Wideband Impedance-varying N-way Wilkinson Power Divider/Combiner for RF Power Amplifiers

Osama Hussein\textsuperscript{1}, Khair Al shamaileh\textsuperscript{2}, Vijay Devabhaktuni\textsuperscript{1}, and Peter Aaen\textsuperscript{3}

\textsuperscript{1}University of Toledo, OH, US, \textsuperscript{2}Purdue University Northwest, IN, US, \textsuperscript{3}University of Surrey, Guildford, UK

Abstract — We propose a compact wideband multi-way power divider/combiner with planar structure for applications to RF power amplifiers (PAs). Uniform transmission lines in the conventional divider are replaced with non-uniform transmission lines (NTLS), which are governed by a truncated Fourier series. An optimization-driven framework is employed in even-mode analysis to obtain the coefficients of the NTLS considering predefined operating bands, whereas three isolation resistors are optimized in the odd-mode analysis to achieve optimal isolation and output port matching over the design bandwidth. For verification purposes, a 4–10 GHz 3-way divider is simulated, and measured. Simulations and measurements are in close proximity and show input/output ports matching of better than \(-10\) dB and transmission of \(-4.9\pm 1\) dB across the design bandwidth.

Index Terms — multi-way power divider, non-uniform transmission lines (NTLS), power amplifiers (PAs), power combiner, wideband Wilkinson power divider (WPD).

I. INTRODUCTION

Power dividers/combiners are widely used fundamental front-end components in a variety of microwave/millimeter wave systems, power amplifiers (PAs), mixers, and antenna feeding networks. PAs have applications that span wireless and radio communications equipment, phased array radar modules, unmanned aerial vehicles (UAVs), and electromagnetic compatibility (EMC) testing [1]-[5]. PAs can also be used in communication systems measurements such as tests of intermodulation, adjacent channel power, multi-tone, and high signal levels. However, PAs have limitations, especially for applications where a high RF amplification gain is required. To overcome this, a power combiner can be used to combine the individual powers from multiple lower power PAs. Such a network has the advantages of: 1) graceful degradation reliability characterized by the accommodation of the failure of a single PA without a total loss of the transceiver/transponder power [6], 2) it is less expensive and complex to manufacture moderate-power PAs than high-power PAs, and 3) lower power PAs can be biased to operate in the linear region, resulting in the reduction of the intermodulation distortion and undesired harmonics.

Many power dividers/combiners for large operating bandwidths, high efficiency, high isolation, and small size have been proposed in literature. The Wilkinson power divider (WPD) or combiner, proposed by E. Wilkinson in 1960 [7], is widely used in front-end microwave subsystems due to its ease of design and fabrication, high isolation between its ports, as well as perfect matching at all ports. Port isolation is widely regarded as an asset in RF power combining, as it can be used to suppress odd mode instability between the combined amplifiers [8]. This alone often explains the preference of Wilkinson type combiners over other dividers/combiners in microwave PA networks. Accordingly, broadening the operating bandwidth while maintaining the same desired electrical features are of utmost importance. A variety of designs have been proposed [9]-[13], however, the major drawbacks are the increased physical size, the use of reactive components, and the bulky 3D geometries.

In this paper, a general procedure to design and characterize a NTLS wideband multi-way planar Wilkinson power divider/combiner is presented. The proposed device is modeled and simulated for equal-split division. Then, the input and output ports can be reversed to enable power combining rather than division. Thereafter, the phases of the transmission parameters are measured to verify in-phase functionality.

The article is organized as follows: Section II discusses the design procedure of the proposed wideband NTL multi-way WPD. Simulations and measurements of a wideband 3-way prototype is presented in Section III. Finally, conclusions are given in Section IV.

II. MULTI-WAY WPD DESIGN

A schematic diagram of the proposed wideband equal-split NTL divider is shown in Fig. 1. The \(N\)-way divider can be reduced to its equivalent 2-way model [14]. Hence, the even-odd mode analysis will be adopted.

To reduce the \(N\)-way divider to its equivalent 2-way model illustrated in Fig. 2, the first branch is assumed to be the \(n\)-th branch with 
\(1/N\) fraction of total input power, whereas the other branch is in turn the sum of power ratios of the rest of the \(N-1\) branches; or in other words, 
\((N-1)/N\).

![Fig. 1. A Schematic diagram of a wideband NTL N-way WPD.](image-url)
Following the procedure presented in [14], \( Z_{in} \) is found to be equal to 103 \( \Omega \). Once the characteristic impedance of the \( n \)-th branch is determined, the process is iterated until the characteristic impedances of all the \( N \) original branches are obtained. In this context, the equivalent 2-way model is developed only once as the power is split equally between the \( N \) output ports (i.e., same characteristic impedances \( Z_{in} \) for all \( N \) branches).

### A. Even Mode Analysis

The even mode equivalent circuit for the proposed \( N \)-way divider is shown in Fig. 3. The NTL has a length \( L \) with a varying characterisitics impedance \( Z(z) \) and propagation constant \( \beta(z) \), and matches a source impedance \( Z_s \) to a load impedance \( Z_L \). The isolation resistors \( R_{ij/2} (j=1,2,3) \) are terminated with an open circuit as a result of the symmetric excitation at the two equivalent output ports. To design the NTL, the magnitude of the reflection coefficient, \(|\Gamma|\), should be zero (or very small) over the frequency range of interest. \(|\Gamma|\) at the input port is expressed in terms of \( Z'_{in} \) shown in Fig. 3, where \( Z'_{in} \) is calculated after obtaining the \( ABCD \) parameters of the NTL.

\[
\begin{bmatrix} A & B \\ C & D \end{bmatrix}_{Z(z)} = \begin{bmatrix} A_1 & B_1 \\ C_1 & D_1 \end{bmatrix} \cdots \begin{bmatrix} A_K & B_K \\ C_K & D_K \end{bmatrix},
\]

where the \( ABCD \) parameters of the \( k \)-th segment are [15] (assuming lossless transmission lines):

\[
A_i = D_i = \cos(\Delta \theta), \quad B_i = Z^2 ((i-0.5)\Delta z) C_i = j Z ((i-0.5)\Delta z) \sin(\Delta \theta), \quad i = 1, 2, \ldots, K,
\]

\[
\Delta \theta = \frac{2\pi}{\lambda} \Delta z = \frac{2\pi}{c} f \sqrt{\varepsilon_{eff}} \Delta z.
\]

where \( c \) is the speed of light and \( f \) is the center frequency of the design bandwidth. The effective dielectric constant, \( \varepsilon_{eff} \), of each section is calculated using the well-known microstrip line formulas [15]. Furthermore, the non-uniform impedance profile is governed by a truncated Fourier series that is expressed as [16]:

\[
Z(z) = Z_{in} \exp \left( c_0 + \sum_{p=1}^{P} \left[ a_p \cos \left( \frac{2\pi p z}{d} \right) + b_p \sin \left( \frac{2\pi p z}{d} \right) \right] \right).
\]

where \( Z_{in} = (Z_s Z_L)^{0.5} \) is the characteristic impedance of the WPD branch. Thus, an optimum designed NTL has its reflection coefficient magnitude over the frequency range of interest, with an increment of \( \Delta f \) as close as possible to zero. Therefore, the optimum values of the Fourier coefficients can be obtained through minimizing the following error function [17]:

\[
\text{Error}_{in} = \max(E_{in}^{P_m}, E_{in}^{L_m}),
\]

where

\[
E_{in}^{P_m} = |\Gamma_{in} (f_m)|^2.
\]

\[
\Gamma_{in} (f_m) = Z_{in}^{P_m} (f_m) - Z_s
\]

\[
Z_{in}^{P_m} (f_m) = \frac{A (f_m) Z_1 + B (f_m)}{C (f_m) Z_1 + D (f_m)}.
\]

The resulting \( Z(z) \) should be within reasonable fabrication tolerances to ensure easy fabrication. As such, the following physical constraint is considered in the minimization of (4):

\[
Z_{min} \leq Z(z) \leq Z_{max}
\]

To find the values of the coefficients \((c_0, a_p, b_p)\) that minimize the bound-constrained nonlinear error function in (4) across the desired bandwidth, MATLAB function "fmincon.m" is used.

### B. Odd Mode Analysis

Figure 4 shows the equivalent odd-mode circuit of the proposed divider which is used to obtain the optimum values of the isolation resistors that achieve acceptable output ports isolation and matching conditions. Due to the asymmetric excitation of the output ports, each \( R_{ij/2} \) resistor will be terminated with a short circuit.

\[
3^{rd} \text{Section} \quad 2^{nd} \text{Section} \quad 1^{st} \text{Section}
\]

\[
V_2 \quad V_1 \quad Z_{in}^o
\]

After determining the optimum values of the Fourier series coefficients by following the procedure described previously, the NTL transformer is subdivided into 3 sections, and the \( ABCD \) matrix for each section is calculated by employing (1) and (2). Then, the total \( ABCD \) matrix of the whole network shown in Fig. 4 can be calculated as follows [17]:

\[
ABCD = \begin{bmatrix} A & B \\ C & D \end{bmatrix}_1 \begin{bmatrix} A & B \\ C & D \end{bmatrix}_2 \begin{bmatrix} A & B \\ C & D \end{bmatrix}_3.
\]
The locations of the resistors are distributed uniformly. Finally, as illustrated in Fig. 4, the following equation can be written:

\[
\begin{bmatrix}
V_1 \\
I_1
\end{bmatrix} = \begin{bmatrix} A & B \\
C & D \end{bmatrix}_{\text{Total}} \begin{bmatrix}
V_2 \\
I_2
\end{bmatrix}.
\]  

(8)

Setting \( V_2 \) in (8) to zero, and solving for \( V_1 / I_1 \), one obtains:

\[
\frac{V_1}{I_1} = \frac{B}{D} = Z^o_{in}.
\]  

(9)

For perfect output port matching, the following condition should be satisfied:

\[
\Gamma_{out}(f_m) = \frac{Z_{\text{in}}^o(f_m) - Z_0}{Z_{\text{in}}^o(f_m) + Z_0}.
\]  

(10)

where \( f_m \) \( (m = 1, 2, \ldots, M) \) denotes the frequencies at which (10) is calculated. In this context, \( \Delta f \) is chosen to be 0.2 GHz. So, for a perfect output ports matching over the desired range, the following error should be minimized [17]:

\[
\text{Error}_{\text{out}} = \max(E_{11}^{\text{out}}, \ldots E_{M}^{\text{out}}) - E_{M}^{\text{out}}).
\]  

(11.a)

where

\[
E_{m}^{\text{out}} = |\Gamma_{out}(f_m)|^2.
\]  

(11.b)

This optimization problem is solved keeping in mind that \( R_{11}, R_{12}, \) and \( R_{13} \) are the optimization variables to be determined.

III. SIMULATIONS AND MEASUREMENTS

In this section, based on the design procedure presented in II, a design example of a 3-way equal split WPD with fractional bandwidth of 86% is simulated, fabricated and measured. The design example is carried out using RO4003C substrate with a thickness of 0.813 mm, relative permittivity of 3.55, and loss tangent of 0.0027. The length of each NTL transformer of the proposed WPD is set to 10 mm. The characteristic impedance of the conventional 3-way WPD arm, \( Z_0 \), is calculated in II and is found to be equal 103 \( \Omega \). Figure 5 shows a photograph of the fabricated power divider.

Simulations were obtained using HFSS, which is a full-wave EM simulator, whereas measurements were made with an HP 8720B vector network analyzer (VNA). Short-open-load-thru calibration was performed to the two ports of the VNA using a 3.5 mm HP/Agilent 85052A mechanical calibration kit. First, port 1 of the VNA was connected to an open-circuit standard and calibrated. Then, it was connected to a short-circuit standard and calibrated. Finally, it was connected to a broadband 50 \( \Omega \) matched load for load calibration. The same process was repeated for port 2 of the VNA. Thru calibration was made by connecting the two VNA ports together to compensate for the losses due to cables and connectors.

After a two-port calibration was performed, input/output matching parameters of the proposed divider/combiner were measured by connecting VNA port 1 to the divider’s port of interest, while terminating the remaining ports with a matched load. Transmission parameters were measured by connecting VNA port 1 to the input port of the proposed divider and VNA port 2 to one of the output ports; whereas the rest of the divider’s ports were terminated with a matched load. The same process was repeated for port 2 of the VNA. Thru calibration was made by connecting the two VNA ports together to compensate for the losses due to cables and connectors.

As shown in Fig. 6, simulation and measurement results of the input port matching are below \(-12 \text{ dB}\) over the 4–10 GHz band.

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Fig. 5. Photograph of the fabricated 3-way WPD structure.

Fig. 6. Simulated and measured S-parameters of the proposed divider.

Fig. 7. Simulated and measured S-parameters of the proposed divider.
A new high efficiency, high power transmitter modules, S. Shamaileh, V. Devabhaktuni, and N. Dib, “scheme and measurement results over the purposes, 3
divider to its equivalent 2
fundamental
proposed device excellent symmetry of the fabricated layout and hence the ±5.4° over the design bandwidth.
imbalance equals to
in Fig. 8. Measured results show almost a constant response of 0.18 ns for both S21 and S31 over the 4–10 GHz band (group delay of S41 = group delay of S21 due to structural symmetry).

Figure 9 shows the measured magnitude and phase imbalances for the proposed equal-split in-phase divider. Measured magnitude imbalance equals to ±0.37 dB, whereas the phase imbalance is ±5.4° over the design bandwidth. Such results indicate an excellent symmetry of the fabricated layout and hence the proposed device can operate as a power combiner as desired.

IV. CONCLUSION
This paper presented a general design of N-way wideband power divider/combiner that can be used in PAs which are a fundamental component in a variety of wireless communication systems. A combining technique was used to reduce the N-way divider to its equivalent 2-way model. Then, the even and odd mode analysis were used to obtain the NTLs and the optimized values of the isolation resistors, respectively. For verification purposes, 3-way power divider/combiner with fractional bandwidth of 86% was fabricated and measured. The good agreement between both simulation and measurement results over the assigned frequency band proves the validity of the design procedure.

REFERENCES