A Node-Cooperative ARQ Scheme for Wireless Ad Hoc Networks
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Abstract—In this paper, the authors propose a node-cooperative automatic repeat request (ARQ) scheme for wireless ad hoc networks, which is suitable for mobile wireless channels with high and correlated frame-error profile. An analytical model based on a two-state Markovian process is proposed to describe the behavior of the proposed retransmission scheme and to obtain its throughput, average delay, and delay jitter. The results of Monte Carlo simulations are included to demonstrate the efficacy of the proposed scheme and to verify the accuracy of the analytical models. Results show that a cooperation among a small number of nodes can significantly improve the performance of the retransmission process in terms of throughput, average delay, and delay jitter by reducing the average duration of retransmission trials.

Index Terms—Automatic repeat request (ARQ), cooperative diversity, network performance, wireless ad hoc networks.

I. INTRODUCTION

COMMUNICATIONS over wireless channels in an ad hoc network usually suffer from high frame-error rates due to the limited transmission power, the user mobility, and the lack of protection against interfering signals. Automatic repeat request (ARQ) schemes are de facto parts of wireless link-layer protocols to combat the high frame-error rate and to avoid expensive retransmissions of erroneous data blocks by the transport layer’s error-control mechanism [2], [3]. Conventional ARQ schemes have been designed for wireline networks, where the frame errors are random. By random error, we mean that there is no correlation between frame-error probabilities for different frames. However, due to the inherent characteristics of the fading process in wireless channels, the frame errors appear in bursts rather than randomly. When the link between two communicating nodes is experiencing frame errors, there is a high probability that the bad channel condition will continue for a considerably long period. The duration of a bad channel condition or channel fading may be as long as the transmission time of multiple data frames. Conventional retransmission schemes are not very effective in such environments with bursty frame errors and will cause significant degradation in the performance of a link-layer protocol [14].

Recently, spatial-diversity techniques in different forms of multiple transmit and receive antennas have been proposed to improve the quality of communication over wireless fading channels. Multiple input and multiple output (MIMO) communication systems [4], [5] and the corresponding channel coding techniques, such as space time coding (STC) [6], have been proposed to utilize space diversity in the next-generation wireless networks. However, the implementation of multiple antennas on small mobile devices is quite difficult due to the device-size and cost constraints. An alternative form of space diversity can be achieved in a multiuser environment by allowing nodes to cooperate [1], [6], [7]. In cooperative communications, each node not only transmits and receives data for its own applications, but can also provide an alternative path for the other pairs of communicating nodes. In other words, each node acts as a relay node to facilitate better communications between other pairs of nodes at the link level.

The theoretical and implementation aspects of cooperative diversity in the physical layer have been areas of active interest among researchers [8]–[10]. However, to the best of our knowledge, the impacts of cooperative techniques on the upper layers of communication protocols have not been thoroughly studied so far.

In this paper, we propose a simple but effective ARQ scheme, namely node-cooperative stop and wait (NCSW) for wireless ad hoc networks. The proposed scheme is inspired by the idea of cooperative diversity in order to improve the performance of link-layer protocols. In the NCSW, nodes in the transmission range of each other form temporary cooperation groups. In conventional retransmission schemes, the neighbor nodes are oblivious to the ongoing transmission between a sender node and a receiver node. However, in the NCSW scheme, neighbor nodes that have enough resources and are willing to cooperate can assist the sender node in the retransmission process by retransmitting the same copy of the previous frame simultaneously. Intuitively, cooperation among individual nodes can increase the probability of a successful retransmission and mitigates negative impacts of the fading process. In order to investigate this intuition, we develop analytical models for the throughput, the average delay, and the delay jitter of the NCSW scheme by using a two-state Markov process for wireless fading channels. We present results of Monte Carlo simulations in order to demonstrate the better performance of the proposed scheme and to verify the accuracy of the analytical models. Both the analytical and the simulation results indicate that
cooperation of a small number of nodes can produce significant performance gain, especially when the average quality of the channel between the sender and the receiver nodes is poor.

The rest of this paper is organized as follows. In Section II, the underlying assumptions and the system model are specified. The proposed ARQ scheme and the analytical models are presented in Section III. Simulation results are given in Section IV. Some concluding remarks and possible future research are given in Section V.

II. SYSTEM MODEL

We consider an ad hoc wireless network model as shown in Fig. 1. For the sake of generality, a group of autonomous nodes without any central control is considered. Although there is no fixed infrastructure, the model can generalize other types of wireless networks with infrastructures, such as cellular networks and wireless LANs (WLANs). In fact, a single node in this model can be a mobile device, a base station, or an access point. A cooperation group is a subset of nodes that can reach each other with a single hop. In other words, nodes in a cooperation group are in the radio coverage area of each other.

Cooperation groups may be set up during the connection setup stage (e.g., call setup in cellular networks or association in WLAN) or packet level handshaking. There is no need for extra signaling in order to form and manage cooperation groups. Cooperation groups are dynamic groups without tight membership requirement. Each neighbor node may join several cooperation groups depending on its position, capability, and willingness to cooperate. The overall structure of cooperation groups can be different in the transmission time of different packets. Thus, the mobility of nodes does not disrupt the operation. As shown in Fig. 2, each of those cooperation groups can be modeled as a single-hop wireless network. At any time instant, one sender node captures the shared media to send a burst of frames to its intended destination node. During that time period, the neighbor nodes in the group monitor the shared channel to assist the sender and the receiver nodes if an error happens. The whole process is transparent from a sender node’s point of view. Thus, a sender node performs its normal operation. A receiver node only needs to know the number and identity of the neighbor nodes during the current packet transmission time. Intuitively, node cooperation can improve the probability of a successful retransmission if there are extra resources available. Otherwise, all nodes perform their normal operations.

A. Fading-Channel Model

Variations of the wireless channel gains due to the destructive and constructive combination of multiple propagations with different path delays and center frequencies is known as a fading process. For flat fading channels, where the power spectrum density of the channel is constant over the whole frequency band of the information signal, a two-state Markov process as illustrated in Fig. 3 can adequately describe the process of a frame success or a failure [13]. The channel is deemed to be in the good state (G) if a transmitted frame can be correctly decoded by the receiver; otherwise, when the channel is in the bad state (B), the transmitted frame cannot be decoded successfully and needs to be retransmitted by the sender.

If the channel is in state G during the transmission time of the current frame, it will either stay in state G with a probability \( 1 - q \) or move to state B with a probability \( q \) in the transmission time of the next frame. Similarly, starting
from state B, the channel will either stay in state B with a probability \((1 - r)\) or move to state G with a probability \(r\). Thus, the transition probability matrix for the two-state Markov process is

\[
\begin{bmatrix}
1 - q & q \\
r & 1 - r
\end{bmatrix}
\]

Let \(\epsilon(k)\) be the frame success or failure process, where the discrete time index \(k\) is the transmission of the \(k\)th frame. Let \(T_i\) be the duration of a single frame. Assuming a nonadaptive channel coding rate and a quasi-static fading process (i.e., the fading level is constant for the entire frame duration), the transmitted frame \(k\) cannot be decoded properly by the receiver if the channel power gain is below a certain threshold \(\gamma\) at a time instant \(k\), i.e.,

\[
\epsilon(k) = \begin{cases} 
B & \text{if } |\zeta(k)|^2 \leq \gamma \\
G & \text{if } |\zeta(k)|^2 > \gamma
\end{cases}
\]

(1)

where \(\zeta(k)\) represents the complex value of the fading envelope in the transmission time of frame \(k\). For slow fading channels, the fading envelope can be considered constant for the entire frame duration, i.e., the fading envelope can be considered as a quasi-static process. For a quasi-static Rayleigh fading channel, i.e., \(\zeta(k)\) has a Rayleigh probability distribution function (pdf), it has been shown in [14] that the transition parameters of the two-state Markov process in Fig. 3 can be given by

\[
r = \frac{Q(\theta, \rho\theta) - Q(\rho\theta, \theta)}{e^{\gamma} - 1} \\
q = \frac{1 - e^{-\gamma} - r}{e^{\gamma} - 1}
\]

(2)

where \(Q(\cdot, \cdot)\) is the Marcum Q function

\[
\theta = \sqrt{\frac{2\gamma}{1 - \rho^2}}
\]

and

\[
\rho = J_0(2\pi f_m T_i)
\]

and \(J_0(\cdot)\) is the zero-order Bessel function of the first kind. Similar Markovian models for the Rician and the Nakagami flat fading channels have been given in [15] and [16], respectively.

### III. Node-Cooperative SW Scheme

Depending on the relative velocity of communicating nodes, the average duration of a channel fading can be as long as the transmission time of several frames. For example, for a slow fading channel with a node speed of 5 km/h and a carrier frequency \(f_c = 2.4\) GHz, the average fading duration is about 60 ms [11]. For a typical frame length of 5 ms, a naive retransmission scheme such as the conventional SW has to retransmit an erroneous frame for an average of 12 times. The situation may be even worse in high-rate systems with shorter frame durations.

Space diversity is a well-known technique in communication systems to combat fading in wireless channels by providing diverse and independent paths between a transmitter and a receiver. In our network model shown in Fig. 1, since the channel status between different pairs of nodes are independent of each other, node cooperation can be used to implement a variant of space diversity, which is known as a cooperative diversity [7]. Cooperation among those nodes that happen to be in the same radio coverage area of each other can significantly improve the performance of a retransmission scheme by reducing the number of unsuccessful retransmission trials.

Inspired by the cooperative diversity, we propose an NCSW ARQ scheme. The core concept can be explained using the model shown in Fig. 2, where a sender node is transmitting to a destination node and a typical neighboring node is listening to the ongoing communication. In the NCSW, the error-control procedures of the sender and the receiver nodes are the same as those of a conventional SW retransmission scheme in Fig. 4. However, the neighbor nodes in a cooperation group implement an additional functionality, as shown in Fig. 5. If a transmitted frame cannot be decoded successfully by the receiver, as part of its normal operation, the receiver node will send an NAK to the sender node asking for a retransmission of the erroneous frame, and the sender node will respond to the NAK by retransmitting the frame. In the conventional retransmission scheme, the neighbor nodes are oblivious to the retransmissions between the sender and the receiver nodes. However, in the NCSW scheme, all the other nodes in the cooperation group monitor the ongoing communications between the sender and the receiver nodes. The neighbor nodes decode and store a
Fig. 4. SW ARQ (a) sender and (b) receiver.

copy of the last unacknowledged transmitted frame until the reception of a corresponding ACK. When a transmitted frame is acknowledged by the destination node, all the nodes in the cooperation group will drop their copy of the corresponding frame. However, when the neighbor nodes in a cooperation group receive an NAK from the destination node, they will cooperate with the sender in the retransmission process. Obviously, a node in a cooperation group can retransmit only if it has already received a correct copy of the requested frame. Even if a neighbor node has received a correct copy of the frame, cooperation is not mandatory, and each node may avoid cooperation for internal reasons or network considerations. This freedom of choice guarantees a backward compatibility of the NCSW protocol with the conventional SW protocol.

If proper coding and decoding schemes such as the distributed STC [12] are implemented in the physical layer, the probability of a successful retransmission will be significantly increased due to the diversity gain that can be achieved from the independent and diverse paths. Intuitively, if the channel coding scheme is capable of achieving a full diversity gain and all neighbor nodes have a correct copy of the frame, the probability of a successful retransmission for the NCSW scheme is

\[ 1 - \prod_i P_{ei} \]

where \( P_{ei} \) is the probability of a frame error from node \( i \) in the cooperation group to the destination node, and \( n \) is the number of all the cooperating nodes plus the sender node.

A. Protocol Analysis Model

In this section, we develop an analytical model to describe the frame success/failure process for the proposed NCSW ARQ scheme. The model is a key component for analyzing useful performance metrics such as throughput, average delay, and delay jitter. We accomplish the analysis in three steps.

1) We derive a cooperation model for a pair of sender and receiver nodes with a single neighbor node.
2) We model the impacts of an arbitrary number of neighbor nodes in the cooperation group as an equivalent super neighbor node.
3) We combine the model for the super neighbor node from step 2 and the cooperation model from step 1 to obtain a model for the frame success/failure process for a pair of sender and receiver nodes and an arbitrary number of neighbor nodes.

In step 1, we consider a sender/receiver pair of nodes with a single neighbor node as shown in Fig. 6. A two-state Markov model, as described in Section II, is used to specify a success or a failure of transmissions over a wireless fading channel. We use three distinct two-state Markov processes to model the primary channel from the sender node to the receiver node, the interim channel from the sender node to the neighbor node, and the relay channel from the neighbor node to the destination node.
The corresponding transition probability matrices are denoted as follows. For the primary channel

\[
\begin{bmatrix}
1 - q & q \\
r & 1 - r
\end{bmatrix}
\]

For the interim channel

\[
\begin{bmatrix}
1 - x & x \\
y & 1 - y
\end{bmatrix}
\]

For the relay channel

\[
\begin{bmatrix}
1 - a & a \\
b & 1 - b
\end{bmatrix}
\]

The corresponding transition probabilities are \((q, r), (x, y),\) and \((a, b),\) respectively. During the transmission time of frame \(k\), the neighbor node is in state \(B\) if it is not able to cooperate; otherwise, the neighbor node is considered to be in state \(G\). Assuming that the neighbor node is always willing to cooperate, it will be in state \(B\) at time instant \(k\) if frame \((k - 1)\) cannot be decoded properly by that particular neighbor node, or the relay channel from that particular neighbor to the receiver node is in state \(B\) at the time instant \(k\). With this argument, the status of the neighbor node at time instant \(k\) can be formulated as follows:

\[
N(k) = \begin{cases} 
G, & \text{if } I(k - 1) = G \text{ and } R(k) = G \\
B, & \text{otherwise} 
\end{cases}
\]  

where \(I(k)\) and \(R(k)\) denote the states of the interim and relay channels, respectively.

A four-state Markov model, as shown in Fig. 7, can be used to represent the process of transition among different states of \(\{I(k - 1), R(k)\}\).

Let \(\pi_i\) denote the probability of being in state \(S_i\) in Fig. 7. The following set of linear equations can be solved to obtain \(\pi_i\) for \(0 \leq i \leq 3\):

\[
\begin{bmatrix}
A_{00} & A_{10} & A_{20} & A_{30} \\
A_{01} & A_{11} & A_{21} & A_{31} \\
A_{02} & A_{12} & A_{22} & A_{32} \\
A_{03} & A_{13} & A_{23} & A_{33}
\end{bmatrix}
\begin{bmatrix}
\pi_0 \\
\pi_1 \\
\pi_2 \\
\pi_3
\end{bmatrix}
= 
\begin{bmatrix}
\pi_0 \\
\pi_1 \\
\pi_2 \\
\pi_3
\end{bmatrix}
\]

\[
\pi_0 + \pi_1 + \pi_2 + \pi_3 = 1
\]

where \(A_{ij}\) is the probability of transition from state \(S_i\) to state \(S_j\). As given in (4), \(N(k)\) can be modeled by another two-state Markov process with transition parameters of \((u, v)\), where \(u\) and \(v\) are defined as follows:

\[
u \triangleq P\{N(k) = B|N(k - 1) = G\}
\]

\[
v \triangleq P\{N(k) = G|N(k - 1) = B\}
\]

From the Markov process shown in Fig. 7, it can be seen that

\[
u = 1 - (1 - x)(1 - a).
\]

We can rewrite \(v\) in (6) in a slightly different form as

\[
v = \frac{P\{N(k - 1) = B|N(k) = G\} P\{N(k) = G\}}{P\{N(k - 1) = B\}}.
\]

The solution of (5) can be combined with (8) to obtain \(v\) as

\[
v = \frac{u\pi_0}{1 - \pi_0}.
\]

The Markov process specified by (7) and (9) characterizes the status of a single neighbor node. In step 2, we propose an iterative approach to reduce a cooperation group with multiple neighbor nodes to an equivalent cooperation group with only one super neighbor node. Let \(M \geq 2\) be the total number of neighbor nodes. In the first iteration, we combine neighbor nodes 1 and 2 into one equivalent node. After that, the resulting equivalent node is combined with node 3, and so on, until all the \(M\) neighbor nodes are combined together to form a single super neighbor node.

Let \(N^{(1)}(k)\) and \(N^{(2)}(k)\) be the states of neighbor nodes 1 and 2 at time instant \(k\), respectively. Since a retransmission will succeed if at least one of the neighbor nodes or the sender node can successfully deliver the frame to the receiver node, the combined cooperative node model for nodes 1 and 2, denoted by \(N^{(1,2)}(k)\), can be represented by

\[
N^{(1,2)}(k) = \begin{cases} 
G, & \text{if } N^{(1)}(k) = G \text{ or } N^{(2)}(k) = G \\
B, & \text{otherwise}
\end{cases}
\]

The discrete random process \(N^{(1,2)}(k)\) as specified by (10) can be modeled by a two-state Markov process, whose parameters are defined by

\[
u^{(1,2)} \triangleq P\{N^{(1,2)}(k) = B|N^{(1,2)}(k - 1) = G\}
\]

\[
u^{(1,2)} \triangleq P\{N^{(1,2)}(k) = G|N^{(1,2)}(k - 1) = B\}.
\]

Let \((u_1, v_1)\) and \((u_2, v_2)\) be the corresponding Markov parameters of \(N^{(1)}(k)\) and \(N^{(2)}(k)\), respectively. As explained in step 1, \((u_1, v_1)\) and \((u_2, v_2)\) can be computed by (7) and (9) for nodes 1 and 2, respectively. The status of \(\{N^{(1)}(k), N^{(2)}(k)\}\) can be described by another four-state Markov process, as shown in Fig. 8.

From Fig. 8 and (11), it can be easily seen that

\[
u^{(1,2)} = 1 - (1 - v_1)(1 - v_2).
\]
Using (12), we can obtain $u^{(1,2)}$ as

$$u^{(1,2)} = P\left\{ N^{(1,2)}(k - 1) = G | N^{(1,2)}(k) = B \right\} \frac{P\left\{ N^{(1,2)}(k) = B \right\}}{P\left\{ N^{(1,2)}(k - 1) = G \right\}} = \frac{v^{(1,2)} \pi_3}{1 - \pi_3}$$  \hspace{1cm} (13)$$

where $[\pi_0 \hspace{.5cm} \pi_1 \hspace{.5cm} \pi_2 \hspace{.5cm} \pi_3]$ can be obtained by solving (5) in Fig. 8.

In the next iteration, the two-state Markov model specified by $(u^{(1,2)}, v^{(1,2)})$ is combined with the two-state Markov model of neighbor node 3, which is specified by $(u_3, v_3)$. The combination process follows the same steps that we used to combine neighbor nodes 1 and 2. This process is repeated until all the neighbor nodes in the cooperation group are considered. Finally, we obtain a two-state Markov model for the super neighbor node, which includes the impacts of all neighbor
nodes. We denote the status of the super neighbor node by\
$N^{(1,...,M)}(k)$ and use the following notations for its transition\
probabilities:

\[
U = \mu^{(1,...,M)}\
\Delta = \mathbb{P}\{N^{(1,...,M)}(k) = B|N^{(1,...,M)}(k-1) = G\}\
V = \nu^{(1,...,M)}\
\Delta = \mathbb{P}\{N^{(1,...,M)}(k) = G|N^{(1,...,M)}(k-1) = B\}. \quad (14)
\]

In step 3, we model the transmission and retransmission
processes of the NCSW ARQ scheme with one sender node,
one receiver node, and one super neighbor node. Let $O(k)$
denote the state of the NCSW protocol at time instant $k$. $O(k)$
is either in transmission (T) state or retransmission (R) state
according to the two-state Markov model shown in Fig. 9.

The parameters of this Markov model are defined as

\[
X \triangleq \mathbb{P}\{O(k) = R|O(k-1) = T\}\
Y \triangleq \mathbb{P}\{O(k) = T|O(k-1) = R\}. \quad (15)
\]

In state T, the sender transmits a new frame. However, in state
R, all nodes in the cooperation group retransmit the previously
failed frame. Let $PC(k)$ represent the state of the primary
channel at time instant $k$; $O(k)$ will transit between the T and
R states according to the logic given by Table I. This table
specifies the transition logic for an eight-state Markov model,
as shown in Fig. 10. The corresponding transition probability
matrix $B(8 \times 8)$ is given by

\[
B = \begin{bmatrix}
0 & 0 & 0 & 0 & rV & qV & qV & rV \\
0 & 0 & 0 & 0 & rU & qU & qU & rU \\
qV & qV & qV & 0 & 0 & 0 & 0 & 0 \\
qu & qU & qU & 0 & 0 & 0 & 0 & 0 \\
rU & rU & rU & 0 & 0 & 0 & 0 & 0 \\
qV & qV & qV & 0 & 0 & 0 & 0 & 0 \\
qu & qu & qu & 0 & 0 & 0 & 0 & 0
\end{bmatrix} \quad (16)
\]

where $q$ and $r$ are parameters of the Markov model for the primary
channel, and $(\cdot) = 1 - (\cdot)$. Let $P = [p_{S0}, \ldots, p_{S7}]$ denote
the steady-state-probability vector, where $p_{S_i}$ is the steady-state
probability of being in state $S_i$ in Fig. 10. This vector can be
obtained by solving a set of linear equations given by

\[
P \cdot B = P
\]

\[
p_{S0} + \ldots + p_{S7} = 1. \quad (17)
\]

Having $p_{S_i}$, for $i = 0, \ldots, 7$, and Table I, the parameters of
the two-state Markov model for the NCSW protocol can be
obtained by

\[
X = \frac{p_{S2} + p_{S3}}{p_{S0} + p_{S1} + p_{S2} + p_{S3}}
\]

\[
Y = \frac{p_{S4} + p_{S5} + p_{S6}}{p_{S4} + p_{S5} + p_{S6} + p_{S7}}. \quad (18)
\]

Equation (18) completes the modeling of a frame success/failure
process as a two-state Markov model. Given this model
for the NCSW ARQ scheme and (3), the throughput of the NCSW scheme can be obtained as
\[
\eta_{\text{NCSW}} = \frac{Y}{Y + X}.
\] (19)

In the following section, we use (18) to obtain the average delay and the delay jitter of the NCSW ARQ scheme.

### B. Delay Analysis

The transmission of large frames over a wireless channel is not efficient due to the high probability of frame error [18]. As shown in Fig. 11, large data blocks from the upper layers of the communication-protocol stack (i.e., network layer) are usually broken into smaller fragments to avoid retransmissions of large frames in case of transmission errors. This technique is called packet fragmentation and has been adopted by some existing standards, such as the IEEE 802.11 Medium Access Control (MAC) protocol.

Usually, a sender node is allowed to capture the channel to continuously transmit all fragments of a single packet. Even in a contention-based MAC protocol, the contention mechanism is designed to allow a node to transmit all the fragments as a burst before the next contention period begins. For example, in the IEEE 802.11 MAC protocol as illustrated in Fig. 12, the interframe spacing mechanism is designed to allow a sender to send a sequence of fragments without any interruption. We define an ARQ protocol delay as the time required to complete the transmission of all the fragments of a single packet from the network layer. Since we do not deal with any resource allocation problem in this paper, our delay analysis does not consider the queuing delay. Thus, the transmission delay of an allocation problem in this paper, our delay analysis does not consider the queuing delay. Thus, the transmission delay of an

Next, we introduce a Markov chain with an absorbing state in order to obtain the delay jitter for the NCSW scheme. Let \((q, r)\) be the parameters of the two-state Markov model in Fig. 9 (we replace \([X, Y]\) with \([q, r]\) to simplify the notations). The transmission process of a single fragmented packet can be described by a \((2n_p + 1)\)-state Markov chain with an absorbing state, as shown in Fig. 13.

At the beginning, the system is in \(S_{n_p,T}\) where there are \(n_p\) fragments in the transmission queue. If the first transmission succeeds, the system moves to state \(S_{(n_p-1), T}\); otherwise, it will move to state \(S_{(n_p-1), R}\), where it retransmits the first fragment. This transition rule applies to all states, until the system moves into the absorbing state \(S_{0,T}\), where all fragments of the packet in the transmission queue have been transmitted successfully. In order to make the mathematical manipulations simple, as shown in Fig. 13, we assign integer indices from 0 to \(2n_p\), to the system states. The initial and the absorbing states are given index numbers \(2n_p\) and 0, respectively. All \(S_{x,R}\) states are given odd numbers, and the \(S_{x,T}\) states are assigned even numbers from 2 to \(2n_p\). The \((2n_p+1)\times (2n_p+1)\) state transition probability matrix \((\Pi)\) is given in (21), where the \((i,j)\) element denoted by \(p_{ij}\) is the probability of transition from state \(i\) to state \(j\), \(\bar{r} = 1 - r\) and \(\bar{q} = 1 - q\).

\[
\Pi = \begin{bmatrix}
1 & 0 & 0 & 0 & \cdots & 0 & 0 & 0 & 0 \\
\bar{r} & \bar{r} & 0 & 0 & \cdots & 0 & 0 & 0 & 0 \\
\bar{q} & 0 & 0 & \cdots & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & r & \bar{r} & \cdots & 0 & 0 & 0 & 0 \\
0 & 0 & \bar{q} & q & \cdots & 0 & 0 & 0 & 0 \\
\vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \vdots & \vdots \\
0 & 0 & 0 & 0 & \cdots & r & \bar{r} & 0 \\
0 & 0 & 0 & 0 & \cdots & 0 & \bar{q} & q & 0
\end{bmatrix}.
\] (21)

This matrix has the structure of

\[
\Pi = \begin{bmatrix}
I & 0 \\
V & W
\end{bmatrix}
\]

where \(I\) is a \(1 \times 1\) identity matrix, \(W\) is a \(2n_p \times 2n_p\) matrix containing the probabilities of transition among nonabsorbing states, \(V\) is a \(2n_p \times 1\) matrix that represents the probabilities of transition from the nonabsorbing states to the absorbing state \(S_{0,T}\), and \(0\) is a \(1 \times 2n_p\) zero matrix.

Let \(D_t\) be a random variable representing the number of transitions from a nonabsorbing state \(i\) to the absorbing state in Fig. 13. We show in the Appendix that the delay jitter of the NCSW scheme can be given as

\[
\sigma_p = T_I \cdot \sqrt{\frac{\delta^2_{2n_p} - d^2_{2n_p}}{E[D_{2n_p}]}}
\] (22)

where \(\delta^2_{2n_p} \triangleq E[D^2_{2n_p}]\) and \(d_{2n_p} \triangleq E[D_{2n_p}]\).

### IV. Simulation Results

We simulate a single-hop ad hoc network with one pair of sender–receiver nodes and a varying number of neighbor nodes, as shown in Fig. 2. The channels among the nodes...
The quality of the channel is represented in terms of the ratio of the fading margin over the mean value of the fading envelope as

$$L = \frac{\sqrt{\gamma}}{E[|\zeta(t)|]}.$$  \hspace{1cm} (23)

The mean value of the fading channels is normalized to a unit; thus, $L = \sqrt{\gamma}$. In other words, variations in the values of the fading margin are translated to the variations in the channel quality. As illustrated in Fig. 14, if the value of the fading margin is increased, the channel quality will be below the threshold value more frequently. This means that as the value of the fading margin is increased, there will be more frame errors, which translates to poorer channel quality.

are generated by the Rayleigh fading model. The impacts of path loss and shadowing are not considered due to their very slow variations compared with the activities of a link layer. The Rayleigh fading channels are simulated by low-pass finite impulse response (FIR) filtering of two white Gaussian random processes. The simulation parameters for the fading channels are given in Table II.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Carrier frequency</td>
<td>2400 MHz</td>
</tr>
<tr>
<td>Relative speed of mobile nodes</td>
<td>5 Km/h</td>
</tr>
<tr>
<td>Sampling frequency</td>
<td>8000 samples per second</td>
</tr>
<tr>
<td>Frame duration</td>
<td>5 ms</td>
</tr>
</tbody>
</table>
The data frame duration is set to be 5 ms, which is reasonable for many wireless data networks. A perfect ACK/NAK information on the feedback channels is assumed to be available for the whole cooperation group right after a frame transmission.

In the following sections, we present both the simulation and analytical results for the throughput, the average delay, and the delay jitter of the NCSW scheme.

A. Throughput

To observe the impact of a small number of cooperative nodes on the system throughput, the SW and the NCSW schemes with only two neighbor nodes are simulated. The throughput values of both schemes are obtained from simulations and analyses. As shown in Fig. 15, the results are plotted against the variations of the quality of the primary channel denoted by $L_p$. The quality of all interim and relay channels are assumed to be identical and denoted by $L_r$. To demonstrate the impact of the variations in the quality of the interim/relay channels, the throughput of the NCSW protocol is plotted for two different values of $L_r$, namely, $-5$ and $-1$ dB.

The results in Fig. 15 show that, with cooperation of only two neighbor nodes, the throughput of the NCSW scheme can be improved up to 30%, depending on the quality of the interim/relay channels. A comparison of the analytical and the simulation results also demonstrates the accuracy of the proposed analytical model for the system throughput.

To investigate the impact of the number of neighbor nodes on the protocol throughput, the fading margin of the primary channel is set to $L_p = -1$ dB. At this relatively low quality of the primary channel, we can clearly observe the impact of the number of neighbor nodes on the system throughput. Simulations are performed for two different fading margins for the relay/interim channels, namely $L_r = -5$ dB and $L_r = -1$ dB.

As shown in Fig. 16, when the number of the cooperative nodes increases, the system throughput approaches a saturation level depending on the quality of the primary and the interim/relay channels. If the qualities of the interim/relay channels are good, having only one or two neighbor nodes can significantly improve the system performance; however, when the qualities of the interim/relay channels are poor, more neighbor nodes are required to achieve the same level of performance gain. Saturation of the system throughput is also expected. In fact, regardless of the number of neighbor nodes or their channel qualities, individual frame errors cannot be avoided. However, cooperation of the neighbor nodes can reduce the duration of error bursts.

Another important issue is to separately investigate the impacts of variations in the quality of the interim and the relay channels. The results of this analysis can be helpful in deciding when a node should cooperate. Such a decision can be based on the average quality of the channels from the sender and to the receiver nodes. To keep the system setup consistent with the previous simulations, we obtain the system throughput for only 2 neighbor nodes. We set the fading margin of the primary channel at a fixed level of $L_p = -1$ dB and let the fading margin of the relay channels $L_{\text{relay}}$ at a fixed level of $-5$ dB and let
the fading margin of the interim channels $L_{\text{interim}}$ vary from $-5$ to 0 dB. In the second run, for a fixed fading margin of the interim channels at $-5$ dB, we let the fading margin of the relay channels vary from $-5$ to 0 dB. As shown in Fig. 17, the system throughput follows the same form of variations against the quality of the relay and the interim channels.

B. Average Delay and Delay Jitter

We simulate the SW and the NCSW protocols with only two cooperating neighbor nodes for our delay analysis. For the NCSW scheme, we assume moderate interim and relay channel qualities at a fading margin of $-2.5$ dB. The other channel parameters are the same as in Table II. The fading margin for the primary channel is varied from $-5$ dB (good channel quality) to 0 dB (bad channel quality). Packets from the upper layer, i.e., network layer, are fragmented into 20 frames of 5-ms durations (including ACK/NAK); therefore, if there is no transmission error, it will take 100 ms for all the fragments of a single packet to be transmitted. However, as shown in Fig. 18, on the average, it will require more than 100 ms due to frame errors. As shown in the figure, for a small number of cooperative nodes with moderate interim/relay channel qualities, the NCSW protocol significantly outperforms the SW protocol in terms of transmission delay. For example, when the primary channel is poor ($L_p = 0$ dB), the average delay for the SW scheme is about 265 ms; however, for the same channel condition, the NCSW protocol can reduce the average delay to 160 ms. Thus, due to node cooperation, the average delay is reduced by 60% when the primary link is experiencing a poor condition.

With the same simulation setup, we also investigate the delay jitter caused by the transmission errors in both schemes. Again, by comparing the results given in Fig. 19, we observe a significant improvement in the performance in terms of reduced delay jitter. For example, when the primary channel is in a poor condition, the delay jitter is reduced from 140 to 20 ms, which is equivalent to an 85% reduction. Furthermore, the exponential growth in the delay jitter is reduced to a slow linear growth. The improvement of the delay jitter is more remarkable than that of the delay and the throughput. Intuitively, since node cooperation reduces the negative impact of long and varying error bursts, this significant improvement in the jitter is expected. This is a very important advantage of the proposed scheme for real-time multimedia applications, such as voice over Internet protocol (IP), where reducing the delay jitter is a challenging task in providing the desired quality of service.

V. Conclusion

We have proposed an NCSW ARQ scheme for wireless ad hoc networks. We developed analytical models for the retransmission process and its tangible performance metrics, such as throughput, average delay, and delay jitter. Simulation results were also given to demonstrate the performance gain and to verify the analytical models. It is concluded that node cooperation can significantly improve the performance of ARQ protocols in wireless ad hoc networks. For example, when
approximately 50% of the frames become erroneous due to poor channel condition between the sender and the receiver nodes, the throughput can be improved by up to 30% with only two cooperating nodes with moderate channel qualities. Meanwhile, the average transmission delay can be reduced by 60%, and the average-delay jitter can be decreased by 85%. The remarkable gains in the average-delay and delay-jitter performance are of significant importance for real-time multimedia applications.

Our future research includes the study of the impact of different coding and signal processing techniques at the physical layer and integration issues with the existing MAC protocols, such as the standard IEEE 802.11 MAC protocol.

**APPENDIX**

**DERIVATION OF DELAY JITTER**

Delay jitter is the standard deviation of the packet transmission delay, which is defined as

$$\sigma_p \triangleq \sqrt{E[(T_p - t_p)^2]}.$$  \hspace{1cm} (24)

We can rewrite (24) as

$$\sigma_p^2 = E[(D_p - d_p)^2] \cdot T_i^2.$$  \hspace{1cm} (25)

Since

$$E[(D_i - d_i)^2] = E[D_i^2] - d_i^2$$  \hspace{1cm} (26)

we need to obtain $\delta_i^2 = E[D_i^2].$

Let $d_j$ denote the mean value of $D_j$ as the average number of steps required to move from a nonabsorbing state $j$ to the absorbing state in Fig. 13. Starting from a nonabsorbing state $j$, the system either moves to the absorbing state in one step or gets to the absorbing state via one or more nonabsorbing states. The probability of the first event is

$$P\{\text{go to the absorbing state in one step} \mid \text{current state is } j\} = p_{j0}.$$  

The probability of the second event is

$$P\{\text{go to a nonabsorbing state} \mid \text{current state is } j\} = \sum_{i=1}^{2n_p} p_{ji}.$$  

If the latter case happens, the time of absorption is $(1 + D_i)$. Thus, we have

$$D_j = 1 \times p_{j0} + \sum_{i=1}^{2n_p} p_{ji}(1 + D_i)$$  

and $\delta_i^2$ is given by

$$\delta_i^2 = p_{j0} + \sum_{i=1}^{2n_p} E[(1 + D_i)^2] p_{ji} = p_{j0} + \sum_{i=1}^{2n_p} (1 + 2d_i + \delta_i^2) p_{ji} = p_{j0} + \sum_{i=1}^{2n_p} d_ip_{ji} + \sum_{i=1}^{2n_p} \delta_i^2 p_{ji}$$

$$= 1 + \sum_{i=1}^{2n_p} d_ip_{ji} + \sum_{i=1}^{2n_p} \delta_i^2 p_{ji}.$$  \hspace{1cm} (27)

Organizing (27) into a matrix form, we have

$$\begin{bmatrix} \delta_1^2 \\ \delta_2^2 \\ \vdots \\ \delta_{2n_p}^2 \\ \delta_{2n_p-1}^2 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ \vdots \\ 1 \\ 1 \end{bmatrix} + 2W \begin{bmatrix} d_1 \\ d_2 \\ \vdots \\ d_{2n_p-1} \\ d_{2n_p} \end{bmatrix} + W \begin{bmatrix} \delta_1^2 \\ \delta_2^2 \\ \vdots \\ \delta_{2n_p}^2 \end{bmatrix},$$  \hspace{1cm} (28)

$$= (I - W)^{-1} \begin{bmatrix} 1 \\ 1 \\ \vdots \\ 1 \end{bmatrix} + 2(I - W)^{-1}W \begin{bmatrix} d_1 \\ d_2 \\ \vdots \\ d_{2n_p-1} \\ d_{2n_p} \end{bmatrix}.$$  \hspace{1cm} (29)

Combining (25), (26), and (29), $\sigma_p^2$ can be obtained as

$$\sigma_p^2 = T_i \cdot \sqrt{\delta_{2n_p}^2 - d_{2n_p}^2}.$$  \hspace{1cm} (30)

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**REFERENCES**


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