ORTHOGONALITY-REGULARIZED MASKED NMF FOR LEARNING ON WEAKLY LABELED AUDIO DATA

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ABSTRACT
Non-negative Matrix Factorization (NMF) is a well-established tool for audio analysis. However, it is not well suited for learning on weakly labeled data, i.e. data where the exact timestamp of the sound of interest is not known. In this paper we propose a novel extension to NMF, that allows it to extract meaningful representations from weakly labeled audio data. Recently, a constraint on the activation matrix was proposed to adapt for learning on weak labels. To further improve the method we propose to add an orthogonality regularizer of the dictionary in the cost function of NMF. In that way we obtain appropriate dictionaries for the sounds of interest and background sounds from weakly labeled data. We demonstrate that the proposed Orthogonality-Regularized Masked NMF (ORM-NMF) can be used for Audio Event Detection of rare events and evaluate the method on the development data from Task2 of DCASE2017 Challenge.

Index Terms— Non-negative Matrix Factorization, weakly labeled data, Acoustic Event Detection

1. INTRODUCTION
Non-negative Matrix Factorization (NMF) is a popular tool for discovering structure in a variety of signals. For many years it has been widely used for analysis of musical audio and more recently, of environmental sounds. Analysis of environmental sounds have recently received a lot of attention in the research community due to its vast number of applications, ranging from audio content analysis, human activity monitoring, to surveillance and bioacoustic monitoring. Among others, methods based on NMF have been successfully applied to several tasks of environmental audio analysis such as audio scene classification [1], rare event detection [2] or real life audio event detection [3]. NMF methods offer parsimonious models with significantly fewer parameters than, for instance, Deep Neural Networks (DNNs). Hence further investigating NMF is an interesting direction in the environmental sound research.

NMF models the spectrogram $V$ of a sound signal as a product of a dictionary of spectral bases $W$ and a corresponding activation matrix $H$. The key strategy for NMF to efficiently model the sounds of interest is to express them and the background sounds by different sets of bases. It is easily achieved when we have access to isolated recordings of sound of interest [2] or well annotated data, where the timestamps of the sounds of interest are known [3]. In that case, we can extract the set of bases for the sound of interest using the isolated/annotated recordings and another set of bases for the background sounds using the recordings of the noise. However, in the real world scenario it is often easier to gather weakly labeled data, that is, data in which we do not have exact information of when the interesting sound occurs, but just a tag of which sounds are present in a given audio excerpt. It implies that we do not have access to the clean recordings of the sound of interest: the training data contain parts with background/noise only and parts with background and the target sound. Therefore, the task of expressing the sound of interest and the background with different bases becomes difficult. In [4], inspired by the score informed source separation approaches [5], we proposed a Masked NMF method, which adapts NMF to the problem of learning meaningful bird sound representations from such noisy, weakly labeled data. Using the weak labels, we constrained parts of the activation matrix to zero, hence obtaining more robust set of bases for sounds of interest and noise.

Masked NMF proved successful for Bird Audio Detection [4], but we observed that often the background sounds were reconstructed using the dictionary of bird sounds. That suggests that constraining the activation matrix is not enough to produce separate set of bases for the sound of interest and the background sounds. Therefore, the difference between the set of bases of the target sound and noise has to be increased by “pushing” the subspaces of the bases apart from each other. In this work, we propose to achieve this by introducing an orthogonality regularization term in the objective function of NMF. Regularization of NMF has been proven...
useful in a number of application. For instance, a temporal constraint improves audio source separation [6], sparsity has been shown to improve NMF performance on real life audio event detection [7] and co-occurrence constraint was used for automatic music transcription [8]. In this paper, inspired by the idea of forcing two dictionaries to be different originally introduced for single channel source separation problem [9], we propose to add an orthogonality regularizer, that decorrelates the two dictionaries and promotes orthogonality between dictionaries of the sound and of the background, resulting in the Orthogonality-Regularized Masked NMF (ORM-NMF) method.

The paper is organized as follows. Sections 2 and 3 introduce the standard NMF and Masked NMF respectively. Then, in Section 4 we describe the proposed method and the derived multiplicative update rules. Later we test the method on a rare event detection task using weakly labeled data described in Section 5. The results are presented in Section 6 followed by the conclusions in Section 7.

2. NON-NEGATIVE MATRIX FACTORIZATION

The goal of NMF is to approximate a non-negative data matrix, typically a time-frequency representation of a given sound, \( V \in \mathbb{R}_+^{F \times T} \) as a product of a dictionary \( W \in \mathbb{R}_+^{F \times K} \) and its activation matrix \( H \in \mathbb{R}_+^{K \times T} \), such that:

\[
V \approx \hat{V} = WH.\tag{1}
\]

\( W \) and \( H \) are estimated to minimize some divergence metric \( D(V|WH) \). For any two matrices \( X \) and \( Y \), we define \( D(X|Y) = \sum_{m,n} D(x_{mn},y_{mn}) \). In this work we choose the squared Euclidean distance as the divergence metric, defined as

\[
D(V|WH) = \| V - WH \|^2 \tag{2}
\]

although other error approximation functions, such as generalized Kullback-Leibler (KL) divergence or Itakura-Saito (IS) divergence [10] are also sensible choices and the proposed method can be easily extended to use those. Euclidean distance can be minimized by alternately updating \( W \) and \( H \) by the following multiplicative update rules [11]:

\[
W \leftarrow W \odot \frac{VH^\top}{WHH^\top}, \quad H \leftarrow H \odot \frac{WV^\top}{VWH^\top},\tag{3}
\]

where \( A \odot B \) denotes a Hadamard (element-wise) product of two matrices, \( \frac{A}{B} \) denotes Hadamard division and other multiplications are matrix multiplications.

3. MASKED NMF

In [4] we proposed to extend a standard NMF approach to learning on weakly labeled data. To explain the idea, let us consider the task of detection of rare sound events, as proposed in the Detection and Classification of Acoustic Scenes and Events challenge DCASE2017 [12]. Let \( y \in \{0, 1\} \) be a weak label denoting absence or presence of the target sound, \( V^0 = V_1^0, \ldots , V_{M_0}^0 \) is a set of \( M_0 \) training examples with absence of the target sound and \( V^1 = V_1^1, \ldots , V_{M_1}^1 \) is a set of \( M_1 \) training examples with the presence of the target sound. As the data is weakly labeled, examples containing the target sound most probably also contain noise and other sounds. Therefore, we assume that to reconstruct well the target sound training examples (\( V^1 \)) we also need elements from dictionaries extracted from background sounds examples (\( V^0 \)). At the same time, we do not expect elements of the dictionary atoms of target sounds to be used for reconstructing \( V^0 \). We impose this constraint in the training phase by applying a binary mask to the activation matrix as follows:

\[
V = [V_0, V_1] \approx [W_0, W_1] \left( \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \odot \begin{bmatrix} H_{00} & H_{01} \\ H_{10} & H_{11} \end{bmatrix} \right) = [W_0H_{00}, W_0H_{01} + W_1H_{11}] \tag{4}
\]

where \( W_0 \in \mathbb{R}_+^{F \times K_0} \), \( W_1 \in \mathbb{R}_+^{F \times K_1} \) are “sound” and “background” dictionaries respectively, \( K_0 \) and \( K_1 \) are their corresponding ranks. \( 0 \) is a matrix of zeros with \( K_1 \) rows and the number of columns corresponding to the total size of \( M_1 \) background training data, while \( 1 \) denotes matrices of appropriate dimensions with all elements equal to 1. \( H_{00}, H_{10}, H_{11} \) and \( H_{11} \) are parts of the activation matrix of suitable dimensions. Hence, we are seeking to minimize the Euclidean distance:

\[
\min_{w_0, w_1, H_{\geq 0}} \| V - WH \|^2 = \| V_0 - W_0H_{00} \|^2 + \| V_1 - W_0H_{01} - W_1H_{11} \|^2 \tag{5}
\]

The masking is implemented through appropriate initialization of the activation matrix. As the update rules of NMF are multiplicative, elements initialized with 0 remain 0 throughout the training. Hence, applying the multiplicative rules from eq. 3 we obtain the dictionary:

\[
W = [W_0, W_1], \tag{6}
\]

that was later used for audio classification.

4. PROPOSED METHOD

Masked NMF, although suitable for audio classification task, has some limitations. In previous experiments we have observed that, in spite of the constraint on the activation matrix, the background sounds were often reconstructed using the dictionary of target sounds. It might suggest that the dictionaries are correlated and hence, not discriminative between
the target and background sounds. To overcome this problem we propose to add an additional orthogonality regularizer, which decorrelates the dictionaries by “pushing” them apart from each other. To achieve this, we measure the correlation between the dictionaries \( W_0 \) and \( W_1 \) using the dot product between them, i.e. \( \|W_0^T W_0\|_2^2 \), and aim to minimize it. The emphasis, that is given to the orthogonality regularizer can be adjusted by choosing an arbitrary value of \( \lambda \). Combining the constraint on the activation matrix and the orthogonality regularizer results in the following cost function to minimize:

\[
\min_{w_0, w_1, H} \|V - WH\|^2 + \lambda \|W_1^T W_0\|^2
\]

\[
= \|V_0 - W_0 H_{00}\|^2 + \|V_1 - W_0 H_{01} - W_1 H_{11}\|^2 + \lambda \|W_1^T W_0\|^2
\]

(7)

As \( \|W_1^T W_0\|^2 \) is convex in \( W_0 \) and \( W_1 \), we can minimize the cost function using the gradient decent. Then, following the derivations of Lee and Sung [11], we obtain the corresponding multiplicative update rules for \( W_0 \) and \( W_1 \):

\[
W_0 \leftarrow W_0 \odot \frac{V_1 H_{01}^T + V_0 H_{00}^T}{W_0 H_{01} H_{01}^T + W_1 H_{11} H_{11}^T + \lambda W_1 W_1^T W_0}
\]

\[
W_1 \leftarrow W_1 \odot \frac{V_1 H_{11}^T}{W_0 H_{01} H_{11}^T + W_1 H_{11} H_{11}^T + \lambda W_0 W_0^T W_1}
\]

(8)

As the regularizer does not influence the activation matrix \( H \), the update rule for \( H \) remains the same as in the original NMF problem formulation shown in Section 2:

\[
H \leftarrow H \odot \frac{W^T V}{W^T WH}
\]

(9)

5. EXPERIMENTAL SETUP

The proposed method is evaluated on the task of Detection of rare sound events using only weakly labeled data from the audio recordings of the TUT Rare Sound Events 2017. The dataset was provided for Task 2 of the DCASE2017 challenge [12]. All audio files are resampled to sampling rate of 16000 Hz in order to reduce the dimensionality of the data. We extract perceptually motivated mel-spectrograms with 40 components, using a window size of 64 ms, hop size of the same duration. Mel-spectrograms are a common choice for representation of environmental audio [13, 1]. In order to model temporal dynamics of environmental sounds we choose a spectro-temporal representation of the data, which is achieved by grouping several consecutive frames into 2D patches, also known as shingling. In our experiments, we set the number of consecutive frames to 4, the value that was chosen empirically.

5.1. Dataset

The dataset consists of around 100 isolated sound examples for three target classes: gunshot, baby crying and glass break-

<table>
<thead>
<tr>
<th>Event type</th>
<th>training</th>
<th>testing</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gunshot</td>
<td>134</td>
<td>53</td>
</tr>
<tr>
<td>Glass breaking</td>
<td>96</td>
<td>43</td>
</tr>
<tr>
<td>Baby crying</td>
<td>106</td>
<td>42</td>
</tr>
</tbody>
</table>

Table 1. Experimental dataset. Number of sound recordings per class used for training and testing.

5.2. Event detection

We use the proposed method and the Masked NMF to extract dictionaries \( W_0 \) and \( W_1 \). In the event detection phase, a test sample is decomposed using the trained dictionaries as follows:

\[
V_{test} = [W_0, W_1] H_0 \begin{bmatrix} \lambda \end{bmatrix}
\]

(10)

Finally, \( H_1 \) is binarized using a threshold equal to 50% of the maximum value of the entire activation matrix \( (H_0 \) and \( H_1 \)). The columns of the binarized \( H_1 \) that are greater than 0 indicate the presence of the event.

5.3. Evaluation metrics

To evaluate the method we use metrics used in the DCASE2017 challenge, i.e. event-based error rate (ER) and event-based F-score. An event is considered correctly detected using onset-only condition with a collar of 500 ms. The ER is
calculated by adding the number of substitutions, insertions and deletions for each class before dividing it by the total number of events. The F-score is computed as the harmonic mean between precision and recall based on the total amount of false negatives, true positives and false positives per class. We refer the reader to [15] for more details and explanations about these metrics.

6. RESULTS

The parameters of the system, namely $K_0$, $K_1$ and $\lambda$ were chosen empirically during the development of the method and set constant throughout the experiments to allow for a meaningful comparison. The parameters were chosen to be: $K_0 = 50, K_1 = 10$ and $\lambda = 1000$.

6.1. Vanilla scenario

We compare the proposed method with the Masked NMF approach. We can see that for 4 seconds chunks of audio with 0 dB SNR

### Table 2. Evaluation results in Vanilla Scenario. Error Rate (ER) and F-score (F1) are reported for the proposed method and Masked NMF.

<table>
<thead>
<tr>
<th>Event type</th>
<th>Proposed</th>
<th>Masked NMF</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ER</td>
<td>F1</td>
</tr>
<tr>
<td>Gunshot</td>
<td>0.26</td>
<td>87.5%</td>
</tr>
<tr>
<td>Glass breaking</td>
<td>0.21</td>
<td>89.4%</td>
</tr>
<tr>
<td>Baby crying</td>
<td>0.85</td>
<td>51.3%</td>
</tr>
</tbody>
</table>

6.2. Challenge Scenario

To show that the method has a potential to be used in more complicated scenarios, we evaluate the trained models on the official development data of the DCASE2017 Challenge. Table 3 shows the results for the proposed method, Masked NMF and the DCASE2017 baseline.

### Table 3. Evaluation results in Challenge scenario. Error Rate (ER) and F-score (F1) are reported for the proposed method, Masked NMF and DCASE2017 baseline.

<table>
<thead>
<tr>
<th>Event type</th>
<th>Proposed</th>
<th>Masked NMF</th>
<th>DCASE</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ER</td>
<td>F1</td>
<td>ER</td>
</tr>
<tr>
<td>Gunshot</td>
<td>0.79</td>
<td>64.7%</td>
<td>0.81</td>
</tr>
<tr>
<td>Glass breaking</td>
<td>0.87</td>
<td>50.1%</td>
<td>0.94</td>
</tr>
<tr>
<td>Baby crying</td>
<td>0.97</td>
<td>39.1%</td>
<td>1.07</td>
</tr>
</tbody>
</table>

6.3. Discussion

The results in Table 2 show that the proposed method is a promising way to learn on weakly labeled data. It is interesting to see that the performance on gunshot and glass breaking sounds is much higher than on baby crying sounds. This may show that the proposed method is more suitable for detection of impact than harmonic sounds. Moreover, separate parameter tuning for each class could be beneficial. Further analysis is needed to investigate the reasons for such a big difference.

The results in Table 3 confirm our findings using the Vanilla scenario. The method performs well on the gunshot detection, reasonably well on glass breaking detection and much worse on baby crying detection. It has to be reiterated, that the baseline for DCASE 2017 was using strongly annotated data, hence we expected our method to perform worse, as we allowed ourselves to use weakly labelled data only.

From both scenarios we can see that regularization lowers the Error Rate, but F-score is not always increased. The reasons for this behaviour need more investigation. However, it can be concluded by analysing the results of the DCASE 2017 Challenge, that not always methods that achieve the lower ER achieve higher F-score.

7. CONCLUSIONS

We proposed a novel method based on NMF for learning sound representations on weakly labeled data. Adding a constraint on the activation matrix and an orthogonality regularizer to the standard NMF formulation we are able to learn sound representations without isolated or strongly annotated training data. Using the task of detection of rare events as an example, we showed that the method is a promising direction for Audio Event Detection when no isolated or annotated sounds are present. However, the performance of the method strongly depends on the type of target sound.

In future we plan to compare our method with other algorithms tailored especially for weakly labeled data. Moreover, we would like to understand better the influence of the parameters of the system and the reasons for a big discrepancy of the results between different classes. Finally, we want to compare iterative methods for decorrelating the dictionaries with the proposed approach.

8. REFERENCES


[2] Q. Zhou and Z. Feng, “Robust sound event detection through noise estimation and source separation using


