td>
<td>4499–5071</td>
<td>8500</td>
<td>15</td>
</tr>
<tr>
<td>HR15N</td>
<td>6442–6817</td>
<td>16000</td>
<td>9</td>
</tr>
</tbody>
</table>

Notes:
1. Although we note that four spectroscopic binaries (M-type supergiants with B-type companions) in their initial sample of 23 targets were not followed up by their multi-epoch observations.
2. However, although the ζ Aur stars are typically assumed to be supergiants, estimates of their stellar parameters suggest that the majority are lower mass objects (e.g. Bennett et al. 1996; Eaton & Shaw 2007).
observations, so there is additional temporal information for some of the observed fields. For our current purposes, observations of a given target obtained on the same night were combined to improve the final S/N of the spectra. Full details of the observations are given in Appendix A of Paper I.

Photometric criteria ($V < 16$ mag, $(B - V) > 1$ mag) were used to select the late-type, luminous stars observed by the VFTS, resulting in 18 candidate RSGs. Analysis of their physical parameters by B19 confirms that the large majority of these are RSGs (spanning a wide range in luminosity), but also include what appear to be four massive stars on the asymptotic giant branch (AGB) and one foreground star (VFTS 793, which is removed from the current sample). We note that this sample includes three stars with identifications of the form 2xxx – these were drawn from objects previously excluded from the survey catalogue as potentially foreground stars or LMC members with poor S/N spectra (see Table A.1 in B19).

The RV analysis presented in this work considers the same sample of VFTS objects as B19 (excluding VFTS 793). The locations of the 17 targets in relation to the main clusters/associations in the region are shown in Fig. 1; these include the two older clusters, Hodge 301 (Hodge 1988) and SL 639 (Shapley & Lindsay 1963), for which B19 estimated ages of $24.3^{+3}_{-2}$ Myr and $22.4^{+3}_{-2}$ Myr, respectively.

### 3. Radial velocity analysis

At the resolution of the VFTS data, the high density of absorption features in the optical spectra of RSGs enables precise RVs to be estimated to better than $1 \text{ km s}^{-1}$ in most cases. The RVs for our sample were estimated for each epoch using a slicing approach that splits each spectrum into small wavelength slices. The width and location of these slices are tailored to each setting, ranging from $\sim 30 \text{ Å}$ (LR02) to $45 \text{ Å}$ (HR15N), but kept constant for all targets (see Table 1). Using an iterative cross-correlation approach, these slices are compared to a spectrum calculated from a marcs model atmosphere (Gustafsson et al. 2008) with appropriate physical parameters for a RSG, i.e. $T_{\text{eff}} = 3900 \text{ K}$, $\log g = 0.5$. The final RV estimate for each epoch is the average of the cross-correlation estimates for the slices. The precision of our measurements is estimated using a comparison between all of the slices ($\sigma/\sqrt{N_{\text{slices}}}$, where $N_{\text{slices}}$ is the total number of slices for the spectrum) and, in general, is better than $1 \text{ km s}^{-1}$. Average RVs for each target from all three settings are presented in Table 2, along with the adopted line-of-sight systemic velocities ($v_{\text{ID}}$).

In general we find excellent agreement between the LR02 and LR03 settings, however, there appears to be a systematic offset in the HR15N estimates (with a mean difference of $2.1 \text{ km s}^{-1}$); cf. those from the LR02 and LR03 settings. The reason for this discrepancy is unclear, but is assumed not to be astrophysical in origin. Given this discrepancy, we do not include the HR15N results further in our analysis (unless explicitly specified) and the adopted $v_{\text{ID}}$ is the weighted average of the LR02 and LR03 values. Although potentially greater precision is available from the (higher resolution) HR15N data, in addition to the apparent offset, there were fewer observations with this setting and the S/N tends to be lower.

Comparisons of the RVs estimated for hot stars from the VFTS can provide an independent check of our results as they

---

**Fig. 1.** Spatial distribution of the cool-type stars analysed, labelled by their VFTS identifiers. The spatial extents of NGC 2070, NGC 2060, SL 639, and Hodge 301 (as adopted by Evans et al. 2015), are indicated by the overlaid dashed circles. The underlying image is from a V-band mosaic taken with the ESO Wide Field Imager on the 2.2 m telescope at La Silla. Despite their location within the boundaries of the NGC2060 and NGC2070 clusters, given the ages of these populations, the RSGs in these regions are considered field members.
Table 2. Estimated mean RVs and associated uncertainties from the three spectrograph settings.

<table>
<thead>
<tr>
<th>VFTS ID</th>
<th>Field</th>
<th>RV (km s(^{-1}))</th>
<th>(v_{1D}) (km s(^{-1}))</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>LR02</td>
<td>LR03</td>
<td>HR15N</td>
</tr>
<tr>
<td>0023</td>
<td></td>
<td>270.1 ± 0.4</td>
<td>270.0 ± 0.8</td>
<td>270.7 ± 0.3</td>
</tr>
<tr>
<td>0081</td>
<td>B*</td>
<td>284.9 ± 0.3</td>
<td>285.1 ± 0.9(^{(b)})</td>
<td>287.1 ± 0.3(^{(b)})</td>
</tr>
<tr>
<td>0198</td>
<td>A*</td>
<td>258.2 ± 0.3</td>
<td>257.5 ± 0.6</td>
<td>260.1 ± 0.2</td>
</tr>
<tr>
<td>0222</td>
<td>C*</td>
<td>253.2 ± 0.3(^{(a)})</td>
<td>254.4 ± 0.9(^{(b)})</td>
<td>256.1 ± 0.3</td>
</tr>
<tr>
<td>0236</td>
<td>C*</td>
<td>261.2 ± 0.3(^{(a)})</td>
<td>261.7 ± 0.8(^{(b)})</td>
<td>263.6 ± 0.3</td>
</tr>
<tr>
<td>0275</td>
<td>C*</td>
<td>289.4 ± 0.6(^{(a)})</td>
<td>290.1 ± 1.8(^{(b)})</td>
<td>295.8 ± 1.6</td>
</tr>
<tr>
<td>0281</td>
<td>C*</td>
<td>263.4 ± 0.2(^{(a)})</td>
<td>263.2 ± 1.0(^{(b)})</td>
<td>265.6 ± 0.4</td>
</tr>
<tr>
<td>0289</td>
<td>E</td>
<td>260.7 ± 0.3</td>
<td>261.6 ± 1.0(^{(b)})</td>
<td>262.7 ± 0.5(^{(b)})</td>
</tr>
<tr>
<td>0341</td>
<td>D</td>
<td>282.0 ± 0.3</td>
<td>282.3 ± 0.6</td>
<td>285.0 ± 0.3</td>
</tr>
<tr>
<td>0655</td>
<td>I*</td>
<td>284.4 ± 0.4</td>
<td>285.1 ± 0.7</td>
<td>286.8 ± 0.3</td>
</tr>
<tr>
<td>0744</td>
<td>C*</td>
<td>250.6 ± 0.4(^{(a)})</td>
<td>253.9 ± 1.1(^{(b)})</td>
<td>255.3 ± 0.9</td>
</tr>
<tr>
<td>0828</td>
<td>B*</td>
<td>249.3 ± 0.4</td>
<td>249.3 ± 1.1(^{(b)})</td>
<td>251.0 ± 0.7(^{(b)})</td>
</tr>
<tr>
<td>0839</td>
<td>A*</td>
<td>251.4 ± 0.3</td>
<td>250.2 ± 0.7</td>
<td>251.9 ± 0.4</td>
</tr>
<tr>
<td>0852</td>
<td>F</td>
<td>247.7 ± 0.4</td>
<td>248.8 ± 0.8</td>
<td>248.5 ± 0.5</td>
</tr>
<tr>
<td>0202</td>
<td>I*</td>
<td>287.5 ± 0.4</td>
<td>287.1 ± 0.8</td>
<td>289.2 ± 0.7</td>
</tr>
<tr>
<td>0282</td>
<td>H</td>
<td>276.3 ± 0.6</td>
<td>275.7 ± 1.2(^{(b)})</td>
<td>278.4 ± 0.5(^{(b)})</td>
</tr>
<tr>
<td>0290</td>
<td>I*</td>
<td>249.4 ± 0.4</td>
<td>250.6 ± 0.7</td>
<td>253.6 ± 0.4</td>
</tr>
</tbody>
</table>

Notes. Adopted line-of-sight velocities (\(v_{1D}\)) are a weighted average of the individual epochs in the LR02 and LR03 settings. \(^{(a)}\)Observations of Field C on 2009-10-08 were discarded as a result of low S/N. \(^{(b)}\)Estimates from only one epoch. Published RVs are indicated in the final column from Massey & Olsen (2003, MO03) and González-Fernández et al. (2015, GF15). \(^{(c)}\)Estimates corrected for instrumental variation.

Table 3. Mean RVs and dispersions of the Hodge 301 and SL 639 clusters compared to the local field population for RSGs (this study) and B-type stars in the VFTS (Evans et al. 2015).

<table>
<thead>
<tr>
<th>Region</th>
<th>(\alpha) (J2000)</th>
<th>(\delta)</th>
<th>B-type</th>
<th>RSGs</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No. of stars</td>
<td>RV ± (\sigma)</td>
<td>No. of stars</td>
<td>RV ± (\sigma)</td>
</tr>
<tr>
<td>All</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hodge 301</td>
<td>05 38 17.0</td>
<td>−69 04 01.0</td>
<td>298</td>
<td>270.4 ± 12.4</td>
</tr>
<tr>
<td>SL 639</td>
<td>05 39 39.4</td>
<td>−69 11 52.1</td>
<td>137</td>
<td>271.6 ± 11.8</td>
</tr>
</tbody>
</table>

Notes. Central coordinates as defined by Evans et al. (2015). For these estimates all candidate members of SL 639 were assumed as members.

should trace the same stellar population. The mean velocities for the RSGs (this study) and B-type stars (Evans et al. 2015) for the different associations in the 30 Dor region are given in Table 3. For consistency, we adopted the same definitions (central coordinates and radii) as those used by Sana et al. (2013) and Evans et al. (2015), and we included all the candidate members of the older clusters from Table 2. The agreement between the estimates for hot and cool stars in the different groups in Table 3 is very good (within 1\(\sigma\) in all cases), providing independent support of our adopted RV method for the cool stars. We note that in this study and in Table 2, we used unbiased estimates of the standard deviation that account for the small sample sizes. Figures 2 and 3 show the RVs for the individual B-type stars (from Evans et al. 2015) compared with our estimates for the RSGs in Hodge 301 and SL 639, respectively. Within the uncertainties the systemic velocities are in good agreement. Moreover, the dispersion of the RSGs appears smaller. We expect this is a consequence of the large number of spectral lines available in the RSG spectra (cf. the more limited number of helium and metallic lines in B-type spectra), combined with lower rotational broadening in the cool stars (which limits the RV precision in the more rapidly rotating B-type stars).

Five of our targets have published estimates in the literature, as indicated in the final column of Table 2. Four of these are from the study of González-Fernández et al. (2015), which quoted an uncertainty of ±4 km s\(^{-1}\) on their estimates. Within the respective uncertainties these are also in good agreement with our results.

We find no evidence of runaway RSGs, which have RVs offset by more than 30 km s\(^{-1}\) compared to the surrounding population (Blauw 1961; Eldridge et al. 2011; Boube & Evans 2018; Renzo et al. 2018). Based on the binary supernova scenario, Renzo et al. (2018) found that the number of runaway stars is dwarfed by an order of magnitude by the number of slower moving – nevertheless unbound – walkaway stars. Through dynamical simulations of young (<3 Myr) star clusters, Oh & Kroupa (2016) suggested that a significant fraction of their stellar population can be ejected through dynamical interactions, resulting in a similar velocity distribution for ejected stars.

This walkaway scenario is a possible explanation for the location of the RSGs near to Hodge 301 and SL 639. Particularly in the case of SL 639, as the stars appear to be genuine cluster members (see Sect. 4), it is unlikely that these stars formed in their current location.
3.1. Multi-epoch analysis

Initial tests showed a correlation between the velocities estimated for targets observed in the same fibre configuration. Table A.1 lists the complete set of RV estimates for our sample, and Fig. 4 shows the RV curves for each target. Our targets were observed within eight of the nine fibre configurations used for the VFTS, and some were observed in the same field (see Table 2 for details). From initial analysis of the RV estimates we noticed that targets observed in the same fibre configuration had very similar RVs. An example of this correlation is shown in Fig. 5 for VFTS 222 and 236, both observed in Field C, and also highlights the scale of the instrumental variation (of the order of ±2 km s\(^{-1}\)).

There is no plausible explanation of why the RVs of different RSGs should be coupled in such a way, and we conclude that this is linked to the wavelength calibration of the data. The measured variations correlate approximately with differences in the on-instrument temperature at the time of the arc calibrations (taken during the day) and the science observations; unfortunately no consistent relationship could be found when considering the recorded temperatures. Where possible we therefore attempted to calibrate the velocity scale empirically via groups of RV measurements within the different VFTS fields. In doing this, we acknowledge that these stars may also show physical variations at a level comparable to the (presumed) instrumental effect, hence we potentially remove some genuine RV variations for a given target.

To identify such instrumental variations, the RVs of each target (cf. their medians) are compared with those for other targets in the same fibre configuration\(^3\). We find significant variability (using Pearson’s correlation coefficient) for at least one pair of targets for each field. The correction applied to the results for each epoch is then the weighted average of the RVs for a pair of targets (or three for Field I) within that field. These corrections were then implemented to each target of the relevant field, resulting in corrected RVs for 13 stars. No correction was possible for the remainder (VFTS 289, 341, 852, and 2028) as only one star from our sample was observed per fibre configuration.

After correction, all of the targets are consistent with an absence of significant RV variation on scales above 5 km s\(^{-1}\), except for VFTS 744. This source displays a variation of 11.6 km s\(^{-1}\) between epochs, which is comparable to the variation found by Josselin & Plez (2007) for several of their targets; see Sect. 3.2 for more discussion of the variability of VFTS 744. The remaining targets that display differences on this scale between epochs all have a combination of larger than average uncertainties or uncorrected instrumental variation (e.g. VFTS 023, 852, and 2002, see Fig. 4). No apparent periodicities were detected in the spectroscopy (as found for \(\mu\) Cep by Josselin & Plez 2007), although robust checks would require more intensive spectroscopic monitoring.

It is important to discriminate, if possible, between atmospheric variations arising from large-scale convective cells that dominate the surface of RSGs (Chiavassa et al. 2009, 2010) and the effect of binary motions. Any RV variability from binarity would be somewhat hidden and perturbed by the rising/sinking motion of convective cells on the surface of the star, which causes intrinsic velocity variability in groups of lines formed in the same part of the atmosphere. This variation can be up to ~25 km s\(^{-1}\) (Josselin & Plez 2007); however the effect on the measured RV of the star effectively averages out and is significantly lower. We note that the slice technique used to estimate the RVs is, by its nature, particularly insensitive to variations dominated by particular spectral features (or groups of features).

The low-level RV variations observed in our sample are broadly consistent with what we expect from the atmospheres of single or very long-period RSGs dominated by several large-scale convective cells, as initially hypothesised by Schwarzschild (1975) and shown through radiative hydrodynamical simulations by Freytag et al. (2002). Large variations in the RVs of our sample would therefore be characteristic of significant binary motion (see Sect. 5). From the few known RSGs within binary systems, RV variations of order 40 km s\(^{-1}\) are seen over a full period (e.g. K1 = 20 km s\(^{-1}\); Wright 1977; Eaton & Shaw 2007). With orbital periods up to ~20 yr (Peery 1966; Wright 1977), this implies RV variations of up to 6 km s\(^{-1}\)/yr.

\(^3\) An attempt was made to use B-type stars observed in the same configuration to estimate this offset, however, the precision on the RV measurements for these stars is not sufficient to provide a conclusive result.

Fig. 2. Radial velocity (RV) estimates for members of Hodge 301. Results for the B-type stars from Evans et al. (2015) are shown by the blue circles and estimates for the RSGs in this study are shown by the black squares (for which the uncertainties are not visible on this scale). The average and standard deviation of the B-type stars are indicated by the blue line and shaded region, respectively. The systemic velocity estimated from the RSGs is in excellent agreement with that from the hotter stars (see also Table 3).

Fig. 3. As Fig. 2, for the four RSGs in SL 639 (shown with black stars).
Fig. 4. Absolute RV estimates from the multi-epoch observations of our sample as a function of Heliocentric Julian Date (HJD). Black points indicate the LR02 measurements and red stars show the LR03 measurements; there is an excellent agreement between the two settings (see Table 2 for details). Each panel has the same vertical scale to highlight the amplitude of the observed variations. The fibre configuration (Fields A-I) in which each target was observed is also indicated. Corrections for instrumental variation have been implemented for 13 of the targets (excl. VFTS 289, 341, 852, 2028; see text for details).

3.2. Photometric variability

Four of our sample stars (VFTS 023, 222, 655, 744) have been observed as part of the OGLE survey (Soszynski et al. 2009). The level of photometric variability for all these targets is in good agreement with the expected level of variation for this type of long period semi-regular variable star (Wood et al. 1983).

This type of variability is thought to arise from radial pulsations (e.g. Heger et al. 1997; Stothers 2010) and is known to exist in various Galactic RSGs at this level, on periods of several hundred days (Kiss et al. 2006), and longer term periodic variations (Kiss et al. 2006; Gray 2008).

For all of the four targets with OGLE data available, the Lomb-Scargle periodogram was searched for potential periodicities. There is only a suggestion of significant periods for VFTS 744, which supports the argument that VFTS 744 is an AGB star (see B19 and Sect. 5 for details).

4. Physical properties of the clusters

Given the good agreement of our RV estimates with previous values and the apparently small velocity dispersions in Hodge 301 and SL 639, we investigated the physical properties of the two clusters following the approach used for NGC 2100, a RSG cluster close to 30 Dor, by Patrick et al. (2016).

We estimated the mean cluster velocity and line-of-sight velocity dispersion using an implementation of the Markov chain Monte Carlo (MCMC; Goodman & Weare 2010) method, in which emcee (Foreman-Mackey et al. 2013) is used to sample from the posterior probability distribution. The likelihood function used follows that used by Patrick et al. (2016).
Using the line-of-sight velocity dispersion of the cluster, the virial theorem can be used to define the dynamical mass of the cluster $M_{\text{Dyn}}$ as

$$M_{\text{dyn}} = \frac{\eta r_{\text{eff}}^2}{G},$$  \hspace{1cm} (1)

where $\eta = 9.75$ for a bound cluster and $r_{\text{eff}}$ is the effective radius of the cluster.

To calculate the cluster properties we included all RSG candidates for each cluster and the non-variable B-type stars from Evans et al. (2015). All B-type stars flagged as variable were excluded as binary motion has the effect of artificially increasing the cluster velocity dispersion (Gieles et al. 2010).

Some justification must be given for the inclusion of all RSG candidate cluster members, particularly as some of these candidates are located up to $\sim 35$ pc from the cluster centre. We can see from Table 3 that the dispersion of the field population of both the RSGs and B-type stars is $\sim 13$ km s$^{-1}$ and the dispersion of the clusters is (from RSG results alone) an order of magnitude lower (see Table 4).

To assess the status of the outlying stars, we calculated the probability that their measured velocities are consistent with membership of the clusters (cf. membership of the local field population). The parent population was defined by a convolution of two Gaussian functions, where $P(x|\mu, \sigma)_{\text{cluster}} + P(x|\mu, \sigma)_{\text{field}} = 1$, and with the systemic velocities and dispersions of Hodge 301, SL 693, and the field taken from Evans et al. (2015). In all cases, we find a probability greater than $\sim 90\%$ that the targets are cluster members rather than part of the local field distribution. Therefore, despite their distance from the cluster centres, based on their kinematic properties we classify VFTS 236 as a member of Hodge 301, and VFTS 852 and 2090 as members of SL 639.

Given the small sample size of the RSGs in each cluster, while our estimates take into account the sample size, the velocity dispersions and mass estimates from solely RSGs may be better treated as upper limits. Combining the RSG results with those of the B-type stars allows us to provide more stringent constraints on these measurements.

### 4.1. Hodge 301

From the three RSGs and 14 B-type members, we estimated the mean cluster velocity of Hodge 301 as $262.1 \pm 1.4$ km s$^{-1}$ with a line-of-sight dispersion of $4.2^{+1.7}_{-1.2}$ km s$^{-1}$.

Cignoni et al. (2016) found that a 4 pc radius included 85% of the stars within the cluster. Assuming a Plummer density law (Plummer 1911), where we solve for the mass contained within a radius $M(r)$, we find that the radius containing 50% of the stars (i.e. the effective radius) is $r_{\text{eff}} = 1.68$ pc. This assumes that the half-light radius is equivalent to the half-mass radius, although this is not the case for mass-segregated clusters (see Gaburov & Gieles 2008; Feast et al. 2010).

Our estimated dynamical mass of Hodge 301, from the combination of RSGs and B-type stars, is $\log(M_{\text{dyn}}/M_\odot) = 3.8 \pm 0.3$. This is in excellent agreement with the photometric estimate of $\log(M_{\text{phot}}/M_\odot) = 3.9$ from Cignoni et al. (2016).

### 4.2. SL 639

Using the same methods for SL 639 (from the four RSGs and 11-B-type stars), we estimated a mean cluster velocity of $249.9 \pm 1.0$ km s$^{-1}$, where the line-of-sight dispersion is $\sim 1.9^{+1.8}_{-1.1}$ km s$^{-1}$. In absence of published structural parameters, we assume $r_{\text{eff}} = 1.68$ pc as per Hodge 301. From inspection of the available imaging SL 639 appears less extended than Hodge 301, so adopting this effective radius in Eq. (1) gives an upper limit on the dynamical mass of SL 639 of $\log(M_{\text{dyn}}/M_\odot) < 3.1 \pm 0.8$. This is the first mass estimate for this cluster.

### 4.3. Velocity dispersion of young massive clusters

As a result of the improved precision in the RSG RV measurements, we might expect that the estimates of the line-of-sight velocity dispersion from solely RSGs would provide more stringent constraints. However, the limiting factor in both cases studied in this work is the sample size, which is reflected in the larger uncertainties of the RSG estimates (see Table 4). The limiting factor in the case of the B-type sample is that of the precision of the RV measurements and potential undetected binarity. Therefore, even though the sample size is larger by a factor of three to five, the uncertainties are not significantly smaller than the solely RSG estimates.

The effects of contamination within our RSG sample from undetected binarity, pulsations, or including a non-cluster member, which is unlikely based on the assessment of the measured RVs compared against the distribution of velocities in the field stars, would all act to increase the measured velocity dispersion. Therefore we argue that despite the large uncertainties in the RSG measurements, the RSG sample is not heavily contaminated by the aforementioned effects.

The striking agreement of the average velocities among the members of each cluster is further evidence for an absence of RV variability for the RSGs, otherwise the velocity dispersions would be dominated by such variations (e.g. Gieles et al. 2010; Sana & Evans 2011; Hénault-Brunet et al. 2012). This is also confirmed by results from the LR20 spectra, where the maximum RV variation between any given epoch for all cluster members is $5.2$ km s$^{-1}$ (VFTS 289), which is probably linked to the instrument variations discussed in Sect. 3.

The results of the previous sections highlight that RSGs are effective tracers of the kinematic properties of young clusters, potentially offering advantages in RV precision over their main-sequence counterparts.

### 5. Binary analysis

There is growing evidence that most massive stars evolve within binary systems (e.g. Sana et al. 2012, 2013, 2014;
Duchêne & Kraus 2013; Kobulnicky et al. 2014; Dunstall et al. 2015; Moe & Di Stefano 2017). Simulations of how these stars evolve after the main sequence suggest that RSG lifetimes are significantly shortened as a result of Roche-lobe overflow and common-envelope evolution (Eldridge et al. 2008). In the literature there are only a handful of examples of binary systems containing RSGs, all of which have orbital periods greater than several hundred days to several decades. For example, VV Cep has an orbital period of about 20 yr and two almost equal mass companions (Wright 1977). QS Vul is the shortest period system known with \( P = 249 \text{ d} \) (Griffin et al. 1993), although its status as a RSG was questioned by Eaton & Shaw (2007) from estimates of its stellar parameters.

Before searching for RSG binaries in our dataset, we used Monte Carlo simulations to check the sensitivity of our observations to long-period binaries. To do so, we computed the detection probability of RSG binaries such as VV Cep (\( P = 20.3 \text{ yr} \), \( q = 1.0, \epsilon = 0.35 \)) should they have been observed with a template and hence a spectrophotometric binary candidate to each of the objects in our sample. We found that VV Cep-like binaries would have been detected in 10 to 60% of the cases – with an average of 33% – depending on the data set considered; i.e. we would expect to detect at least five binaries at the 3-sigma variability level if all our objects were VV Cep-analogous. This illustrates that our present observations are able to detect some binary systems if they were present among our RSG, and RSG-candidate, sample despite the limited baseline of the VFTS observations.

5.1. RV-variability detection

The multiplicity of the hot stars from the VFTS survey have been investigated in two papers. Sana et al. (2013) studied the multiplicity properties of the 360 O-type stars, finding an intrinsic binary fraction (after accounting for observational biases) of 51 ± 4%. In good agreement, Dunstall et al. (2015) performed a similar analysis of the early B-type stars and found an intrinsic binary fraction of 58 ± 11%, although they also noted that the fraction might be significantly lower in Hodge 501 and SL 639. The RV variability search criteria used by these two papers to detect binary were

\[
\frac{|v_i - v_j|}{\sqrt{\sigma_i^2 + \sigma_j^2}} > \sigma_{\text{lim}} \quad \text{and} \quad |v_i - v_j| > \Delta RV_{\text{min}},
\]

where \( v_i, \sigma_i (v_j, \sigma_j) \) are the measured RVs and corresponding uncertainty at epoch \( i (j) \), respectively, and \( \sigma_{\text{lim}} \) represents a limit set by the uncertainties on the RV measurements on significant variation. Both criteria need to be met by at least one pair of RV measurements for the object to be considered RV variable and hence a spectroscopic binary candidate. The choice of \( \Delta RV_{\text{min}} \) for these studies reflected the distribution of RV values estimated, 20 and 16 km s\(^{-1}\) for the O- and B-type stars, respectively. These limits were chosen to reject false positives arising from pulsational RV variations and the choice of \( \sigma_{\text{lim}} = 4.0 \) was selected to ensure no false positives given their sample sizes. For the current study, a \( \sigma_{\text{lim}} = 3.0 \) is selected, which reflects the smaller sample size and excludes the presence of any false positives at the 99.7% level.

The choice of \( \Delta RV_{\text{min}} \) is an important consideration for the present study. Figure 6 shows the observed binary fraction (i.e. the fraction of stars meeting both variability criteria) of the whole sample (black solid line) and probable RSGs (red dashed line) as a function of the \( \Delta RV_{\text{min}} \) parameter.

To evaluate the best choice of \( \Delta RV_{\text{min}} \), we investigated the typical velocities of known RSG binaries with the caveat that the known systems are likely a biased sample of the population of RSGs in binary systems. As mentioned above, literature examples of RSGs binaries (e.g. Wright 1977) typically contain B-type star companions (Neugent et al. 2018), where the peak-to-peak RV variations of the primary are \( \sim 40 \text{ km s}^{-1} \) (e.g. \( K \sim 20 \text{ km s}^{-1} \) for VV Cep and \( K \sim 27 \text{ km s}^{-1} \) for QS Vul; Peery 1966; Hack et al. 1992; Eaton & Shaw 2007), over a period of up to 20 yr (Wright 1977), or up to \( \sim 6 \text{ km s}^{-1} \) per year.

It is informative to consider the semi-amplitude velocity \( (K) \) of the RSG that is expected for a range of periods and mass ratios, taking into account the minimum periods excluded by the size of the star. In Appendix B we discuss the cases of an 8 and 15 \( M_\odot \) RSG and, adopting the latter as typical of our sample, we find that in the range \( q > 0.1, 3.25 < \log P [\text{day}] < 4.25, \) we expect \( 2 < K < 30 \text{ km s}^{-1} \). Clearly systems with \( K \sim 2 \text{ km s}^{-1} \) would go undetected for \( \Delta RV_{\text{min}} \) greater than this value (cf. Fig. 6), therefore we adopt a more conservative \( \Delta RV_{\text{min}} \) limit for our data of \( < 4.0 \text{ km s}^{-1} \).

Adopting \( \Delta RV_{\text{min}} < 4.0 \text{ km s}^{-1} \) results in the maximum observed binary fraction for our sample. In this case, the value of \( \sigma_{\text{lim}} \) for the first variability criterion is the limiting factor, and adopting \( \sigma_{\text{lim}} = 3 \) we obtain a binary fraction of 0.3. This estimate is effectively an upper limit on the observed binary fraction of our sample as our results may include false positives from intrinsic RV variations arising in the atmospheres of RSGs or RV shifts from uncorrected instrumental variations. It is interesting to note that not all of the targets meet the criteria even when the variability criteria reach the most relaxed values, despite the expectation that single RSGs can vary with amplitudes up to \( \sim 5 \text{ km s}^{-1} \) (Schwarzschild 1975; Freytag et al. 2002; Josselein & Plaz 2007; Stothers 2010). This reflects the fine precision of our RV measurements.

The subsamples used in Fig. 6 represent a luminosity cut in the sample, where the highest luminosity targets are defined as the most probable RSGs (red dashed line in Fig. 6). Table 2 highlights targets that are considered AGB candidates by B19.
Excluding these uncertain RSGs and adopting the same RV criteria as above, we still recover an upper limit to the binary fraction of 0.3.

5.2. Orbital configurations

To quantitatively assess the parameter space where our data is sensitive and the possible orbital properties of undetected binary systems, we investigated which orbital configurations (period, companion mass) would yield RV signals that are compatible with our observational constraints using Monte Carlo simulations tuned for each target. The parameter space considered in these simulations is orbital period of $2.7 < \log P_{\,[\text{days}]} < 5.0$, in steps of 0.1 (roughly corresponding to 1.5 to 275 yr) and secondary masses are in the range $0.3 < \log M_2 < 1.5$, in steps of 0.1 (roughly corresponding to 0.5 to 35 $M_\odot$). For the targets are taken from B19 and a flat eccentricity distribution is assumed in the range 0–0.95. Using circular orbits increases the detection probability at shorter period, but decreases it at period larger than about $10^5$ days. The impact is however limited to a few per cent such that the overall picture is left unaffected.

To optimize our sensitivity in these simulations we included all RV measurements, including those from the HR15N setting (accounting for the offset of 2.1 km s$^{-1}$, see Sect. 3).

For the targets that display RV variability, these simulations allow us to identify orbital configurations that would fulfill the adopted variability criteria. Targets that do not meet the variability criteria allow us to place limits on companions and period ranges that should have been detected, and thus assess the properties of systems that would remain undetected given the current data.

Figure 7 illustrates the results of the simulations for VFTS 236, which is one of the targets that does not meet the least demanding variability criteria ($\sigma_{\text{vmn}} = 3.0$, $\Delta \text{RV}_{\text{min}} = 0.0$ km s$^{-1}$). For each grid point, 10 000 simulations of the RV variability from the resulting binary systems are evaluated using the variability criteria ($\sigma_{\text{vmn}} = 3.0$, $\Delta \text{RV}_{\text{min}} = 0.0$ km s$^{-1}$). This figure is colour coded according to the number of variability detections for the 10 000 simulations for each grid point, in addition the contours denote the 1, 5, 10, 50, 90, 95, and 99 detection percentiles.

The results of these simulations show that the strongest constraints can be placed on targets in field C as a result of the longer baseline. For targets that do not meet the variability criteria (i.e. apparently single stars), we can typically exclude binary systems within the ranges $q > 0.3$, $\log P_{\,[\text{days}]} < 3.5$, as these should have been detected in 90% of cases (see Fig. 7). The period limit derived is slightly more stringent than the limit of $\log P_{\,[\text{days}]} \approx 3.3$ (for all mass ratios), which results from the size of the RSG (see Appendix B).

5.3. Binary fraction

Of the targets that meet the variability criteria ($\sigma_{\text{vmn}} = 3.0$ km s$^{-1}$, $\Delta \text{RV}_{\text{min}} = 0.0$ km s$^{-1}$), the variability in VFTS 289, 341, 852, and 2028 can likely be explained through uncorrected instrumental variation. In fact, these are the only systems that have no correction for instrumental variations. The only target that meets the criteria for which the variation cannot be explained through the lack of instrumental correction is VFTS 744. Our simulations yield 90% confidence intervals of the probable orbital parameters of $q > 0.1$ and $3.1 < \log P_{\,[\text{days}]} < 4.3$.

If we consider only probable RSGs that have a correction for the instrumental variation, we find a binary fraction of 0.0 using the variability criteria $\sigma_{\text{vmn}} = 3.0$ km s$^{-1}$, $\Delta \text{RV}_{\text{min}} = 0.0$ km s$^{-1}$, for binary systems with parameters $q > 0.3$, $3.2 < \log P_{\,[\text{days}]} < 3.5$, at the 90% confidence level. The process of correcting for instrumental variation (described in Sect. 3) clearly introduces biases and potential correlations into our analysis. These effects act to decrease the number of binary system detections by correcting real velocity variation. However, this does not affect the conclusion that VFTS 744 is the only target in the sample that displays significant variability that cannot be accounted for. Field C has the largest number of targets and the strongest correlation between the stars used to correct for the instrumental bias. If we restrict our binary fraction to these data, we find a binary fraction of 0.2, (with the sensitivity as quoted above), which agrees with our estimated upper limit.

As we quantitatively assessed the parameter space where our observations are able to detect binarity, we now estimate the intrinsic binary fraction by comparing our observed data to the empirically defined binary stellar population of Moe & Di Stefano (2017). Namely a flat orbital period distribution between $3.3 < \log P_{\,[\text{days}]} < 4.3$, where 50% of companions have $q > 0.3$ and the remaining in the range $0.1 < q < 0.3$. The mass ratio exponent is defined based on $q > 1.7$ for $q > 0.3$ and $-0.2$ for $0.1 < q < 0.3$. Eccentricity is defined with an exponent of $+0.8$ within the range $0 < e < 0.8$. With these distributions, we simulate the observed data with a binary fractions ($bf$) in the range $0.0 < bf < 1.0$ in steps of 0.1.

We limit ourselves to the RSG sample and compare the simulations with the results of Fig. 6. Although the dispersion is large, we find that an intrinsic binary fraction of 0.3 in the period range $3.3 < \log P_{\,[\text{days}]} < 4.3$ best reproduces the sharp drops in the
variability rate at ΔRVmin ≈ 7.0 km s−1. This value is in agreement with the detection of long period binary system in O-type stars (Sana et al. 2014) and the derived binary fraction of 30% per order of magnitude for such long period systems as derived by Moe & Di Stefano (2017). This statistic is chosen to compare the observations with the models as below this value; the observed velocities are likely affected significantly by intrinsic variability and measurement errors.

In addition to the RV variation of individual RSGs, the dispersion of RSG RVs within the cluster environments can in principle be used as a tracer of binarity (e.g. Sana et al. 2017). Simulations of the distribution of binary systems that could reproduce the observed data within the cluster proved to have little constraining power on the underlying stellar population, likely as a result of small number statistics (in both the number of targets and epochs). More constraining power is potentially available if we consider the relative velocities of these targets as a whole. This is beyond the scope of the current sample, but is partly addressed by a study of NGC 330 in the SMC (Patrick et al., in prep.).

The lack of any significant RV variables in the current study lends support to the hypothesis that mass transfer from a RSG to a companion results in the rapid evolution of the RSG to other stellar types (Eldridge et al. 2008), such as Wolf–Rayet and helium stars (Wellstein et al. 2001; Göttberg et al. 2018). In addition to this channel, another plausible alternative evolutionary pathway for a RSG is the merger of two main-sequence stars. This scenario results in a rejuvenated main-sequence star that evolves towards the RSG evolutionary stage as a red straggler star (see B19). From a RV variation point of view, these targets would be likely indistinguishable from a star that has evolved as a single star.

6. Conclusions

Estimated RVs are provided for a sample of 17 RSGs (including four lower luminosity AGB candidates) observed by the VFTS project. The targets are distributed across the 30 Doradus region of the LMC and include several stars in the Hodge 301 and SL 639 clusters. Radial velocities are presented for each target from observations with three FLAMES–Giraffe settings. We estimated the RVs using a slicing technique, which is shown to provide accurate and precise results when compared with results for hot stars from the VFTS, as well as previous literature measurements for a subset of our targets. With the multi-epoch data we identified and corrected for correlations in the measured RVs on the scale of ±2 km s−1 for stars in all multi-object field configurations observed. This correction was not possible for four of the target stars.

We provide estimates of the systemic velocities and dispersions of the Hodge 301 and SL 639 clusters, which are in excellent agreement with results from B-type stars (Evans et al. 2015). By combining the RSG velocities with those for the B-type stars we used the virial theorem to estimate the dynamical masses of the two clusters. For H 301 we estimated log(Mdyn/M⊙) = 3.8 ± 0.3, in excellent agreement with estimated mass from photometry (Cignoni et al. 2016). We also obtained an upper limit on the dynamical mass of SL 639 of log(Mdyn/M⊙) < 3.1 ± 0.8; this is the first mass estimate for SL 639.

The effectiveness of RSGs as kinematic tracers is discussed and we demonstrate that RSGs are robust tracers of the mean velocity and line-of-sight velocity dispersion of clusters given their lack of RV variability and apparent lack of binarity. In the specific cases of H 301 and SL 639, the limiting factor on the measurements presented in this work, for solely RSGs, is the sample size.

By considering the multi-epoch data, we estimated an upper limit on the observed binary fraction of our sample. To do this, we first calculated the semi-amplitude velocities for RSG binary systems across a wide range of parameter space and found that the expected values are typically in the range 2 < K < 30 km s−1 for a 15 M⊙ RSG. Using these calculations to guide our choice for the variability criteria used to detect binary candidates, we place an upper limit on the observed binary fraction of 0.3. By simulating binary systems that can reproduce the observed data, we conclude that the binary fraction estimate is sensitive to systems within the parameter space q > 0.3, log P [days] < 3.5, i.e. only among the shortest period systems allowed given the size of the RSG primary.

Using the empirically defined distribution of binary systems from Moe & Di Stefano (2017), we investigate the intrinsic binary fraction by simulating our observed data using a range of intrinsic binary fractions. We find that our observations can be best reproduced by an intrinsic binary fraction of 0.3, accounting for observational biases, considering orbital periods log P [days] < 4.3. To improve upon the binary statistics presented in this work, a more comprehensive multi-epoch RV study (and preferably at greater spectral resolution) is required.
Eldridge, J. J., Fraser, M., Smartt, S. J., Maund, J. R., & Crockett, R. M. 2013, 
MNRAS, 436, 774
Hodge, P. 1988, PASP, 100, 1051
Levesque, E. M. 2017, Astrophysics of Red Supergiants (Bristol, UK: IOP Publishing)
Shapley, H., & Lindsay, E. M. 1963, AJ, 6, 74
Wright, K. O. 1977, JRASC, 71, 152
Appendix A: Multi-epoch radial velocities

Table A.1. Radial velocity (RV) estimates at each epoch for candidate RSGs observed in the VFTS.

<table>
<thead>
<tr>
<th>VFTS ID</th>
<th>HJD – 2 400 000</th>
<th>RV (km s(^{-1}))</th>
<th>(\sigma_{RV}) (km s(^{-1}))</th>
<th>Setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>023</td>
<td>54767.824</td>
<td>271.30</td>
<td>0.61</td>
<td>LR02</td>
</tr>
<tr>
<td>023</td>
<td>54819.809</td>
<td>270.68</td>
<td>0.36</td>
<td>HR15N</td>
</tr>
<tr>
<td>023</td>
<td>54827.772</td>
<td>271.88</td>
<td>1.41</td>
<td>LR02</td>
</tr>
<tr>
<td>023</td>
<td>54828.725</td>
<td>273.49</td>
<td>0.84</td>
<td>LR02</td>
</tr>
<tr>
<td>023</td>
<td>54828.821</td>
<td>271.32</td>
<td>0.91</td>
<td>LR03</td>
</tr>
<tr>
<td>023</td>
<td>54836.563</td>
<td>269.57</td>
<td>1.32</td>
<td>LR03</td>
</tr>
<tr>
<td>023</td>
<td>54860.643</td>
<td>268.65</td>
<td>0.78</td>
<td>LR02</td>
</tr>
<tr>
<td>023</td>
<td>54886.616</td>
<td>268.59</td>
<td>0.97</td>
<td>LR02</td>
</tr>
<tr>
<td>023</td>
<td>55114.859</td>
<td>265.72</td>
<td>3.30</td>
<td>LR02</td>
</tr>
<tr>
<td>081</td>
<td>54804.637</td>
<td>286.16</td>
<td>0.62</td>
<td>LR02</td>
</tr>
<tr>
<td>081</td>
<td>54804.760</td>
<td>287.06</td>
<td>0.27</td>
<td>HR15N</td>
</tr>
<tr>
<td>081</td>
<td>54808.676</td>
<td>285.06</td>
<td>0.90</td>
<td>LR03</td>
</tr>
<tr>
<td>081</td>
<td>54836.752</td>
<td>284.92</td>
<td>0.60</td>
<td>LR02</td>
</tr>
<tr>
<td>081</td>
<td>54867.598</td>
<td>283.11</td>
<td>0.57</td>
<td>LR02</td>
</tr>
<tr>
<td>081</td>
<td>55108.808</td>
<td>284.56</td>
<td>0.65</td>
<td>LR02</td>
</tr>
</tbody>
</table>

Notes. Observations with the same spectrograph setting for each target that were less than a day apart were co-added to improve S/N (for which the quoted epochs are the average of the co-added observations). Full version of this table is available at the CDS. The first 15 lines are shown as a sample.

Table A.1 provides the complete list of estimated RVs for the candidate RSGs considered in this paper. Results for targets in Fields A, B, C, and I are corrected for the apparent instrumental variations using at least two targets in their respective fields (see Sect. 3 for details).

Appendix B: Semi-amplitude radial velocities for RSGs

To investigate the expected range of semi-amplitude velocities (\(K\)) given the mass and physical extent of a RSG primary, we use the following equations:

\[
K = \frac{2\pi a_1}{P}, \tag{B.1}
\]

where \(P\) is the orbital period of the system and \(a_1\) as

\[
a_1 = \left(\frac{Gm_1m_2}{4\pi^2(1 + q)^2}\right)^{1/3}, \tag{B.2}
\]

where \(q = m_1/m_2\) and \(m_1, m_2\) are the mass of the primary and secondary components of the system, respectively.

Figures B.1 and B.2 illustrate the cases for 8 and 15 \(M_\odot\) RSGs, where the solid coloured lines illustrate constant \(K\) values and the black dashed lines represent the minimum period possible, given the maximum radii of RSGs, for different mass ratios. In the range \(q > 0.1, 4.5 < P \text{ [year]} < 50\), we expect \(2 < K < 30 \text{ km s}^{-1}\) for a 15 \(M_\odot\) RSG. Orbital eccentricity and inclination are not taken into account in these calculations, but would both act to decrease the observed semi-amplitude velocity.