Spectroscopy of neutron-rich $^{168,170}$Dy: Yrast band evolution close to the $N_pN_n$ valence maximum


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The yrast sequence of the neutron-rich dysprosium isotope $^{168}$Dy has been studied using multinucleon transfer reactions following collisions between a 460-MeV $^{82}$Se beam and an $^{170}$Er target. The reaction products were identified using the PRISMA magnetic spectrometer and the $\gamma$ rays detected using the CLARA HPGe-detector array. The 2$^+$ and 4$^+$ members of the previously measured ground-state rotational band of $^{168}$Dy have been confirmed and the yrast band extended up to 10$^+$. A tentative candidate for the $4^+ \rightarrow 2^+$ transition in $^{170}$Dy was also identified. The data on these nuclei and on the lighter even-even dysprosium isotopes are interpreted in terms of total Routhian surface calculations and the evolution of collectivity in the vicinity of the proton-neutron valence product maximum is discussed.

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I. INTRODUCTION

Our microscopic understanding of nuclei rests to a large extent upon the well-known shell model with the magic neutron and proton numbers occurring near to stability at $N, Z = 2, 8, 20, 28, 50, 82,$ and 126. The features associated with this model appear most clearly for nuclei in the vicinity of closed shells. Another important approach to the nuclear many-body problem is the macroscopic understanding that is based on the collective properties of nuclei. These properties are most prominent in the regions around the doubly midshell nuclei which maximizes the number of possible neutron and proton interactions. The importance of the number of proton-neutron interactions, which is equal to the product of valence nucleons $N_pN_n$, for quadrupole collectivity is well known [11]. It has been shown that both the energy, $E(2^+)$, and the reduced transition probability, $B(E2)$, of the first 2$^+$ state, as well as the energy ratio $E(4^+)/E(2^+)$ have a smooth dependence on this quantity [2–5].

Neglecting any potential subshell closures, the nucleus with the largest number of valence particles with $A < 208$ is $^{170}$Dy. Accordingly, it should be one of the most collective of all nuclei in its ground state [6]. However, at present nothing is known experimentally about $^{170}$Dy, which makes the nucleus with the largest $N_pN_n$ value below $^{208}$Pb with excited states reported in the current literature [7]. It is also the most neutron-rich, even-Ne dysprosium isotope that has been studied to date. The isotope $^{169}$Dy has been identified but no excited states have been observed [8]. Looking how $E(2^+)$ changes in Fig. 1, the dysprosium isotopes appear to become more collective, that is, have lower $E(2^+)$ values, with increasing neutron numbers from $^{160}$Dy up to $^{164}$Dy [9–11]. At $^{166}$Dy, however, $E(2^+)$ increases again [12,13], suggesting that the maximum collectivity in dysprosium...
II. EXPERIMENT

The nuclei studied in this article were populated using multinucleon transfer reactions of a $^{82}$Se beam and a 500 $\mu$g/cm$^2$ thick self-supporting $^{170}$Er target. The primary $^{82}$Se beam was delivered by the Tandem XTU-ALPI accelerator complex at Laboratori Nazionali di Legnaro (LNL) [18] and had an energy of 460 MeV with a typical intensity of $\sim$2 pA. Beamlike fragments were identified event by event using the PRISMA magnetic spectrometer [19]. PRISMA was placed at the grazing angle of 52°. The energies of $\gamma$ rays from both the beamlike and the targetlike fragments were measured using the CLARA $\gamma$-ray detector array [20].

The PRISMA magnetic spectrometer consists of a 50-cm-long and 30-cm-diameter quadrupole magnet and a dipole magnet with 1.2-m radius of curvature; it covers a solid angle of 80 msr. The atomic number ($Z$) resolution in this experiment was $Z/\Delta Z \approx 65$ and the mass resolution was $A/\Delta A \approx 200$ for elastic scattering of $^{82}$Se. At the entrance of PRISMA, 25 cm from the target, a position-sensitive microchannel plate (MCP) was placed. The MCP measured the ($\theta$, $\phi$) direction of the ion entering PRISMA and gave a time reference for the ion at the beginning of the spectrometer [21]. After the magnets, a 1-m-wide multiwire parallel-plate avalanche counter (MWPPAC) segmented in ten elements that measured the $(x, y)$ position and gave a time reference for the ion at the end of the spectrometer was mounted. This was followed by an ionization chamber segmented into four sections along the optical axis of PRISMA and ten sections transverse to it that measure the energy and energy-loss characteristics of the transmitted heavy ion [22]. From the energy measurements in the ionization chambers, the atomic number $Z$ of the ion could be determined.

Because of the neutron-rich nature of $^{166}$Dy it is not possible to study this nucleus and its neighbors using traditional methods of high-spin spectroscopy that employ fusion-evaporation reactions. To populate states in nuclei with $A > 164$ in the dysprosium isotopic chain, isotopic separation on-line followed by $\beta$-decay measurements [7], in-beam fragmentation [16], and deep inelastic multinucleon transfer reactions together with a binary partner gating technique have been used so far. However, the nucleus $^{170}$Dy is very hard to study even with these techniques. The latter technique is the one used in the current work. For a recent review on deep inelastic multinucleon transfer reactions, see Ref. [17].

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be determined using $\Delta E - E$ techniques. By reconstructing the trajectory in PRISMA from the position measurements in the MCP and the MWPPAC and the time of flight (TOF), the mass of the ion was determined [23]. In Fig. 2 the atomic number ($Z$) and mass ($A$) distribution of the beamlike fragments is shown for $Z = 34–36$ (i.e., Se, Br, and Kr ions). The velocity vector of the beamlike fragments were obtained from the ($x, y$) position in the MCP and the TOF between the MCP and the MWPPAC. Table I gives the relative experimental yields for $Z = 36$ ions.

In its full complement, CLARA consists of 25 Compton-suppressed clover detectors (in this experiment 23 clover detectors were mounted) distributed in a hemisphere opposite to the entrance of PRISMA, covering the angles $104^\circ–256^\circ$ with respect to the entrance direction of the ions in the spectrometer. Each clover detector is in turn composed of four germanium crystals surrounded by a bismuth germanate Compton-suppression shield. The triggers used in the experiment were coincidences between the MCP and CLARA or the MWPPAC and CLARA. For an event to be considered valid, the ion had to be detected in the MCP, the MWPPAC, and the ionization chamber, but not in any of the side ionization chambers. There also had to be at least one coincident $\gamma$ ray detected in CLARA.

Doppler correction was performed event by event using the velocity vectors measured by PRISMA. This gave an energy resolution of 4.4 keV (0.7 %) at 655 keV for the beamlike fragments and 5.8 keV (1.1 %) at 542 keV for the targetlike fragments. The velocity vector of the targetlike fragment was obtained using simple two-body kinematics between the beamlike fragment and the unobserved binary reaction partner (the targetlike fragment before neutron evaporation). Because the PRISMA MCP has an angular resolution of $\Delta \theta < 1^\circ$, the Doppler broadening of the beamlike fragments is mainly attributable to the finite angular size of the CLARA crystals.

Using the measured $Z$ of the beamlike fragments, the atomic number of the targetlike fragments was adopted under the assumption that there was no evaporation of charged particles. Using the same procedure, an upper limit on the mass of the targetlike fragment was obtained as the assumption of no evaporated particles is violated, particularly by neutron emission. Because only an upper limit of the mass was obtained from the PRISMA information, the $\gamma$-ray spectra contained lines not only from the maximum-mass dysprosium binary partner, but also from lighter dysprosium isotopes associated with neutron evaporation channels. The targetlike fragments could thus not be uniquely identified event by event. It was, however, possible to suppress the contribution from the lighter dysprosium isotopes by using the TOF information, corresponding to the total kinetic energy loss [24]. Because an energy greater than the separation energy of a neutron needs to be transferred from the beamlike fragment for the neutron to evaporate, beamlike fragments with a partner that evaporates neutrons will, on average, have a lower velocity than beamlike fragments originating from the pure binary transfer reaction channels. Requiring a high velocity of the beamlike fragment by setting conditions on the TOF information from PRISMA, the peaks corresponding to fragments that have undergone neutron evaporation could be heavily suppressed (see Fig. 3).

![FIG. 3.](image)

**FIG. 3.** Spectrum of $\gamma$-ray energies from targetlike fragments gated on the beamlike fragments $^{84}$Kr (top) and on beamlike fragments $^{84}$Kr plus a short time of flight (bottom). The transitions identified as the rotational band in $^{168}$Dy are marked with solid lines.

![FIG. 4.](image)

**FIG. 4.** (Color online) Coincidence $\gamma$-ray spectra gated on the beamlike fragments $^{84}$Kr and on the $\gamma$-ray energies 173, 268, 357, and 442 keV and the summed spectrum (open histogram) from top to bottom. An estimation of the background using adjacent gates are also shown (solid histogram). The background gates are about 20 times the width of the gates on the $\gamma$-ray peaks and normalized relative to the size of the peak gates. The transitions identified as the rotational band in $^{168}$Dy are marked with solid lines.
III. RESULTS AND DISCUSSION

The two previously reported γ-ray transitions in 168Dy at 75 and 173 keV are clearly apparent in this spectrum. Three previously unreported transitions at 268, 357, and 442 keV are also identified in the spectrum. The efficiency and internal-conversion corrected relative intensities of the γ rays shown in Fig. 3 are 1.7 ± 0.5, 1.00 ± 0.12, 0.62 ± 0.09, 0.30 ± 0.07, and 0.25 ± 0.08, respectively, assuming that the transitions are of E2 character. To verify that these transitions originate from the same decay sequence, the γγ-coincidence method was applied to the data. The results from the γγ-coincidence analysis (using an A and a Z selection) are shown in Fig. 4, which shows that the 173-, 268-, 357-, and 442-keV transitions form a mutually coincident γ-ray cascade, assumed to be the ground-state band excitations in 168Dy. The 2+ → 0+ transition is heavily converted and very close in energy to the corresponding transitions in the other even-N dysprosium isotopes and thus not included in the γγ-coincidence analysis.

The three new γ rays are assigned on the basis of systematics to be the transitions associated with the yrast 6+ → 4+, 8+ → 6+, and 10+ → 8+ decays in 168Dy. The level scheme deduced for 168Dy from the current work is shown in Fig. 1. Because no reported γ-ray lines exist in 170Dy that can be used for γγ-coincidences, the γ-ray energy of 777 keV, associated with the 2+ → 0+ transition in 82Kr [25], which is the binary reaction partner of 170Dy, was used. By using gates on the beamlike fragments, γ rays from neutron evaporation channels from the respective targetlike fragments can be TOF suppressed in the γγ-coincident spectrum. In Fig. 5, both the singles spectrum and the γγ-coincidence spectrum (using an A, a Z, and a TOF selection) are shown. Because of the finite Z resolution, there is a large leakage from 170Er in the singles spectrum. In both the singles spectrum and the γγ-coincident spectrum a peak appears at 163 keV. This peak is tentatively identified from the dysprosium energy systematics as a candidate for the transition associated with the yrast 4+ → 2+ decay in 170Dy. The corresponding 2+ → 0+ γ ray would be too weak to be observed because of internal conversion and detector efficiency.

As reported in Ref. [7], an irregularity in the energy systematics of the yrast 2+ and 4+ states exists at N = 98 for Z = 64 (gadolinium) and Z = 66 (dysprosium). Extending the systematics to higher spin shows that this irregularity also appears further up in the yrast band of Z = 66, showing that this is a systematic effect and not only a small fluctuation at low energies (see Fig. 6). This irregularity also appears in elements with larger Z at higher spin. According to existing

![FIG. 5. (Color online) Spectrum of γ-ray energies from targetlike fragments gated on the beamlike fragments 82Kr plus time of flight (top). Coincidence γ-ray spectra gated on the beamlike fragments 82Kr, time of flight plus the γ-ray energy 777 keV in the beamlike fragments (bottom). An estimation of the background using adjacent gates is also shown (solid histogram). The background gates are about 20 times the width of the gates on the γ-ray peaks and normalized relative to the size of the peak gates. The tentative γ ray associated with the yrast 4+ → 2+ transition in 170Dy is marked with a solid line.](image)

![FIG. 6. (Color online) Experimental energy levels for Z = 64 (gadolinium), Z = 66 (dysprosium), Z = 68 (erbium), Z = 70 (ytterbium), and Z = 72 (hafnium) isotopes with N = 94–108. The experimental values are obtained from Refs. [7,9–11,13,30–39] and the current work [red (gray) triangles].](image)

![FIG. 7. Experimental (circles) and calculated (solid line) moments of inertia at a rotational frequency of $\hbar \omega = 0.05, 0.10, 0.15,$ and 0.20 MeV for dysprosium isotopes with N = 94–104. The experimental values are obtained using linear interpolation between measured rotational frequencies from Refs. [7,9–11,13] and the current work.](image)
data, the global energy minimum at \( N = 104 \) is clear at low spins and stays quite stable up to \( I^* = 12^+ \). However, for \( Z = 68 \) (erbium) the energy levels of the isotopes with \( N = 102 \) and \( N = 104 \) increase relative to \( N = 98 \) even above the corresponding energy levels in \( Z = 70 \) (ytterbium), causing \( N = 98 \) to become a new global minimum. The data on \( ^{168}_{66}\text{Dy} \) presented in this article show no such increase relative to \( ^{164}_{66}\text{Dy} \).

The irregularity at \( N = 98 \) is not reproduced by the results of the total Routhian surface calculations [26–28] shown in Fig. 7. The irregularity could be caused by a strong interaction between the ground-state band and the two quasineutron bands in \( ^{166}_{66}\text{Dy} \) [29]. The interpretation that the irregularity is an effect in \( ^{166}_{66}\text{Dy} \) and not in neighboring isotopes is strengthened by the tentative identification of the \( 4^+ \rightarrow 2^+ \) transition at 163 keV in \( ^{170}_{66}\text{Dy} \) as well as higher spin systematics in neighboring elements. The energy systematic of the yrast band of \( ^{166}_{66}\text{Dy} \) as well as the tentative identification of the \( 4^+ \rightarrow 2^+ \) transition at 163 keV in \( ^{170}_{66}\text{Dy} \) further suggests that maximum collectivity in dysprosium isotopes does not occur at \( N = 98 \).


IV. SUMMARY

The current work demonstrates the possibility of identifying heavy, high-

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