On the Bits per Joule Optimization in Cellular Cognitive Radio Networks

Wuchen Tang, Muhammad Z. Shakir, Khalid A. Qaraqe, Erchin Serpedin, Muhammad A. Imran, and Rahim Tafazolli

Abstract—Cognitive radio has emerged as a promising paradigm to improve the spectrum usage efficiency and to cope with the spectrum scarcity problem through dynamically detecting and re-allocating white spaces in licensed radio band to unlicensed users. However, cognitive radio may cause extra energy consumption because it relies on new and extra technologies and algorithms. The main objective of this work is to enhance the energy efficiency of proposed cellular cognitive radio network (CRN), which is defined as bits/Joule/Hz. In this paper, a typical frame structure of a secondary system user (SU) is considered, which consists of sensing and data transmission slots. We analyze and derive the expression for energy efficiency for the proposed CRN as a function of sensing and data transmission duration. The optimal frame structure for maximum bits per joule is investigated under practical network traffic environments. The impact of optimal sensing time and frame length on the achievable energy efficiency, throughput and interference are investigated and verified by simulation results compared with relevant state of art. Our analytical results are in perfect agreement with the empirical results and provide useful insights on how to select sensing length and frame length subject to network environment and required network performance.

Index Terms—Cellular cognitive radio networks; energy efficiency; throughput; spectrum sensing; optimal frame structure.

I. INTRODUCTION

Spectrum efficiency is a critical issue for cellular communication networks. However, recent reports by Federal Communications Commission (FCC) have pointed out that 70% of the allocated spectrum bands in the US is not fully utilized, whereas only 2% of the spectrum is used in the US at any given moment of time. [1]. Cognitive radio was first introduced in 1999 [2] to improve the current severely underutilized, whereas only 2% of the spectrum is used in the US. The FCC has pointed out that 70% of the allocated spectrum bands in the US is not fully utilized, whereas only 2% of the spectrum is used in the US at any given moment of time. [1]. Cognitive radio was first introduced in 1999 [2] to improve the current severely underutilized spectral white space, whereas only 2% of the spectrum is used in the US. The FCC has pointed out that 70% of the allocated spectrum bands in the US is not fully utilized, whereas only 2% of the spectrum is used in the US at any given moment of time. [1]. Cognitive radio was first introduced in 1999 [2] to improve the current severely underutilized spectrum white space.

In addition to spectrum efficiency enhancement as the primary target, another important issue for the sustainable development of cognitive radio technology for cellular networks is energy efficiency, which has been recently marked as one of the alarming bottlenecks in the telecommunication growth paradigm mainly due to dramatically varying global climate [6] and slowly progressing battery technology [7]. Therefore, currently green radio is playing an equally or even more important role than increasing the communication capacity and has prompted new waves of research and standard development activities. High energy efficiency will be one of the key requirements for practical deployment of cellular cognitive radio networks (CRNs). However, the majority of the current research still aims at improving the throughput of CRN [8–10] while energy-efficiency issues in CRN have not been well addressed until recently when some works have started to touch. In [11], the optimal sensing strategy is studied based on sequential sensing over multiple channels. The sensing-access strategies and the sensing order are identified to achieve the maximum energy efficiency. However, only the variable sensing length is considered. In [12], the authors proposed energy efficient transmission duration design and power allocation methods. However, the considered system model is very simple and the interference from PU to SU is ignored. Because the length of sensing slot is assumed fixed, the impact of the sensing length on the sensing accuracy is not considered.

B. Main Contribution

In this paper, we investigate the variable frame structure of SU which consists of sensing and data transmission slots. The energy efficiency (bits/Joule/Hz) in the proposed cellular CRN is formulated as a function of variable sensing and data transmission slot durations under practical primary traffic load. The impact of optimal sensing time and frame length on the achievable energy efficiency, throughput and interference is investigated and studied. The accuracy of derived theoretical expressions is compared with relevant state of art and verified by simulation results. The selection of optimal sensing and data transmission slot durations of the SU cognitive transmission with different performance metrics, e.g., energy efficiency and throughput, under a practical traffic load environment is addressed and the diversity is highlighted in a cellular CRN set-up.

The rest of this paper is organized as follows. Section II defines the system model. In Section III, the problem of energy efficiency optimization is formulated followed by the analysis based on the frame structure. Performance analysis and discussions to validate the analytical results are presented in Section IV followed by the concluding remarks in Section V.

II. SYSTEM MODEL

In this paper, we consider the uplink of a single secondary system coexisting with a primary system in a cellular CRN. The cognitive data transmission of the SU is activated subject to the spectrum sensing outcomes. A typical frame structure of the SU is shown in Fig. 1 where the frame of length $T$ consists of the sensing slot with length $\tau$ and the data transmission slot with length $T-\tau$. The SU performs energy detection [13] for spectrum sensing and then decides to transmit or keep silent according to the sensing result. Once the channel has been confirmed as idle, the SU starts to transmit on the corresponding channel because we assume (i) the SU is heavily loaded and always has data to transmit due to its secondary priority, (ii)
the percentage of transmission with interference out of data
due to missed detection lead to more interference between
spectrum is actually occupied by the PUs and wrongly detected
sensing errors of the spectrum, that is, the situation where the

\[ P = \frac{\alpha_1}{T - \tau} \left(1 - \exp\left(-\frac{T - \tau}{\alpha_0}\right)\right). \]  

In addition, there may be additional interferences because of
sensing errors of the spectrum, that is, the situation where the

A new primary and secondary transmission on the
available channel consists of a transmission link and two
interference links, as depicted in Fig. 2, where Tx and Rx
denote the transmitter and receiver, respectively. The instan-
taneous channel gain of the secondary transmission link on
the available channel is denoted as \( h_{ss} \), while the interference
link from PU to SU and from SU to PU are shown as the
narrow arrows with channel gains \( h_{pu} \) and \( h_{sp} \), respectively.
Channel is assumed ergodic stationary and known before the
transmission phase. The quality of channel could be
estimated in a very short time interval compared with the
sensing length. For example, in IEEE 802.11a, only 4 pilot
symbols are used for channel estimation [14] while in IEEE
802.22 wireless regional area network (WRAN) thousands of
samples are required for a typical sensing [8]. Therefore, for
the frame structure of SU, the channel estimation time could
be ignored and thus is not considered in Fig. 1. The signals
of PU are assumed to be complex-valued phase-shift keying
(PSK) signals, whereas the noise at the SU is assumed to be
independent and identically distributed circularly symmetric
complex Gaussian (CSCG) with zero mean and \( N_0 \) variance.

It is noted that even if the channel is sensed and is available
for SU to transmit, the corresponding PU might still become
activated during the data transmission phase of the current
frame. This would lead to the situation that both the SU and the
PU transmit on the same channel and interfere with each other.
In this case, the percentage of transmission with interference
due to this PU unpredictable activity out of data transmission
duration could be expressed as [15]

\[ P_s = 1 - \frac{\alpha_0}{T - \tau} \left(1 - \exp\left(-\frac{T - \tau}{\alpha_0}\right)\right). \]  

Moreover, in contrast with missed detection, another type
of sensing errors that is referred to as false alarm, describes
the situation that the spectrum is actually idle and wrongly de-
dected as occupied by the PUs, which would also decrease the
throughput and thus affect energy efficiency of cellular CRNs.
Therefore, the optimal sensing time should be addressed in
order to provide sufficient sensing accuracy and save the time
as much as possible for data transmission in a unit frame.

III. ENERGY EFFICIENCY OF PROPOSED CELLULAR CRN

In this work, the SU employs energy detection spectrum
sensing and transmits based on the decision made by the
sensing phase. To control the interference to PU, the target
detection probability \( P_{fa} \) should be guaranteed. With given
sensing length and \( T_d \), the probability of false alarm for the
licensed channel under energy detection scheme is given by
[8]:

\[ P_{fa}(\tau) = Q \left(\sqrt{2\gamma + 1}Q^{-1}(\gamma_d) + \sqrt{\tau}\right), \]  

where \( \tau \) represents the sensing time, \( \gamma \) denotes the received
SNR from the PU at the secondary detector on the licensed
channel, \( f_s \) represents the sampling frequency and \( Q(\cdot) \) stands
for the complementary distribution function of the standard
Gaussian.

Then, if the licensed channel is detected as idle (\( H_0 \)), the
SU would perform data transmission during the data
transmission slot, whereas if the licensed band is sensed as
occupied (\( H_1 \)), the SU has to keep silent until the next frame.
The instantaneous transmission rate of the SU on the licensed
channel is denoted by \( r_0 \) when the channel is actual idle,
and is denoted by \( r_1 \) when the channel is actual occupied
by PU, which occurs when both the SU and the PU transmit
on the same channel and interfere with each other. Based on
the transmission interference links depicted in Fig. 2, \( r_0 \) and
\( r_1 \) are respectively given by

\[ r_0 = \log_2 \left(1 + \frac{h_{ss} P_{su}^t}{N_0}\right) = \log_2 \left(1 + \frac{P_{su}^0}{N_0}\right), \]  

\[ r_1 = \log_2 \left(1 + \frac{h_{ss} P_{pu}^t}{h_{ps} P_{su}^t + N_0}\right) = \log_2 \left(1 + \frac{P_{pu}^0}{P_{su}^0 + N_0}\right), \]  

where \( P_{su}^t \) and \( P_{pu}^t \) define the transmission power while \( P_{su}^0 \)
and \( P_{pu}^0 \) define the received power levels of secondary signal
and primary signal at secondary receiver, respectively.

Based on the above analysis, the average interference to the
PU and the average throughput of the SU could be expressed
by (4) and (5), respectively (at the top of next page).

In order to formulate the energy efficiency problem of SU,
the power consumed in a frame duration should be addressed,
which mainly contains three parts: electronic circuit con-
sumption \( P_e \), spectrum sensing consumption \( P_s \), and the
data transmission consumption on the licensed channel \( P_{su}^t \). The
electronic circuit power \( P_e \) is the average power assumption
of device electronics, such as mixers, filters, and digital to
analog converters, and it is almost fixed (given). Generally, the power
used during spectrum sensing is much smaller compared to the
data transmission power. The average total power consumed
within a frame could be calculated as


\[ I = \frac{T - \tau}{T} \mathbb{E}\left\{ \left[ P \left( H_0 \right) \left( 1 - \mathcal{P}_{fa} \right) P_s - \mathbb{E}\left[ P(0) \left( 1 - \mathcal{P}_{fa} \right) P_s + P(\mathcal{H}_1) \left( 1 - \mathcal{P}_d \right) P_{sp} \right] \right\}. \]

\[ R = \frac{T - \tau}{T} \mathbb{E}\left\{ P \left( H_0 \right) \left( 1 - \mathcal{P}_{fa} \right) \left( r_0 \left( 1 - P_s \right) + r_1 P_s \right) + P(\mathcal{H}_1) \left( 1 - \mathcal{P}_d \right) \left( r_0 \left( 1 - P_{sp} \right) + r_1 P_{sp} \right) \right\}. \]

\[ J = \frac{(T - \tau)}{P_c T + P_s \tau + P_{su} (T - \tau)} \left( \frac{P \left( H_0 \right) \left( 1 - \mathcal{P}_{fa} \right) \left( r_0 \left( 1 - P_s \right) + r_1 P_s \right) + P(\mathcal{H}_1) \left( 1 - \mathcal{P}_d \right) \left( r_0 \left( 1 - P_{sp} \right) + r_1 P_{sp} \right)}{P(\mathcal{H}_0) \left( 1 - \mathcal{P}_{fa} \right) + P(\mathcal{H}_1) \left( 1 - \mathcal{P}_d \right)} \right) \]

which could be expressed using conditional probability theory as

\[ E = \frac{\text{Average Number of the Bits Received}}{\text{Average Total Energy Consumed}} = \frac{RT}{E} \]

and it is measured in bits/Joule/Hz. By substituting (5) and (7) into (8), we can express the energy efficiency of SU in the considered cellular CRN with power control as (9) (at the top of this page).

Based on the derived energy efficiency formula for our proposed cellular CRN, the energy efficiency optimization problem, under the average interference constraint and total transmission power constraint can be formulated as follows

\[ \text{maximize } \mathbb{E}\{J\} \]

\[ \text{subject to } I \leq \mathcal{I}, R \geq \mathcal{R}, T > \tau > 0. \]

where \( \mathbb{E}\{J\} \) represents the expectation of \( J \). Variable \( I \) denotes maximum acceptable interference for PU and \( \mathcal{R} \) is the targeted throughput for the SU. It can be seen that (10) is exceptionally complex with complicated expressions for \( I \) and \( \mathcal{R} \). The constraints \( \mathcal{I}, \mathcal{R} \) are also not fixed due to different QoS of different wireless networks.

To explore the optimal sensing and frame slot duration, we take into account the concavity of the energy efficiency \( J \) and throughput \( R \). First, we examine the throughput which presents a simpler expression as energy efficiency. If we define \( D = T - \tau \) which indicates the data transmission length, the expression of \( R \), (5), can be considered as function of \( (\tau, D) \). Variables \( \tau \) and \( D \) are independent so that \( P_s \) and \( P_{sp} \) are as both functions of \( D \) and have nothing to do with \( \tau \). In this case, according to the Theorem 1 of [8], one can conclude that there exists an optimal sensing time which yields the maximum achievable throughput and \( R \) is concave for the range of \( \tau \) in which \( \mathcal{P}_{fa} \leq 0.5 \).

**Proposition 1**: Given the throughput of the SU as \( R \), \( R \) is not concave with respect to the frame length \( T \).

**Proof**: See Appendix A.

In the sequel, as \( J = \frac{RT}{E} \), the convexity of the derived energy efficiency with respect to \( \tau \) and \( T \) both depend on the value of multiplication factor \( \frac{T}{E} \). In this case optimal values of \( \tau \) and \( T \) depend on the specific system characteristics in particular, on the assumed power consumption and primary traffic model. In order to find this value for the considered system conditions, different values of \( \tau \) and \( T \) have to be systematically tested to calculate the energy efficiency. That is, an exhaustive search has to be performed and it may require a certain amount of time and resources to obtain the optimum value. However, the values of \( \tau \) and \( T \) for the system is operational and it does not have to be calculated dynamically when the system is operational do not have to be computed dynamically if the PU traffic model does not change significantly. In other words, the optimal values of \( \tau \) and \( T \) can be obtained off-line only once for a particular system with stable PU traffic load and then they do not have to be re-calculated again in a short term.

**IV. PERFORMANCE ANALYSIS AND DISCUSSIONS**

In this section, we present and discuss the simulation results of the proposed cellular CRN environment with variable frame structure. We assume that all the mobile users including both the PU and SU are mutually independent and uniformly distributed in the typical cellular CRN. The probability density function (PDF) of the distribution of mobile users which are located at \( (r_d, \theta_d) \) from its serving base station (BS) and can be given in polar coordinate as

\[ p(r_d, \theta_d) = \frac{r_d}{\pi R^2}, \]

where \( R_m \) is the radius of macro-cell, \( 0 \leq r_d \leq R_m \) and \( 0 \leq \theta \leq 2\pi \). To simulate a real channel environment, we consider a two slope path-loss model to obtain the mean received power as a function of distance between the mobile user and the respective serving BS [16]. Energy detection is employed for spectrum sensing. Simulated results are obtained using 10000 Monte-Carlo simulations. Major metrics such as energy efficiency and throughput are illustrated in per Hz basis. Unless otherwise stated, the values of the other parameters used are listed in Table I.

Fig. 3 consists of two sub-figures that illustrate energy efficiency of SU as a function of variable sensing length and variable frame length with fixed frame duration \( T = 100 \) ms and with fixed sensing duration \( \tau = 2 \) ms, respectively. It can be clearly observed that there is an optimal sensing length with maximum achievable energy efficiency located at 1.8 ms while the optimal frame length value is located at 132 ms. It is to note that the variable frame length is equivalent to a variable data transmission length if the sensing length is fixed. In addition, energy efficiency extended from the state-of-the-art method [8] is illustrated by dashed lines for comparison.
It can be seen that our theoretical analysis based on derived expressions in Section III is much more accurate than that in [8] because unsynchronized traffic activity is considered which is a realistic feature in real network environments.

The achievable throughput results are also provided in Fig. 4, which shows a very similar trend to the energy efficiency. However, compared with the optimal sensing value at 1.8 ms for maximum energy efficiency, there is still a diversity in terms of the optimal sensing lengths for maximum throughput, which is located at 2.2 ms. A similar diversity between the optimal frame lengths for maximum energy efficiency and throughput also exists at 132 ms and 236 ms, respectively. Moreover, the derived throughput in [8] is also much lower than the values predicted by simulation results and the corresponding optimal sensing length with bias is 2.55 ms because of the same reason that ideal synchronization is assumed between the SU and PU traffic activities. It is observed that the our theoretical and simulated results are in perfect agreement for all cases.

Last but not least, the caused interference with the increase in sensing length and frame length is illustrated by Fig. 5. There is a non-intuitive result shown in Fig. 5. When the sensing time is very short such as less than 1.5 ms, interference increases with the increase in sensing time. This is because the target $\mathcal{P}_d$ is fixed as 0.9, and as $\tau$ increases, $\mathcal{P}_\sigma$ decreases which leads to more cognitive secondary transmission and thus higher $P_s^\alpha$. However, the level of interference decreases with a further significant increase in spectrum sensing time $\tau$ since $\mathcal{P}_d$ will now be a rather small constant under such condition. Therefore, allocating more time for spectrum sensing with a fixed frame length such as 100 ms, leads to an accurate spectrum sensing and thereby reduces the interference with a fixed frame length. While the result pertaining to various frame durations with fixed sensing length is much more intuitive, it can be justified through the fact that longer frame durations lead to a much higher $P_s^\alpha$ which causes additional interference. Additionally, consistent with previous energy efficiency and throughput results, the interference levels extended from [8] are significantly underestimated compared to our simulation results.

V. CONCLUSIONS

In this paper, we analyzed the energy efficiency of the SU in a proposed cellular CRN based on the frame structure which consists of variable sensing and data transmission slots. The achievable bits per Joule of the SU has been analytically expressed under a realistic VOIP traffic model. The impact of variable sensing and frame lengths, on the achievable energy efficiency and interference have been critically illustrated with energy detection spectrum sensing. Moreover, the SU’s achievable throughput is also provided for comparison. The analysis of the diversity between the optimal frame structures with achievable maximum energy efficiency and throughput of the SU is useful to determine the future required cognitive frame structure for cellular CRN. The accuracy of our analysis
has been verified by both simulations and comparisons with relevant state of art. The proper frame structure should also be adaptively chosen to achieve the required performance of the SU and at the same time to further reduce the interference to the legal PU.

APPENDIX A: PROOF OF PROPOSITION 1

The first partial derivative of variable $R$ with respect to $T$ can be expressed as

$$R(T) = \frac{\tau}{T^2} \left\{ P(H_0) (1 - \mathcal{P}_{fa}) \left( r_0 (1 - P_{p}^a) + r_1 P_{ip}^a \right) ight. \right.$$  

$$+ P(H_1) (1 - \mathcal{P}_{d}) \left( r_0 (1 - P_{ip}^a) + r_1 P_{p}^a \right) \right. $$

$$+ \frac{T - \tau}{T} \left\{ P(H_0) (1 - \mathcal{P}_{fa}) \left( r_0 \left( -\frac{\partial P_{p}^a}{\partial T} \right) + \frac{r_1}{\tau} \frac{\partial P_{p}^a}{\partial T} \right) \right.$$  

$$+ P(H_1) (1 - \mathcal{P}_{d}) \left( r_0 \left( -\frac{\partial P_{ip}^a}{\partial T} \right) + \frac{r_1}{\tau} \frac{\partial P_{ip}^a}{\partial T} \right) \right\}. \quad (A.1)$$

With series expansion of exponential function $e^x = 1 + \frac{x}{\tau} + \frac{x^2}{2!} + \frac{x^3}{3!} + \ldots$ and when $T$ approaches $\tau$ and $+\infty$, the limits of $P_{p}^a$ and $P_{ip}^a$ are equal to as

$$\lim_{T \to \tau} P_{p}^a = \lim_{T \to \tau} \left( 1 - \frac{\alpha_0}{T - \tau} \left( 1 - \exp \left( -\frac{T - \tau}{\alpha_0} \right) \right) \right) = 0, \quad (A.2)$$

$$\lim_{T \to +\infty} P_{p}^a = \lim_{T \to +\infty} \left( 1 - \frac{\alpha_0}{T - \tau} \left( 1 - \exp \left( -\frac{T - \tau}{\alpha_0} \right) \right) \right) = 1, \quad (A.3)$$

$$\lim_{T \to +\infty} P_{ip}^a = \lim_{T \to +\infty} \left( 1 - \frac{\alpha_0}{T - \tau} \left( 1 - \exp \left( -\frac{T - \tau}{\alpha_0} \right) \right) \right) = 0, \quad (A.4)$$

respectively.

Similarly, the limits of $\frac{\partial P_{p}^a}{\partial T}(T - \tau)$ and $\frac{\partial P_{ip}^a}{\partial T}(T - \tau)$ when $T$ approaches $\tau$ and $+\infty$ can be expressed as

$$\lim_{T \to \tau} \frac{\partial P_{p}^a}{\partial T}(T - \tau) = \lim_{T \to \tau} \frac{\alpha_0}{T - \tau} \left( 1 - \exp \left( -\frac{T - \tau}{\alpha_0} \right) \right) = 0, \quad (A.6)$$

$$\lim_{T \to +\infty} \frac{\partial P_{p}^a}{\partial T}(T - \tau) = \lim_{T \to +\infty} \frac{-\alpha_0}{T - \tau} \left( 1 - \exp \left( -\frac{T - \tau}{\alpha_0} \right) \right) = 0, \quad (A.7)$$

$$\lim_{T \to +\infty} \frac{\partial P_{ip}^a}{\partial T}(T - \tau) = \lim_{T \to +\infty} \frac{\partial P_{ip}^a}{\partial T}(T - \tau) = 0, \quad (A.8)$$

By substituting the equations (A.2) - (A.8) into (A.1), the limits of $R(T)$, when $T$ approaches $\tau$ and $+\infty$, can be finally expressed as

$$\lim_{T \to \tau} R(T) = \frac{1}{\tau} \left[ P(H_0) (1 - \mathcal{P}_{fa}) r_0 + P(H_1) (1 - \mathcal{P}_{d}) r_1 \right] > 0,$$

$$\lim_{T \to +\infty} R(T) = 0 \left[ P(H_0) (1 - \mathcal{P}_{fa}) r_1 + P(H_1) (1 - \mathcal{P}_{d}) r_0 \right] = 0, \quad (A.9)$$

respectively.

REFERENCES


