High-spin spectroscopy of natural and unnatural parity states in the mirror-pair $^{45}$V/$^{45}$Ti

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(Received 28 September 2005; published 8 February 2006)

High-spin states in the proton-rich nucleus $^{45}$V have been identified for the first time. A comprehensive $γ$-ray decay scheme has been established following an experiment performed at the Vivitron accelerator at IReS Strasbourg by using the Euroball $γ$-ray detector array coupled to the Neutron Wall and Euclides detector arrays. The natural (negative-)parity scheme is identified up to the $T_z = \pm 2$ band termination in addition to a positive-parity collective structure based on a $d_{5/2}$ particle-hole excitation. Comparison of this scheme with that of the mirror partner, $^{45}$Ti, has yielded detailed information on the variation of Coulomb energy as a function of excitation energy and angular momentum. This is the first time that such an analysis has been performed for a collective structure built on a cross-shell excitation. Comparison of the observed Coulomb energies with those predicted by large-scale shell-model calculations is presented. In this case, unusually, the calculations do not fare as well as for heavier nuclei in the shell. In addition, stark differences between the two nuclei are observed for the decay intensities of the parity-changing E1 decays that de-excite the positive-parity deformed bands.

DOI: 10.1103/PhysRevC.73.024304 PACS number(s): 21.10.Hw, 23.20.Lv, 27.40.+z, 21.10.Sf

I. INTRODUCTION

One of the most fundamental symmetries in Nature is the exchange symmetry between neutrons and protons in the nucleus, which reflects the approximate charge symmetry and charge independence of the attractive nucleon-nucleon interaction. Although it is now known [see, e.g. (1)] that these two symmetries are only approximate, they retain enough validity to result in startling symmetries in nuclear behavior, which can be readily observed in the study of isobaric triplets. These symmetries lead naturally to the use of the isospin quantum number, $T$, one of the most powerful and elegant concepts in nuclear physics. States of the same isospin in a mass multiplet (i.e., isobaric analog states, IAS) will be degenerate if electromagnetic effects are ignored and if charge symmetry and/or change independence are assumed. Of course, in nuclei, the Coulomb force between protons breaks the symmetry and lifts the degeneracy of the IAS. The simplest case to consider is that of a pair of mirror nuclei ($A$, $B$) with $T_z = (N - Z)/2 = \pm \frac{1}{2}$ such that $Z_A = N_A + 1 = N_B$ and $Z_B = N_B - 1 = N_A$. The $T_z = \pm \frac{1}{2}$ pair discussed here, $^{45}$V/$^{45}$Ti, is one such example. In such mirror pairs the energy difference between excited states—termed the mirror energy differences, MED—can be established through modern spectroscopic techniques and can yield direct information on Coulomb effects if the charge symmetry of the strong nuclear force is assumed.

Over the past decade, advances in experimental techniques—specifically the development of large $γ$-ray spectrometers coupled to sensitive channel-selection devices—have afforded the opportunity to study proton-rich nuclei in detail up to $A \approx 60$. In the $f_{7/2}$ shell between $^{40}$Ca and $^{56}$Ni, this has allowed the detailed spectroscopy of essentially all the $T_z = \pm \frac{1}{2}$ mirror pairs [2–11] and the even-$A$ $T_z = 1$ isobaric triplets [12–18]. In all of these cases, the energy differences between excited states have been extracted and interpreted in terms of Coulomb effects. One of the real surprises is that the quantitative analysis of Coulomb energies by this approach has yielded far more reliable and subtle information on nuclear structure phenomena than had been previously supposed. It is particularly surprising given the long-established Nolen-Schiffer anomaly [19], which refers to the large discrepancy consistently found when attempting
to reproduce the binding energy differences of the ground states of mirror nuclei. A key advantage of performing these studies in the $f_{7/2}$ shell comes from the development of the large-scale pf-shell-model calculations, based on the code described in Ref. [20], that are available in this mass region and that have been shown to be extremely reliable. The work on isobaric analog nuclei has prompted modifications to the shell-model calculations to include both multipole (e.g. [7]) and monopole (e.g. [15, 21]) Coulomb terms. Thus this work provides an extremely stringent test of this important model and, conversely, the reliability of the model provides a valuable tool in the interpretation of the measured Coulomb energies.

The relative isolation of the $f_{7/2}$ shell from other major orbits results in yrast structures whose state wave functions are dominated by pure $(f_{7/2})^n$ configurations (e.g. [22]), where $n$ is the number of $f_{7/2}$ particles outside $^{40}\text{Ca}$. This, in turn, means that the evolution of Coulomb energies along the yrast line can be interpreted consistently without significant changes in configuration. It has now been demonstrated both experimentally (e.g. [2, 6, 7, 10]) and theoretically (e.g. [8, 15, 21]) that the largest angular-momentum-dependent effect on the Coulomb energy in this mass region arises from the recoupling of pairs of $f_{7/2}$ protons from $J = 0$ to $J = 6$. In addition, it has been possible to relate smaller variations in the MED to other specific spin-dependent phenomena, such as changes in radius and/or deformation as a function of spin [7, 15, 21].

To date, all the analysis of MED for nuclei in the $f_{7/2}$ shell has been restricted to the natural parity structures dominated by $(f_{7/2})^n$ configurations. However, nonyrast unnatural parity states, which are based on one-particle-one-hole excitations from the $d_{3/2}$ orbital below $^{40}\text{Ca}$, are common in this region. The Nilsson diagrams in the region show that particle-hole excitations from $d_{3/2}$ are expected to have a prolate deformation-driving effect. The resulting strongly coupled deformed collective structures built on low-lying $J^\pi = \frac{1}{2}^+$ states have been established in a number of light $f_{7/2}$ cases, such as the $T_e = +\frac{1}{2}$ nuclei $^{47}\text{V}$ [23] and $^{49}\text{Cr}$ [24]. As yet, there has been no analysis of Coulomb effects associated with these structures through studies of the analog sequences in the less accessible $T_e = -\frac{1}{2}$ mirror partners.

In this paper we present, for the first time to our knowledge, an extensive level scheme of the $T_e = -\frac{1}{2}$ nucleus $^{45}\text{V}$. Before this work some low-lying states of both parities had been identified by Gronemeyer et al. [25]. The current work identifies the negative-parity yrast structure up to the $f_{7/2}$ band-termination state. In addition, the positive-parity structure based on the $d_{3/2}$ particle-hole excitation is extended up to high spins. MED have been established, and a detailed analysis of the Coulomb effects for both structures is presented and supported by the predictions of the large-scale shell-model calculations. In addition, we show evidence for an anomaly in the comparison of the $\gamma$-ray intensities depopulating the positive-parity structures.

II. EXPERIMENTAL DETAILS

The experiment was performed by using the Vivitron accelerator at IReS Strasbourg. A $^{24}\text{Mg}$ beam was accelerated to 83 MeV and impinged on a 500 $\mu\text{g/cm}^2$ $^{24}\text{Mg}$ self-supporting target. The $T_e = \pm\frac{1}{2}$ mirror pair, $^{45}\text{V}$ and $^{45}\text{Ti}$, were then produced in a fusion-evaporation reaction through the $1p2n$ and $2p1n$ evaporation channels, respectively. Gamma rays from the reaction were detected in the Euroball array [26, 27] which, at the time, consisted of 26 Clover detectors and 15 Cluster detectors, each containing 4 or 7 individual hyperpure Ge crystals, respectively—a total of 209 individual detector elements. Each individual Clover and Cluster detector unit was Compton suppressed, and within each unit $\gamma$-ray add-back routines were applied to increase the total photopeak efficiency of the array for high-energy transitions.

The predicted cross section for $^{35}\text{V}$ is expected to be of the order of 1 mb—around 100 times smaller than that of the mirror nucleus $^{45}\text{Ti}$. Given this, and the near-identicality of the $\gamma$-ray transitions expected for the mirror pair, additional and unambiguous channel selection was necessary. To achieve this, the evaporated particles were recorded in two ancillary devices. The Euclides array [28] was used to record protons and alpha particles emitted in the reaction. Euclides consisted of 40 $\Delta E - E$ Si detector telescopes arranged in five rings. Each of the five detectors in the most forward ring was electrically segmented into four parts, making a total of 55 effective telescopes in the whole array. Two-dimensional gates on the individual $\Delta E - E$ plots were used to discriminate between emitted alpha particles and protons. Of particular importance in this experiment is the identification of the number of neutrons emitted. For this purpose, the Euroball Neutron Wall [29] was used, which consisted of 50 individual detectors, containing BC501A liquid scintillators, covering a solid angle of $\approx1\pi$ at forward angles and located at an average distance of $\approx0.5\text{ m}$ from the target position. Discrimination between $\gamma$ rays and neutrons was achieved by using a combination of time-of-flight (TOF) and pulse-shape discrimination, the latter utilizing the zero-crossover time (ZCO) of a bipolar amplified pulse. Discrimination was therefore achieved by using two-dimensional gates on individual TOF-ZCO matrices. For this reaction and analysis procedure, the total efficiency for single-neutron detection with this array was found to be 15%. The experimental trigger was defined when one neutron had been detected. The Euclides data was not specifically included in the trigger.

In the offline analysis the energy and angle information from the Euclides and Neutron Wall detector elements for each evaporated particle were used to perform a kinematic reconstruction of each event. This allowed the recoil vector of the final nucleus to be determined, permitting a more accurate $\gamma$-ray Doppler correction. This then reduces the Doppler broadening arising from the recoil cone.

III. DATA ANALYSIS AND RESULTS

In an attempt to unambiguously assign $\gamma$ rays to the weak reaction channel of interest, $^{45}\text{V}$, singles $\gamma$-ray spectra were generated in coincidence with different combinations of evaporated particles. One such spectrum is found in Fig. 1(a), which
FIG. 1. Singles $\gamma$-ray spectra created with different conditions placed on the Euclides and Neutron Wall detectors. (a) Spectrum recorded when two protons and one neutron were detected. The numerically labeled peaks all originate from $^{45}$Ti (the $2p1n$ channel) and those labeled with the filled squares correspond to $^{44}$Sc—the $3p1n$ channel. The $2p2n$ channel ($^{44}$Ti) is also present, but too weak to be labeled. (b) Spectrum recorded when two neutrons were detected. The labeling scheme is the same as (a). (c) Same spectrum as (b), but having also applied the nearest-neighbor rejection procedure (see text). The peaks labeled with filled diamonds originate from the $2p2n$ channel, $^{44}$Ti. (d) The clean two-neutron-gated spectrum. The same as (c) but with an additional time-of-flight analysis applied (see text). The numerically labeled transitions are assigned to $^{45}$V.

shows $\gamma$ rays recorded in coincidence with two protons and one neutron. As expected, the $2p1n$ channel $^{45}$Ti dominates, with all the labeled peaks corresponding to known [30] transitions in $^{45}$Ti. Also present, and marked in this spectrum, are transitions from the $3p1n$ channel, $^{44}$Sc, where one of the three protons emitted was not detected by the Euclides array. To produce a similar spectrum for $^{45}$V, the $1p2n$ channel, a $2n$-gated spectrum was produced (gating on the proton is not helpful, as all major channels have at least one proton emitted). This spectrum, requiring that two separate neutron detectors record a neutron, is shown in Fig. 1(b). As can be seen, the spectrum is virtually identical to the $2p1n$-gated spectrum of Fig. 1(a). This is because when two neutron detectors record neutrons in most cases this corresponds to one scattered neutron recorded twice. To alleviate this, a nearest-neighbor-rejection procedure was employed. In this method, particular pair combinations were rejected based on their physical proximity. To determine the acceptable separation of detectors, a correlation analysis
was performed in which the coincidence frequency of each pair of detectors was analysed. Specific pair combinations were rejected if the coincidence frequency was above a certain level. The spectrum resulting from this procedure is shown in Fig. 1(c). Although some of the $^{45}$V remains, the spectrum is now dominated by the $2p$-$2n$ channel $^{44}$Ti—the strongest of the $2n$ channels.

To identify the $^{45}$V transitions, the remainder of the scattered $1n$ events need to be removed. This was achieved by an additional time-of-flight (TOF) analysis suggested by Ljungvall et al. [31], where the difference in TOF between the two neutrons in the $2n$ event is analyzed. For genuine $2n$ events the TOF should be approximately the same for each neutron, and the TOF difference should be zero. For scattered $1n$ events, now that near-neighbor coincidences have been removed, the TOF difference should be nonzero. This can clearly be seen in Fig. 2(a), where the TOF difference is shown for all $2n$ events (i.e., mostly scattered $1n$ events) and for events where the nearest-neighbor-rejection analysis has been applied (i.e., mostly real $2n$ events). The final pure $2n$ spectrum was produced by gating on the central region of the TOF-difference spectrum, with appropriate background subtractions. The result is shown in Fig. 1(d). Close examination of the spectrum shows that all of the $1n$ transitions have been removed. For example, the insets in Fig. 1(a) to 1(c) all show the strong 586 keV transition in $^{45}$Ti, which is completely gone in the inset of Fig. 1(d). Thus we can be confident that only genuine $2n$ events remain.

Figure 1(d) is, as expected, dominated by transitions from the $2p$-$2n$ channel, $^{44}$Ti, but should also contain the transitions from $^{45}$V. From the work of Gronemeyer et al. [25], a few low-lying states and $\gamma$ transitions had previously been identified. The only known natural parity states were two nonyrast states with $J^\pi = \frac{3}{2}^-$ and $\frac{5}{2}^-$, in addition to the $J^\pi = \frac{7}{2}^-$ ground state. The $J^\pi = \frac{3}{2}^+, \frac{5}{2}^+$ and $\frac{7}{2}^+$ members of the band built on the $d_{3/2}$ intruder level had also been identified. The 329 and 411 keV decays from the $\frac{3}{2}^+$ and $\frac{5}{2}^+$ states, respectively, can be seen in Fig. 1(d). In addition to these, and the well-known transitions in $^{44}$Ti, a number of other peaks can be identified that have energies very close to those in $^{45}$Ti, and these we assign to $^{45}$V. Each of the labeled transitions in the $^{45}$Ti spectrum in Fig. 1(a) has a corresponding (mirrored) transition in $^{45}$V, which is marked in Fig. 1(d). The strongest suggested $^{45}$V transition is the 600 keV transition, presumed to be the mirror of the 586 keV $J^\pi = \frac{17}{2}^- \rightarrow \frac{15}{2}^-$ transition in $^{45}$Ti. Figure 2(b) shows the TOF-difference spectrum for these two transitions. Comparison with Fig. 2(a) clearly shows that the 600 keV transition is associated with the emission of two neutrons.

Figure 3 shows the level schemes of the $A = 45$ mirror pair, on the left-hand side of which is the scheme of $^{45}$V deduced from this work. On the right-hand side is shown a portion of the $^{45}$Ti level scheme, based on the comprehensive published level schemes of Bednarczyk et al. [30,32]. The current work confirms the published schemes. The placement and ordering of the $\gamma$ rays in the new scheme for $^{45}$V was achieved through a detailed 2D and 3D $\gamma$-ray analysis, described below. Owing to the very close proximity of the $\gamma$ rays of the transitions in the mirror pair, production of clean $\gamma$-ray gated spectra for $^{45}$V was extremely difficult, with only the 329 keV transition providing a clean gate. In addition, the low beam intensity ($\lesssim 1$ pnA) of the difficult $^{24}$Mg beam, coupled with the low cross section for production of $^{45}$V, limited the statistics obtained. Thus, a clean two-neutron-gated $\gamma$-$\gamma$ analysis was not possible. These issues conspired to such an extent that an angular correlation analysis was not possible in this case. However, given that the placement of the $\gamma$ rays in the scheme has been confirmed through a $\gamma$-ray coincidence analysis (see below), we can confidently assign the multipolarities of the $\gamma$ rays, and hence the spins and parities of the states, by mirror symmetry arguments based on comparison with the well-known [30] $^{45}$Ti scheme. There is no evidence to date that suggests that this method is not completely reliable, and we therefore quote the spins and parities as unambiguous assignments, based on the well-established assignments of the analog states in the mirror partner $^{45}$Ti [30]. The measured energies and intensities of the $\gamma$ rays, and the state energy, spin, and parity assignments are listed in Table I. The remarkable similarity in the decay intensities of the states (with one notable exception, which will be discussed later) can be seen in the table.

No $\gamma$ decays in the yrast $f_{7/2}$ (negative parity) band in $^{45}$V have been observed previously. The members of this band were identified first in Fig. 1(d) by comparison with known transitions in $^{44}$Ti and then confirmed through $\gamma$-ray coincidence analysis. In this way the structure shown in Fig. 3 up to the $J^\pi = \frac{27}{2}^-$ band-termination state was established.
The $\gamma$-$\gamma$ coincidence (doubles) analysis was undertaken with a $\gamma$-$\gamma$ matrix incremented on the condition that at least one neutron was detected. Figures 4(a) and 4(b) show spectra generated in coincidence with the 787 keV (9/2$^-$ $\rightarrow$ 7/2$^-$) transition in $^{45}$V and the equivalent 743 keV transition in $^{45}$Ti. The symmetry between the spectra is obvious, and the sequence up to the band termination is clearly seen. A triple $\gamma$-$\gamma$ coincidence analysis was also undertaken to confirm the ordering of the $^{45}$V scheme and to reduce contamination in the spectra. Figure 5(a) shows a spectrum generated in coincidence with both the 787 keV transition and any one of the 378, 600, or 953 keV yrast-band transitions in $^{45}$V. Figure 5(b) shows the equivalent spectrum produced by using the mirrored transitions in $^{45}$Ti. Again the sequence is confirmed, and some of the weaker transitions are seen, such as those populating and de-exciting the $J^{\pi} = 9/2^-$ state (although the order of these two was not determined). It should be noted that the ratio of the intensities between the equivalent spectra for $^{45}$Ti and $^{45}$V is always around the factor of 100 expected from the relative cross sections. This can be seen clearly in Figs. 4, 5, and 6.

The positive-parity sequence in $^{45}$V is based on the $d_3/2$ $J^{\pi} = 3/2^+$ intruder band head at 386.1 keV [25]. Also observed in Ref. [25] were the $J^{\pi} = 5/2^+$ and 7/2$^+$ states of this sequence. All the other states shown in this sequence in Fig. 3 up to $J^{\pi} = 19/2^+$ are new. Gronemeyer et al. [25] identified two $E1$ transitions de-exciting the $J^{\pi} = 3/2^+$ state. These populate the nonyrast $J^{\pi} = 3/2^-$ and $J^{\pi} = 5/2^-$ states at 57.2 and 56.4 keV via 328.9 and 329.7 keV transitions. In the current work, these two cannot be distinguished, so Fig. 3 and Table I quote the measured average energy (329.1 keV), and the intensity is distributed equally between them. The same approach is taken for the 741 keV transition decaying to these two near-degenerate states from the $J^{\pi} = 5/2^+$ level (although Gronemeyer et al. show this decaying exclusively to the $J^{\pi} = 5/2^-$ state). The 1$n$-gated $\gamma$-$\gamma$ matrix was also used for a doubles analysis of this sequence of states. Figures 4(c)
and 4(d) show spectra generated in coincidence with the 329 keV transition in $^{45}$V and the 292 keV equivalent transition in $^{45}$Ti. Again, all the transitions in the sequence up to $J^\pi = 7/2^-$ are seen. This is confirmed in the triples coincidence analysis. Figure 5(c) shows a spectrum generated in coincidence with both the 329 keV transition and any of the 411, 475, 886, or 1217 keV transition in the positive-parity band in $^{45}$V. Figure 5(d) shows the equivalent spectrum produced by using the mirrored transitions in $^{45}$Ti.

An example of how weak transitions were placed in the level scheme is shown in Fig. 6, which shows double-gated spectra for the positive-parity structure. These spectra firmly place the 1776 keV transition to be the $J^\pi = 11/2^+ \rightarrow 13/2^+$ member of the sequence (and not the $J^\pi = 12^+$ to $13^+$, as mirror symmetry of transition energies might suggest). Figures 6(a) and 6(c) show spectra for $^{45}$V double-gated on both the 329 keV transition and the (a) 1217 keV or (c) 1776 keV transitions. This clearly shows that the 1217, 1421, and 1776 transitions are in sequence. The equivalent mirrored spectra for $^{45}$Ti are shown in Figs. 6(b) and 6(d).

One important result here is the obviously different intensity of the parity-changing decay(s) from the $J^\pi = 7/2^+$ state in $^{45}$V when compared with that of $^{45}$Ti. In $^{45}$Ti, this intensity is carried by the 707 keV transition to the $J^\pi = 3/2^-$ state. This is shown in the inset to Fig. 1(a) and is a weak transition in comparison with the strong 743 keV yrast transition.

### Table I. Assigned spin, parity and excitation energy for excited states and transition energy and relative intensity for $\gamma$ decays for $^{45}$V and $^{45}$Ti. Intensities are quoted relative to the strong 11/2$^-$ to 7/2$^-$ yrast transition.

<table>
<thead>
<tr>
<th>$J_i^\pi$</th>
<th>$J_f^\pi$</th>
<th>$^{45}$V</th>
<th>$E_x$ (keV)</th>
<th>$E_\gamma$(keV)</th>
<th>$I_\gamma$(%)</th>
<th>$^{45}$Ti</th>
<th>$E_x$ (keV)</th>
<th>$E_\gamma$(keV)</th>
<th>$I_\gamma$(%)</th>
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<tr>
<td>3/2$^-$</td>
<td>2/2$^-$</td>
<td>$^{45}$V</td>
<td>57.2$^a$</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>36.4$^a$</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>5/2$^-$</td>
<td>4/2$^-$</td>
<td>$^{45}$V</td>
<td>56.4$^a$</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>39.8$^a$</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>9/2$^-$</td>
<td>7/2$^-$</td>
<td>$^{45}$V</td>
<td>1324.0(5)</td>
<td>1324.0(5)</td>
<td>10(2)</td>
<td>—</td>
<td>1353.6(2)</td>
<td>1353.6(3)</td>
<td>3.6(1)</td>
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<td>9/2$^-$</td>
<td>$^{45}$V</td>
<td>1462.0(5)</td>
<td>1462.0(5)</td>
<td>100(20)</td>
<td>—</td>
<td>1468.2(2)</td>
<td>1468.2(2)</td>
<td>100(1)</td>
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<td>11/2$^-$</td>
<td>$^{45}$V</td>
<td>2625.9(7)</td>
<td>1163.9(5)</td>
<td>17(3)</td>
<td>—</td>
<td>2656.2(3)</td>
<td>1180.8(2)</td>
<td>29.6(4)</td>
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<td>13/2$^-$</td>
<td>$^{45}$V</td>
<td>3004.7(7)</td>
<td>378.0(3)</td>
<td>25(7)</td>
<td>—</td>
<td>3015.0(4)</td>
<td>358.3(2)</td>
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<td>17/2$^-$</td>
<td>15/2$^-$</td>
<td>$^{45}$V</td>
<td>3064.7(7)</td>
<td>600.1(2)</td>
<td>66(4)</td>
<td>—</td>
<td>3601.1(4)</td>
<td>586.0(2)</td>
<td>92(4)</td>
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<td>19/2$^-$</td>
<td>17/2$^-$</td>
<td>$^{45}$V</td>
<td>4391.5(6)</td>
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<td>—</td>
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<td>21/2$^-$</td>
<td>$^{45}$V</td>
<td>6206.4(11)</td>
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<td>76(6)</td>
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<td>25/2$^-$</td>
<td>$^{45}$V</td>
<td>7159.3(11)</td>
<td>952.9(3)</td>
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<td>11(2)$^b$</td>
<td>—</td>
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<td>292.1(2)</td>
<td>38(2)</td>
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<td>4/2$^+$</td>
<td>$^{45}$V</td>
<td>797.0(4)</td>
<td>410.9(4)</td>
<td>27(7)</td>
<td>—</td>
<td>742.6(3)</td>
<td>441.0(2)</td>
<td>29(1)</td>
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<tr>
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<td>6/2$^+$</td>
<td>$^{45}$V</td>
<td>1271.6(7)</td>
<td>474.7(4)</td>
<td>13(2)</td>
<td>—</td>
<td>1225.3(4)</td>
<td>482.4(2)</td>
<td>13.6(5)</td>
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<tr>
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<td>7/2$^+$</td>
<td>$^{45}$V</td>
<td>1916.5(8)</td>
<td>644.0(7)</td>
<td>5(2)</td>
<td>—</td>
<td>1880.5(4)</td>
<td>654.9(2)</td>
<td>5.6(1)</td>
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<tr>
<td>9/2$^+$</td>
<td>7/2$^+$</td>
<td>$^{45}$V</td>
<td>1916.5(8)</td>
<td>644.0(7)</td>
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<td>1880.5(4)</td>
<td>654.9(2)</td>
<td>5.6(1)</td>
</tr>
<tr>
<td>11/2$^+$</td>
<td>9/2$^+$</td>
<td>$^{45}$V</td>
<td>2488.9(9)</td>
<td>572.8(7)</td>
<td>8(1)</td>
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<td>2473.2(5)</td>
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<td>7.0(1)</td>
</tr>
<tr>
<td>13/2$^+$</td>
<td>11/2$^+$</td>
<td>$^{45}$V</td>
<td>3444.2(13)</td>
<td>1528(1)</td>
<td>&lt;3</td>
<td>—</td>
<td>3446.0(5)</td>
<td>972.6(2)</td>
<td>1.37(3)</td>
</tr>
<tr>
<td>15/2$^+$</td>
<td>13/2$^+$</td>
<td>$^{45}$V</td>
<td>3910.0(16)</td>
<td>465(1)</td>
<td>&lt;3</td>
<td>—</td>
<td>3921.1(5)</td>
<td>475.2(2)</td>
<td>3.7(1)</td>
</tr>
<tr>
<td>17/2$^+$</td>
<td>15/2$^+$</td>
<td>$^{45}$V</td>
<td>5685.5(17)</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>5639.4(7)</td>
<td>401.3(3)</td>
<td>1.40(6)</td>
</tr>
<tr>
<td>19/2$^+$</td>
<td>17/2$^+$</td>
<td>$^{45}$V</td>
<td>1775.5(7)</td>
<td>—</td>
<td>9(1)</td>
<td>—</td>
<td>1717.7(5)</td>
<td>10.0(2)</td>
<td></td>
</tr>
</tbody>
</table>

$^a$The excitation energies of these states were taken from the work of Gronemeyer et al. [25].

$^b$For these 329 and 741 keV transitions in $^{45}$V the final state cannot be determined in this work (see text). Thus the average $\gamma$-ray energy is recorded and the intensity split equally between the two possible decay paths.
detected and are in coincidence with (a) the 787 keV transition in \( \text{^{45}V} \), (b) its mirrored transition, 743 keV, in \( \text{^{45}Ti} \), (c) the 329 keV transition in \( \text{^{45}V} \), and (d) its mirrored transition, 292 keV, in \( \text{^{45}Ti} \). Spectra were in coincidence with (a) the 787 keV transition in \( \text{^{45}V} \), (b) its mirrored transition, 743 keV, in \( \text{^{45}Ti} \), (c) the 329 keV transition in \( \text{^{45}V} \), and (d) its mirrored transition, 292 keV, in \( \text{^{45}Ti} \).

In the inset of Fig. 1(d) the 741 keV transition decaying from the analogous state in \( \text{^{45}V} \) can be seen and is about a factor of 10 stronger (see Table I) in relative intensity. In addition to the evidence presented in Figs. 1(a) and 1(d), the large difference in relative intensity between the 707 and 741 keV analog transitions has also been confirmed in a triples analysis. Although it has not been possible to measure the proportions of the intensity flowing to the \( J^{π} = \frac{5}{2}^{−} \) and \( \frac{3}{2}^{−} \) states individually, the total intensity decaying from the \( J^{π} = \frac{5}{2}^{−} \) state is much larger in \( \text{^{45}V} \) than in \( \text{^{45}Ti} \). Indeed, if the assignment of \( J^{π} = \frac{5}{2}^{−} \rightarrow \frac{5}{2}^{−} \) for the 741 keV transition in Ref. [25] is correct, the equivalent transition in \( \text{^{45}Ti} \) is either missing or extremely weak. Due to the strength of the 707 keV transition in \( \text{^{45}Ti} \) compared with the 414 keV \( M1/E2 \) transition, strong contributions from multipoles of order 2 and higher are considered unlikely, and so we presume that this transition (and hence the mirrored 741 keV transition in \( \text{^{45}V} \)) is purely \( E1 \) in character. The other two parity-changing transitions seen to de-excite the \( J^{π} = \frac{3}{2}^{−} \) state in \( \text{^{45}Ti} \) (the 1226 and 1186 keV transitions) are of low relative intensity (see Table I). The equivalent transitions in \( \text{^{45}V} \), if it is assumed that they carry the same intensity, would not be observed in the present work.

**IV. DISCUSSION**

The different \( E1 \) intensity is of considerable interest, as relative intensities between mirror pairs have previously been observed to be almost identical. Indeed, the two other cases of anomalous decay intensities that have recently been observed—for the \( A = 35 \) mirror pair at low spin [33] and at high spin [34] and the \( A = 31 \) [35,36] mirror pair—both involve \( E1 \) transitions. In general, when considering the isospin dependence of transition strengths, it is found [37] that \( E1 \) transitions, which proceed only through an isovector component of the transition operator, should have identical strengths in mirror partners. Indeed, this is not generally true for \( E2 \) or \( M1 \) transitions—although the expected approximate similarity in wave functions between mirror partners tends to result in similar decay branching ratios and hence similar relative intensities. It is therefore noteworthy that this intensity...
anomaly has so far been observed only for $E1$ transitions—the only type of decay where the transition strengths should be equal. Ekman et al. [33] suggested that this could result from isospin mixing, to which $E1$ transitions may be particularly sensitive. Of course, the data presented so far consider only relative intensities and not transition strengths. This interpretation thus awaits measurement of transition strengths and, of course, detailed calculations.

The measured MED for the $f_{7/2}$ band, plotted as $E_x(J)_{[45V]} - E_x(J)_{[45Ti]}$, is shown in Fig. 7. It is now well established (e.g. [2,6,7,10]) that the largest spin-dependent phenomenon contributing to Coulomb effects is the alignment or recoupling of pairs of protons from $J = 0$ to $J = 6$—the maximum allowed for an $f_{7/2}$ pair. As the spin recouples, the spatial overlap of the pair is reduced, resulting in a reduction in the Coulomb energy. This effect is typically around 100 keV for $f_{7/2}$ particles. The largest effect observed in the experimental MED plot is the rise from $\approx 30$ to $\approx 450$ keV from the lowest point around $J^* = \frac{13}{2}^-$ to the peak at $J^* = \frac{19}{2}^-$. This can be understood easily in an $f_{7/2}$ picture in terms of the proton recoupling effect as follows. In $^{45}$Ti, the odd neutron blocks the alignment of a pair of neutrons, and so a pair of $f_{7/2}$ protons recouples, eventually to the full assignment of $J = 6$. Indeed, one easily imagines the $J^* = \frac{19}{2}^+$ state in $^{45}$Ti with a configuration similar to the $J^* = \frac{7}{2}^-$ ground state but with the two protons maximally aligned to $J = 6$ rather than $J = 0$—i.e. with a significant contribution from the $[\pi(f_{7/2})^2]^{J=6} \otimes [\nu(f_{7/2})^2]^{J=7/2}$ configuration. The same is true for $^{45}$V, but swapping protons for neutrons. Thus, the alignment of protons in $^{45}$Ti (and hence neutrons in $^{45}$V) results in the MED peak at $J^* = \frac{19}{2}^-$. As the $J^* = \frac{27}{2}^-$ band-terminating state is approached, the alignment of the other type of particle is required in each case. Thus the Coulomb effects go in the opposite direction, and the MED reduces back toward zero at high spins. It is interesting to note the overall downward trend of the MED at low spins, before the alignment effect. There is no obvious intuitive explanation for this, and this anomalous low-spin behavior has been seen in a number of other cases (e.g., $A = 47$ and 49 [7]). It has been shown [10,21] that an anomalously high two-body Coulomb matrix element for $J = 2$ needs to be incorporated into the calculations to account for the experimental data. This is the so-called $J = 2$ anomaly. It is expected that this anomaly should influence the MED at low spins, and the observed low-spin variations seen in MED could be attributed, at least in part, to this anomaly. The presence of the negative dip in the MED in this $A = 45$ pair [Fig. 7(a)] from $J^* = \frac{1}{2}^-$ to $J^* = \frac{17}{2}^-$ is also consistent with the effect of this anomaly, although Fig. 7(b) indicates that the radial Coulomb effect (see below) is also important here.

FIG. 7. Mirror energy differences—defined as $E_x(J)_{[45V]} - E_x(J)_{[45Ti]}$—between states in $^{45}$V and $^{45}$Ti for the negative-parity yrast sequence as a function of spin. (a) Comparison of the experimental MED with those predicted using the full pf-shell model. (b) The three components (see text) of the predicted MED, the sum of which give the model prediction in (a).
As with other studies in this shell, the large-scale pf-shell model has been used to help interpret these data. This model, based on the work of Caurier et al. [20], has been modified (e.g. [7,15,21]) to include different Coulomb phenomena and has to date been remarkably successful in giving a quantitative description of the trends of Coulomb effects with spin. In Fig. 7 we present the results of the latest version of the model, described by Zuker et al. [21]. In this case three components of the MED are determined separately as a function of spin. These components are presented individually in Fig. 7(b), the sum of which provide the total shell-model prediction of Fig. 7(a). Details of this can be found in Ref. [21], but the principles are outlined as follows. First, the Coulomb multipole term accounts for angular momentum recoupling of protons. It uses Coulomb matrix elements determined in a harmonic oscillator basis. Second, the Coulomb monopole term accounts for Coulomb effects associated with changes in radii as a function of spin. Third, the isospin nonconserving (INC) component is an additional multipole term added for \( J = 2 \) proton couplings, the inclusion of which accounts for the \( J = 2 \) anomaly described earlier. In other cases of mirror pairs higher in the shell, the agreement with this model has been extremely good (e.g. [7,8,10]). For this \( A = 45 \) pair, however, the agreement in Fig. 7(a) is less good, and for some states (e.g., the \( J^\pi = \frac{17}{2}^- \) state) the model fails completely. Indeed, unlike in the heavier cases, there seems little to be learned from examination of the different components in Fig. 7(b). Similar difficulties were experienced [21] in describing the \( A = 46 \) mirror pair. It is suggested that for these lighter systems the full pf valence space is not appropriate and that perhaps two-particle two-hole excitations from the sd orbits below \(^{40}\text{Ca}\) need to be included.

It is of particular interest in this work to examine the MED for the \( d_{3/2} \) band, which is shown in Fig. 8. Here the MED is plotted relative to the band-head energies of the corresponding \( J^\pi = \frac{3}{2}^+ \) states. The MED shows a smooth decrease for most of the structure. It is possible to interpret this in a fairly straightforward way in terms of proton recoupling if it is assumed that (i) these structures correspond to a single \( d_{3/2} \) hole in \(^{40}\text{Ca}\) coupled to six \( f_{7/2} \) valence particles and that (ii) the trends of the MED with spin are determined entirely by the \( f_{7/2} \) particles — i.e., the \( d_{3/2} \) hole is a spectator.

This analysis can be undertaken by carefully considering the possible structure of the \( J^\pi = \frac{3}{2}^+ \) band-head state in \(^{45}\text{Ti}\). The state can be formed either from a \( d_{3/2} \) neutron excitation (i.e. \( |\pi f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} J^\pi = \frac{3}{2}^- J = 1 \) if \( |\pi f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} J^\pi = \frac{3}{2}^- J = 1 \) or from a proton excitation \( |\pi f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} f_{7/2}^\text{val} J^\pi = \frac{3}{2}^- J = 1 \). That is, the \( \sigma = \frac{1}{2} \) \( J^\pi = \frac{3}{2}^+ \) states \( A \) and \( B \) described by coupling either a \( d_{3/2} \) neutron-hole to a \( T = 1, J^\pi = 0^+ \) even-even core \(^{46}\text{Ti}\) or by coupling a \( d_{1/2} \) proton-hole to a \( T = 1, J^\pi = 0^+ \) odd-odd core \(^{46}\text{V}\). These two core states are, of course, isobaric analog states. Therefore, if we assume the approximations of perfect charge independence and pure isospin, we can determine the fractional contribution from each configuration from isospin coupling rules. The contribution depends on the square of the Clebsch-Gordan coefficient \( T_{\text{core}}^J J_{\text{core}}^T t - J_\text{core} T_\text{T} \), where \( t \) and \( t_e \) are the isospin and the isospin projection of the excited particle. The value of \((t \cdot t_e)\) turns out to be \( \frac{1}{2} \) for the former (neutron excitation) and \( \frac{1}{2} \) for the latter (proton excitation).

Following a similar argument, the \( J^\pi = \frac{3}{2}^+ \) state in \(^{45}\text{V}\) is constructed by coupling either a \( d_{3/2} \) proton-hole to a \( T = 1, J^\pi = 0^+ \) even-even core \(^{46}\text{Cr}\) or coupling a \( d_{3/2} \) neutron-hole to a \( T = 1, J^\pi = 0^+ \) odd-odd core \(^{46}\text{V}\)—again with fractional contributions of \( \frac{1}{2} \) and \( \frac{1}{4} \). (Note, these fractions are also well reproduced from shell-model calculations). Hence it is easy to show that one might expect the trend of the \( A = 45 \) MED roughly to follow \( \frac{1}{2} \) of the MED for the known \([12]\) \( T = 1 \) mirror pair \(^{46}\text{Ti}/^{46}\text{Cr}\). This crude estimate is shown in Fig. 8 (dashed curve) for comparison and, although such a comparison on a state-by-state basis cannot be quantitatively meaningful, the agreement of the overall trend up to \( J^\pi = \frac{11}{2}^+ \) is impressive. To complete the story, it should be noted that these \( T = \frac{1}{2} \) states can also be constructed by coupling a \( d_{3/2} \) hole to a \( T = 0 \) core (rather than \( T = 1 \)). However, \( T = 0 \) restricts the core to \( N = Z = 24 \text{V} \), for which the lowest \( T = 0 \) state is \( J^\pi = 3^+ \). Thus, in both nuclei, this coupling would be expected to produce a \( K^\pi = \frac{9}{2}^+ \) band head in addition to the \( K^\pi = \frac{7}{2}^+ \) band, and for states with higher spins than \( J^\pi = \frac{9}{2}^+ \) there would be two sets of states that could readily mix. Shell-model calculations performed including a \( d_{3/2} \) excitation \([38]\) suggest that these two sets of states do indeed mix. This provides an explanation for the deviation of the two curves at spins higher than \( J^\pi = \frac{11}{2}^+ \).

V. SUMMARY

A comprehensive new high-spin level scheme of the proton-rich nucleus \(^{45}\text{V}\) including both negative-parity states built on \( f_{7/2} \) configurations and a collective positive-parity structure built on a \( d_{3/2} \) particle-hole excitation has been established. Comparisons with the mirror partner \(^{45}\text{Ti}\) have been made, and the mirror energy, differences established and analyzed

![FIG. 8. Mirror energy differences between states in \(^{45}\text{V}\) and \(^{45}\text{Ti}\) for the positive-parity sequence as a function of spin. The dashed curve shows the experimentally observed MED \([12]\) for the \( A = 46 \) mirror pair \((^{46}\text{Cr}/^{46}\text{Ti})\) multiplied by a factor of 0.66 (see text).](image)
in terms of Coulomb phenomena. In particular, the MED of the structures built on the particle-hole excitation have been interpreted in terms of a core-hole coupling picture based on isospin coupling rules. The $E1$ decay pattern observed in the mirror pair does not follow the same symmetry picture seen for the $M1/E2$ transitions. This appears to be an emerging phenomenon that needs to be investigated both experimentally and theoretically.

**ACKNOWLEDGMENTS**

The authors particularly thank the accelerator staff at the Vivitrion facility at IReS Strasbourg for their enormous efforts in producing the difficult $^{24}\text{Mg}$ beam needed for this run. This work was supported by the United Kingdom Engineering and Physics Sciences Research Council, the Swedish Research Council and the European Union through contract EUROVIV: HPRI-CT-1999-00078.